

Complex Adaptive Systems

Examples from Biology with Computer Science Applications

Lecture 14

Ant Colonies

Evolution of Altruism (compare Axelrod and
The prisoners dillema)

Is Altruism a Nash Equilibrium?

Ant defection.

Ants evolved from wasps about 100 million years ago.

There are an estimated 22,000 species.



E. O. Wilson
Harvard University

Bert Hölldobler
University of Würzburg

*The Superorganism: The Beauty,
Elegance, and Strangeness of
Insect Societies*

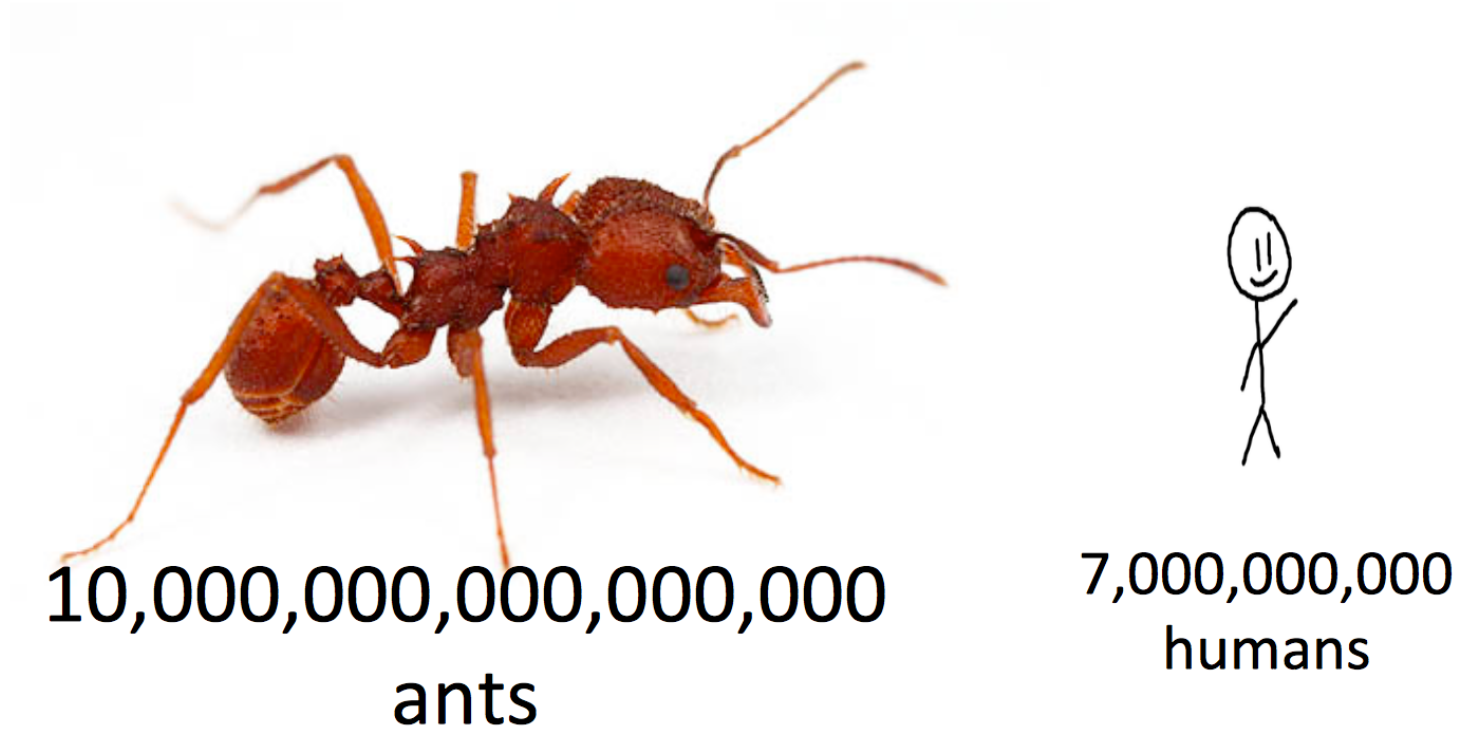
The Ants

Insect Societies



Deborah Gordon
Stanford University
Compares ant foraging
To TCP/IP throttling
(Desert Harvester and
Argentine Ants)

Planet of the Ants



10 quadrillion ants.

7 billion humans.

“Lean on a tree almost anywhere, and the first creature to crawl on you will probably be an ant.”

Holldobler & Wilson, *Journey to the Ants*

QUEEN ANT



Queen ants are the founders of all colonies. Once mated, she can stay fertilized for many years laying millions of eggs. Some queens can lay thousands of eggs each day. They really are egg laying machines. In some species live up to 30 years. Some species have multiple queens.

Worker Ants



Worker ants are sterile females. Can live up to 5 years. In *Pogonomyrmex* sp. the jobs the workers do depend on age not caste.

Winged Princess | Alate | Virgin Queen



Mate with a drone during the nuptial flight. Stores enough sperm for the rest of her life. Her job is to find a good place for the colony, clip her own wings off and burrow as quickly as possible. Once underground she starts producing workers.

Winged Drone | Alate | Male Ant



These are the only males in the colony. Males are haploid (only one set of chromosomes). Leave the colony during the nuptial flight and then die.

Basic Ant Biology

- All ants are **eusocial**
 - The colony is the unit of selection
 - Queen(s): reproducers, not masterminds
 - Reproductives: winged male and female alates
 - Workers: female, short lived compared to queens
 - Genetic sex determination
 - Haplodiploidy
 - Sociobiology
 - Division of labor:
 - All males are reproductive
 - Female **caste** determined by environment & larval feeding
 - Assignment to task groups is determined by colony need
 - Emergence of cooperative foraging, learning, farming, herding..
- Communication through **pheromones and antennal contact**
- **Self organization** (dumb ants, smart colonies)



Haplodiploid sex determination

- Sex is determined by the number of sets of chromosomes
 - Females are diploid: usual case in sexual reproduction: genes are inherited from mother + father
 - Males are unfertilized: all genes come from the egg (mother)
 - Males have $\frac{1}{2}$ the number of chromosomes as females (haploid)
 - Males have no fathers and can only produce daughters
 - The queen determines* how many males and females to make
- Female workers could produce sons, however, females are more related to their sisters (queens produced by her colony) than to their sons

| <u>Sex</u> | Daughter | Son | Mother | Father | Full Sister | Full Brother | |
|------------|---------------|---------------|---------------|---------------|---------------|---------------|--|
| F | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{3}{4}$ | $\frac{1}{4}$ | |
| M | 1 | - | 1 | - | $\frac{1}{2}$ | $\frac{1}{2}$ | |

This depends on all the offspring of the queen resulting from a single mating.

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This depends on all the offspring of the queen resulting from a single mating.

How does this relate To Nash Equilibrium?

20 ants per colony



© alexanderwild.com

20 MILLION ants per colony



20 MILLION ants per colony

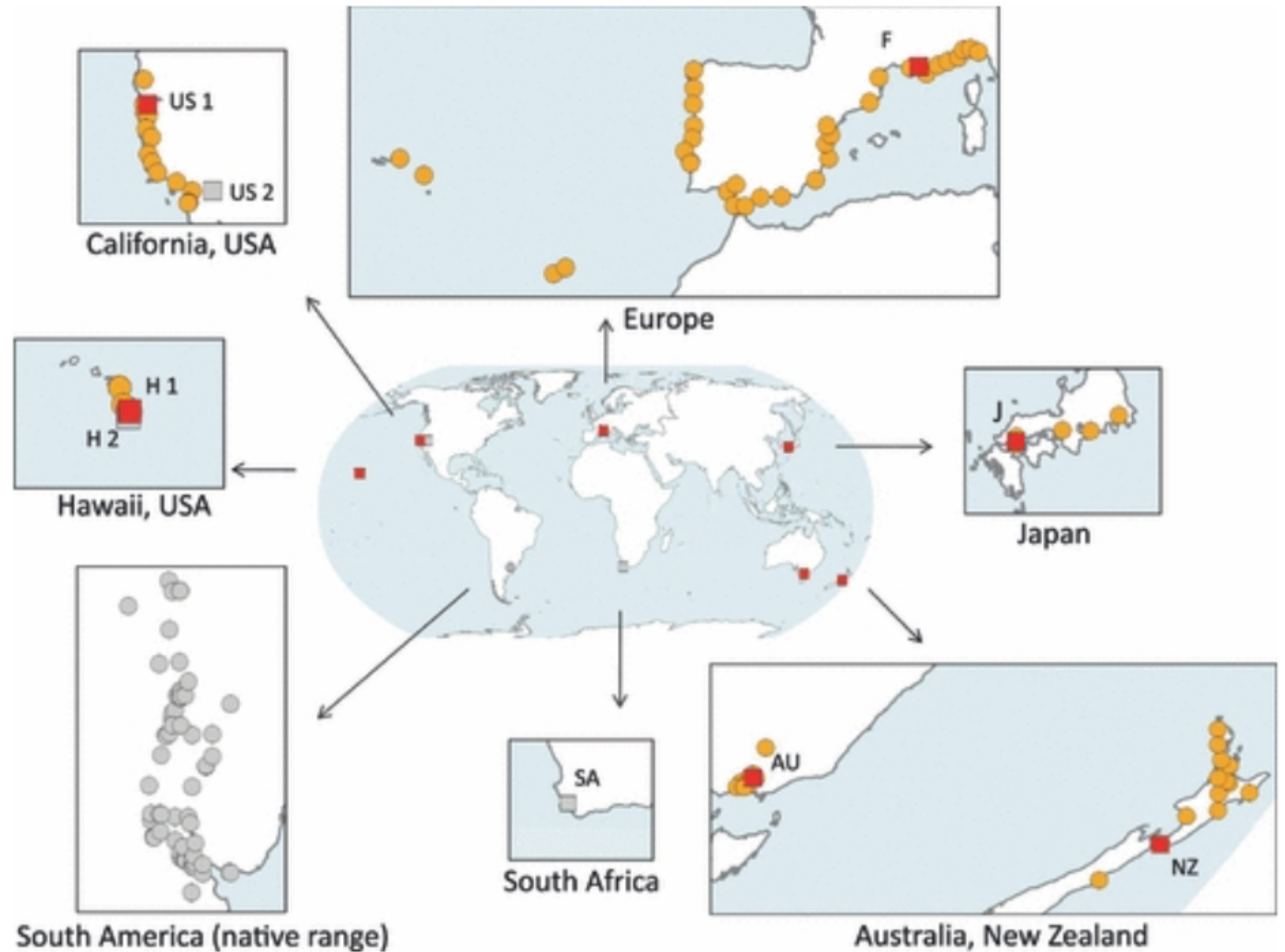


No foreman, no blueprints, no one is in charge

Cooperation

- Most ants use chemical signals to mark divisions between colonies.
- Argentine ants create multiple nests.
- Humans accidentally transported colonies of ants from South America around the world
- . Since there were no other Argentine ant colonies to compete with those founder ants have expanded one giant colony in each region.
- These are called super or mega-colonies.

The largest of these Argentine ant Supercolonies is 6,000 km long (Europe).



Van Wilgenburg, Ellen, Candice W. Torres, and Neil D. Tsutsui. "The global expansion of a single ant supercolony." *Evolutionary Applications* 3.2 (2010): 136-143.

Cooperation in Superorganisms



4 simple behaviors → cooperative foraging

- **Count**
- Remember
- Communicate
- Move



Steps



Seeds



Interactions

4 simple behaviors → cooperative foraging

- Count
- **Remember**
- Communicate
- Move

Site Fidelity

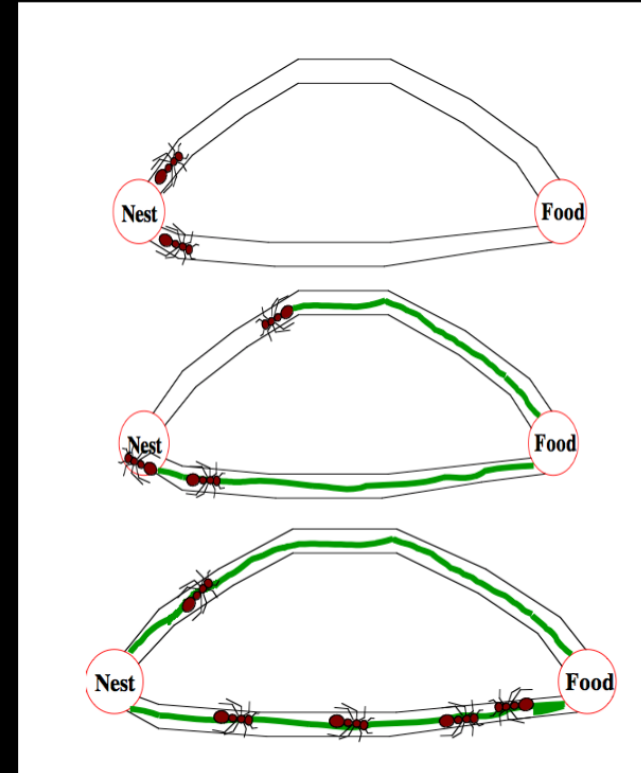
There and back again...and again



4 simple behaviors → cooperative foraging

- Count
- Remember
- **Communicate**
- Move

Pheromones

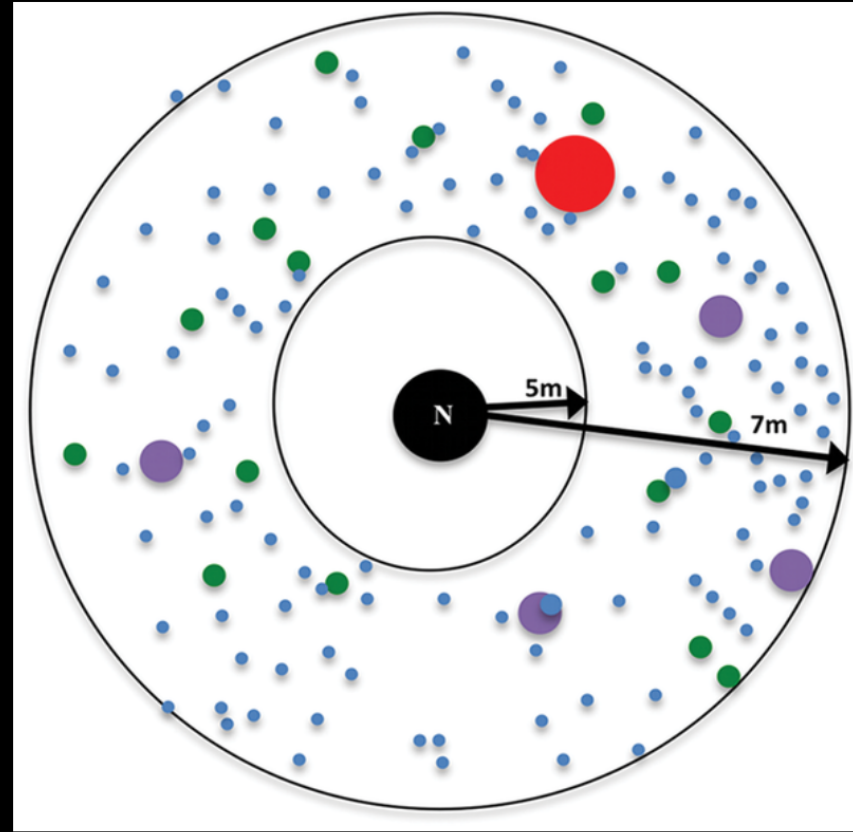


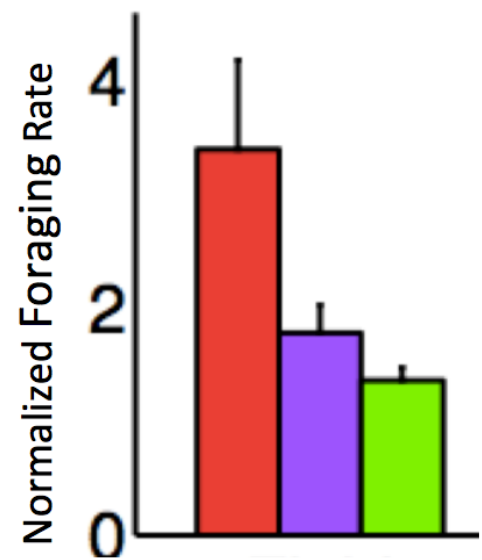
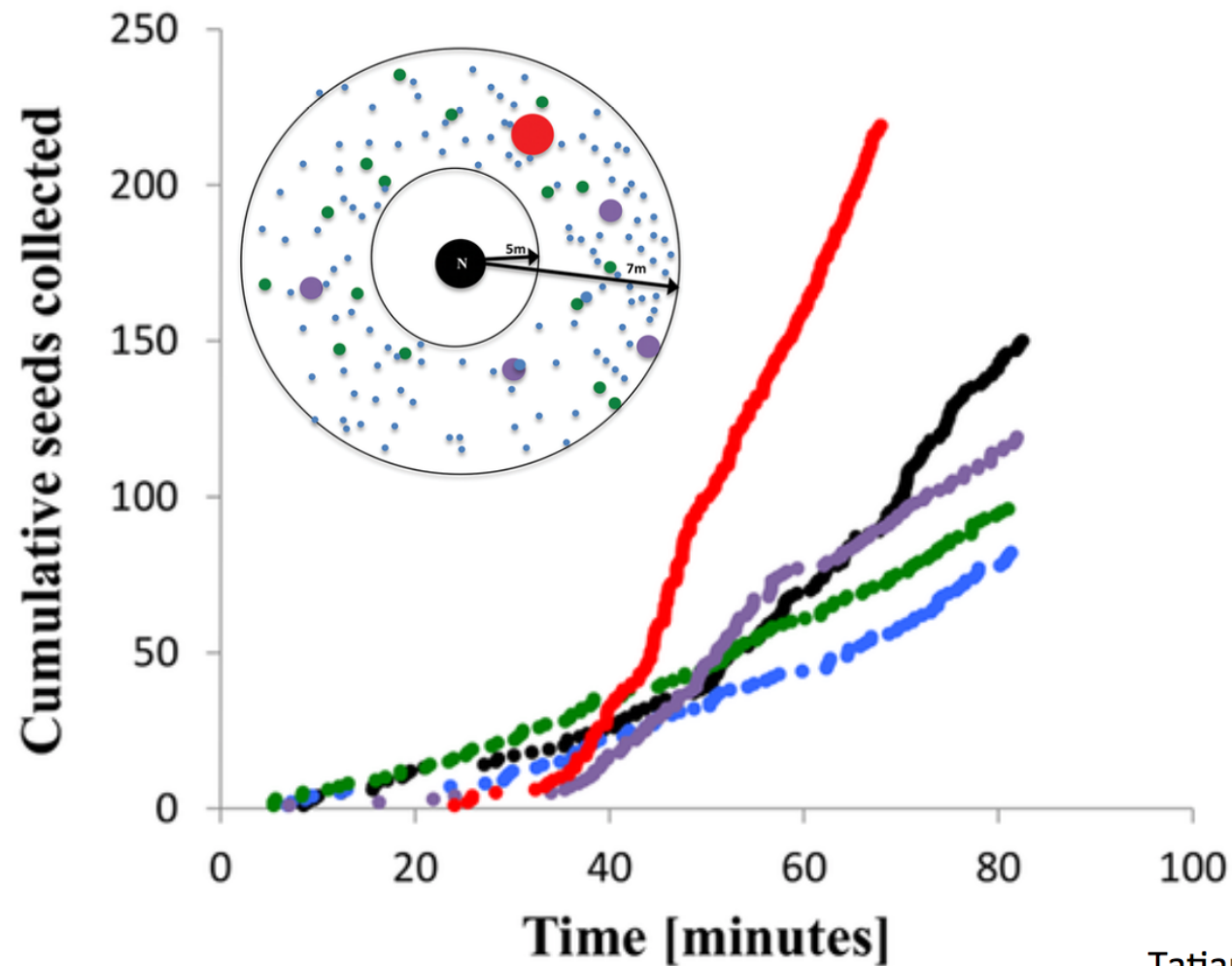
4 simple behaviors → cooperative foraging

- Count
- Remember
- Communicate
- **Move**
 - Travel
 - Search
 - Thoroughly
 - Broadly



How does complex foraging emerge from interactions among these 4 behaviors?

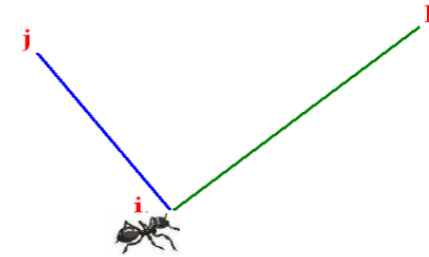
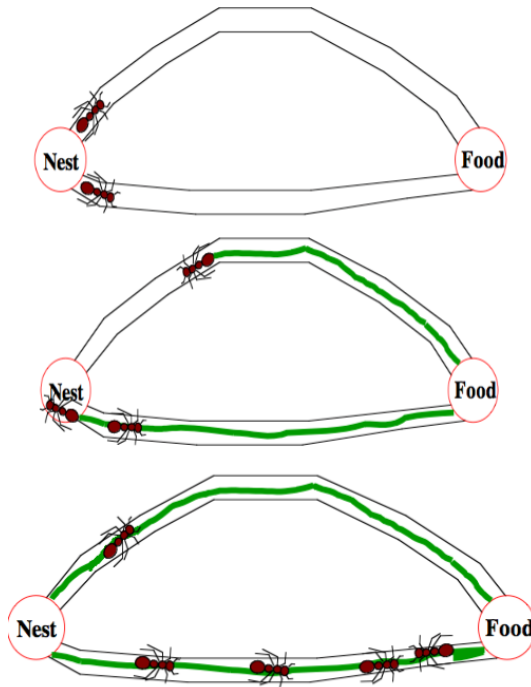




Tatiana Flanagan et al Alife 2011, PLoS ONE 2012

How should ants behave to collect seeds as fast as possible?

Pheromone recruitment: a well-studied emergent behavior



$$p_{ij}^k(t) = \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{l \in N_i^k} [\tau_{il}(t)]^\alpha \cdot [\eta_{il}]^\beta} \quad \text{if } j \in N_i^k$$

Ant colony optimization

Memory vs. Communication

Site Fidelity

There and back again



Memory vs. Communication

private vs. public information

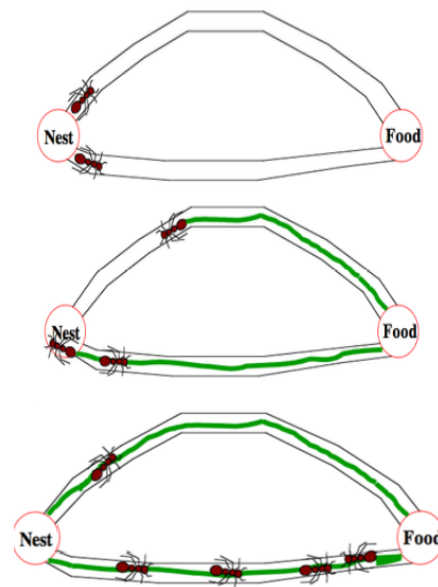
Site Fidelity

There and back again



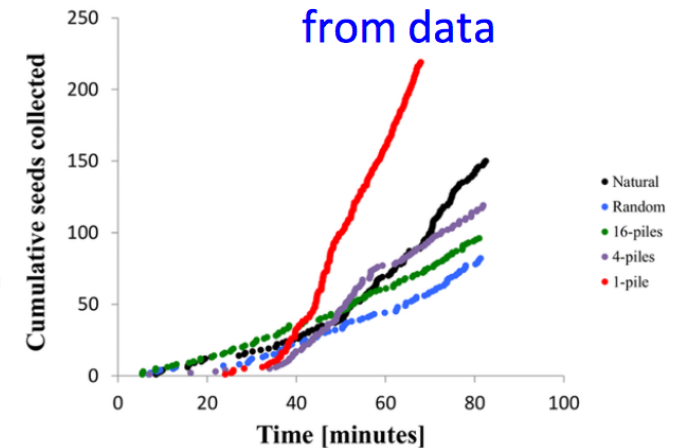
Pheromone Communication

Recruit nestmates



$$p_{ij}^k(t) = \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{l \in N_i^k} [\tau_{il}(t)]^\alpha \cdot [\eta_{il}]^\beta} \text{ if } j \in N_i^k$$

Both processes are
indistinguishable
from data



Agent Based Model

How important is remembered vs. communicated information?

Ants search for food on a grid

Travel from the nest

Move with directed & random walks

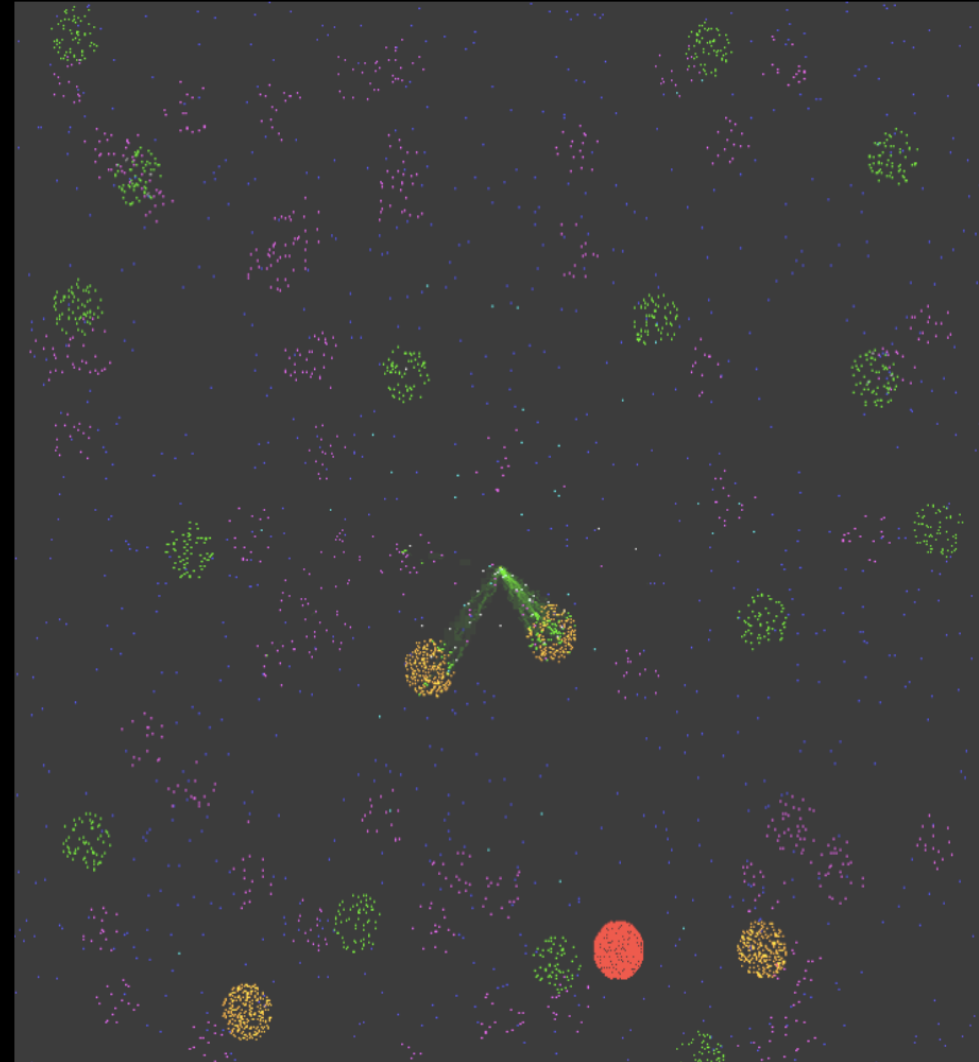
Upon finding food, ants

Count the seeds nearby

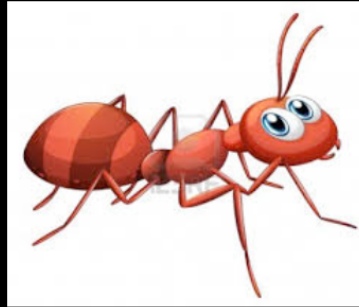
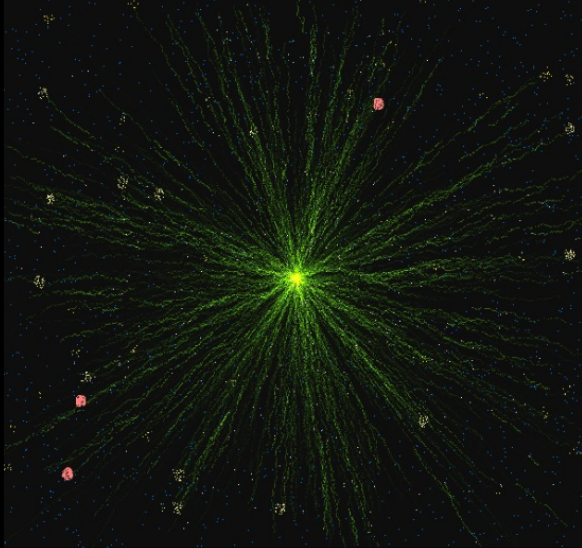
Decide whether to use

- memory (site fidelity) or
- communication (pheromones)

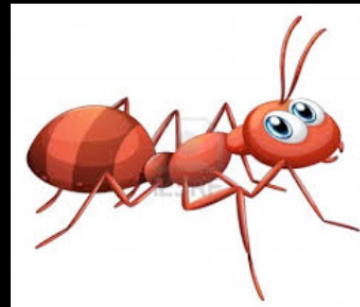
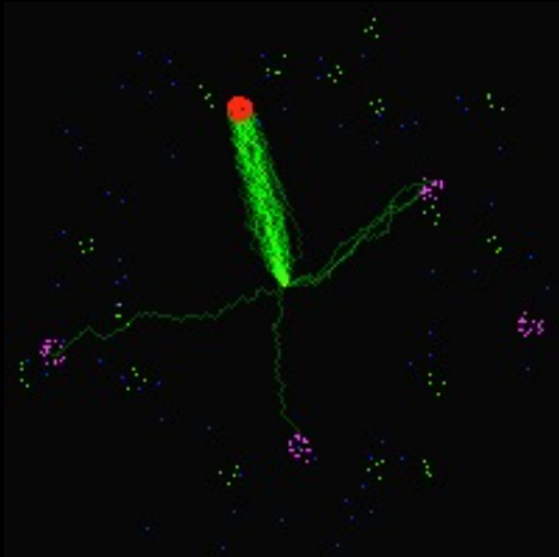
GOAL: Combine behaviors in individuals to maximize seeds collected by colony



Foraging success depends on interactions among behaviors



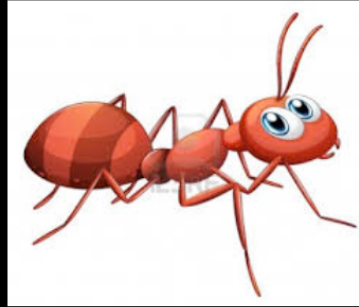
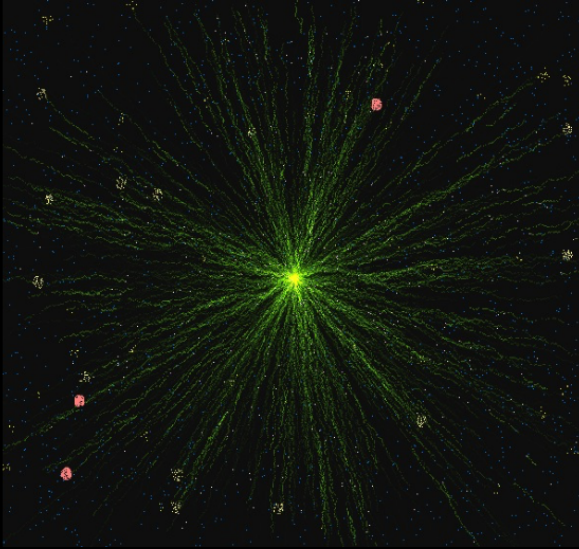
Lay pheromone
Whenever I find a seed



| | | | | |
|--|----|---|----|--|
| | | | | |
| | NW | N | NE | |
| | W | C | E | |
| | SW | S | SE | |
| | | | | |

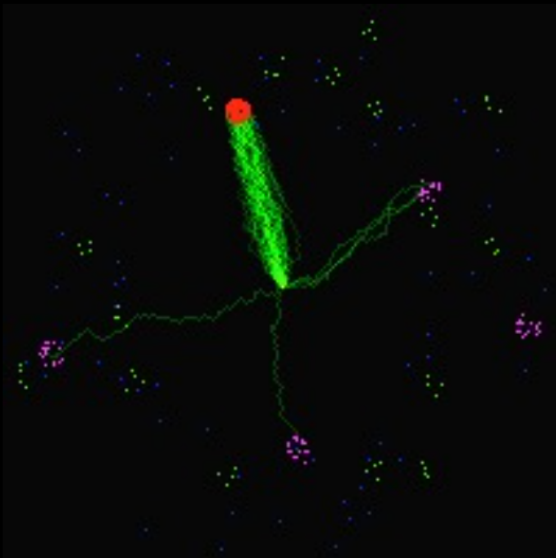
Lay pheromone
Only if count > 5

Foraging success depends on interactions among behaviors

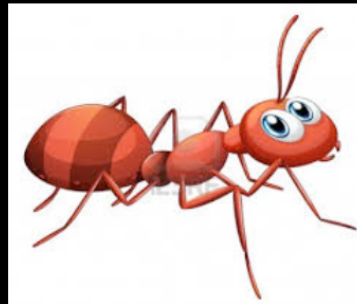


Lay pheromone
Whenever I find a seed

Decision to lay pheromones or use site fidelity
depends on seed density in the current pile



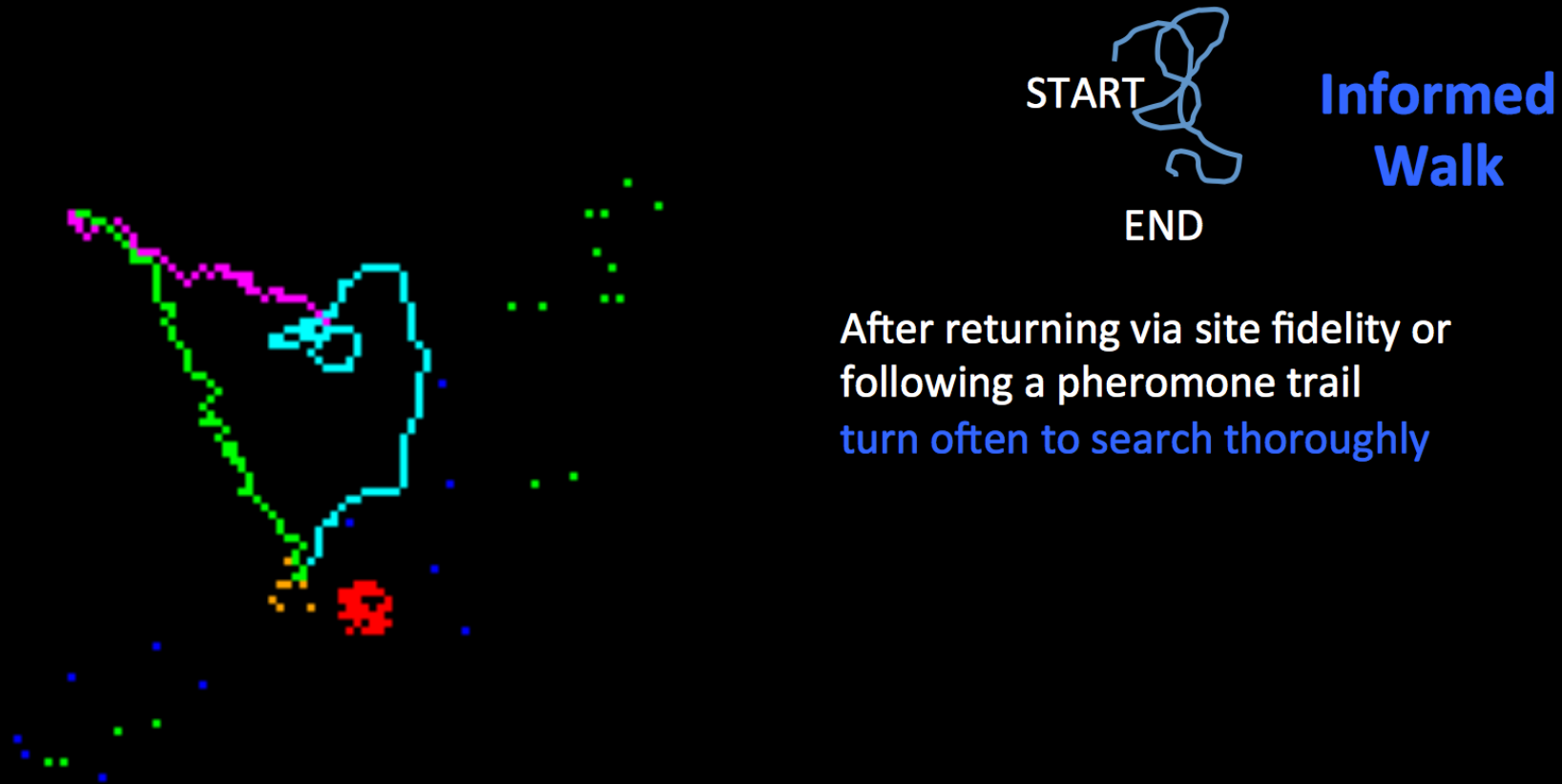
Communication & memory interact with counting



| | | | | |
|--|----|---|----|--|
| | | | | |
| | NW | N | NE | |
| | W | C | E | |
| | SW | S | SE | |
| | | | | |

Lay pheromone
Only if count > 5

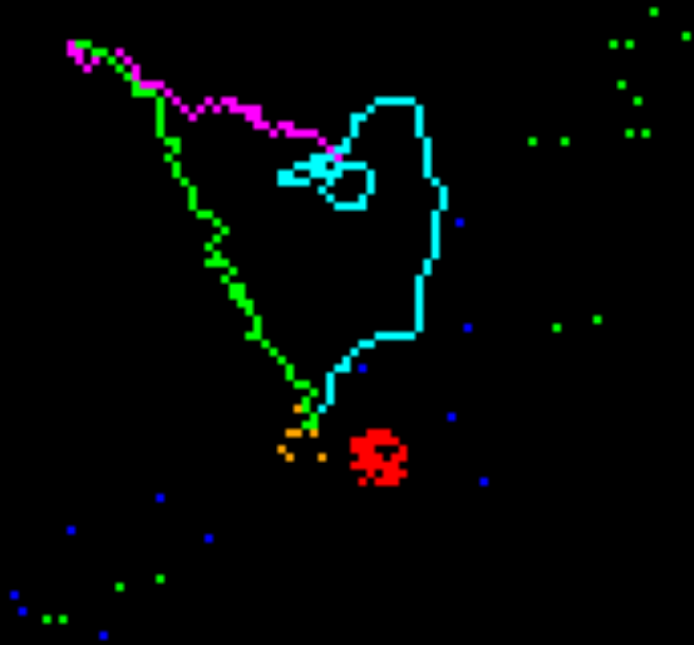
Foraging success depends on interactions among behaviors



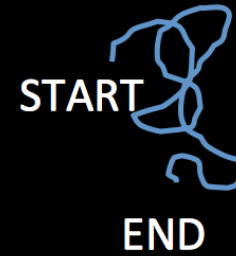
After returning via site fidelity or following a pheromone trail
turn often to search thoroughly

Movement interacts with
communication & memory

Foraging success depends on interactions among behaviors



Movement interacts with communication & memory



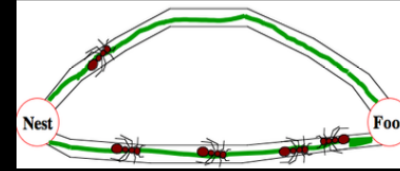
Informed Walk

After returning via site fidelity or following a pheromone trail turn often to search thoroughly



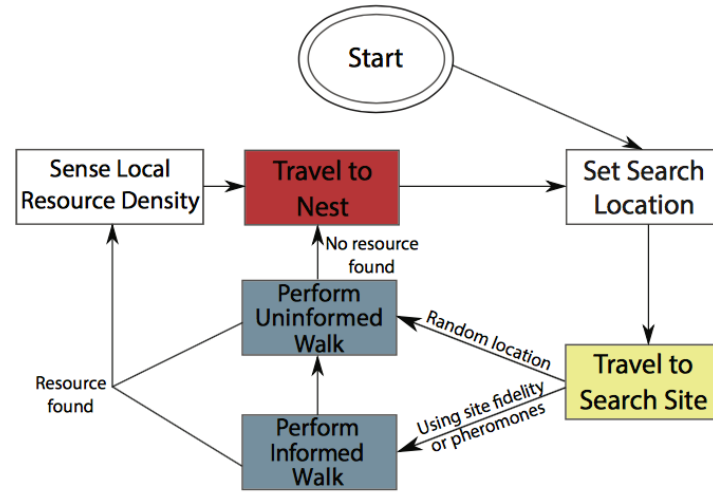
Uninformed Walk

When searching at random, walk in persistent directions to search widely



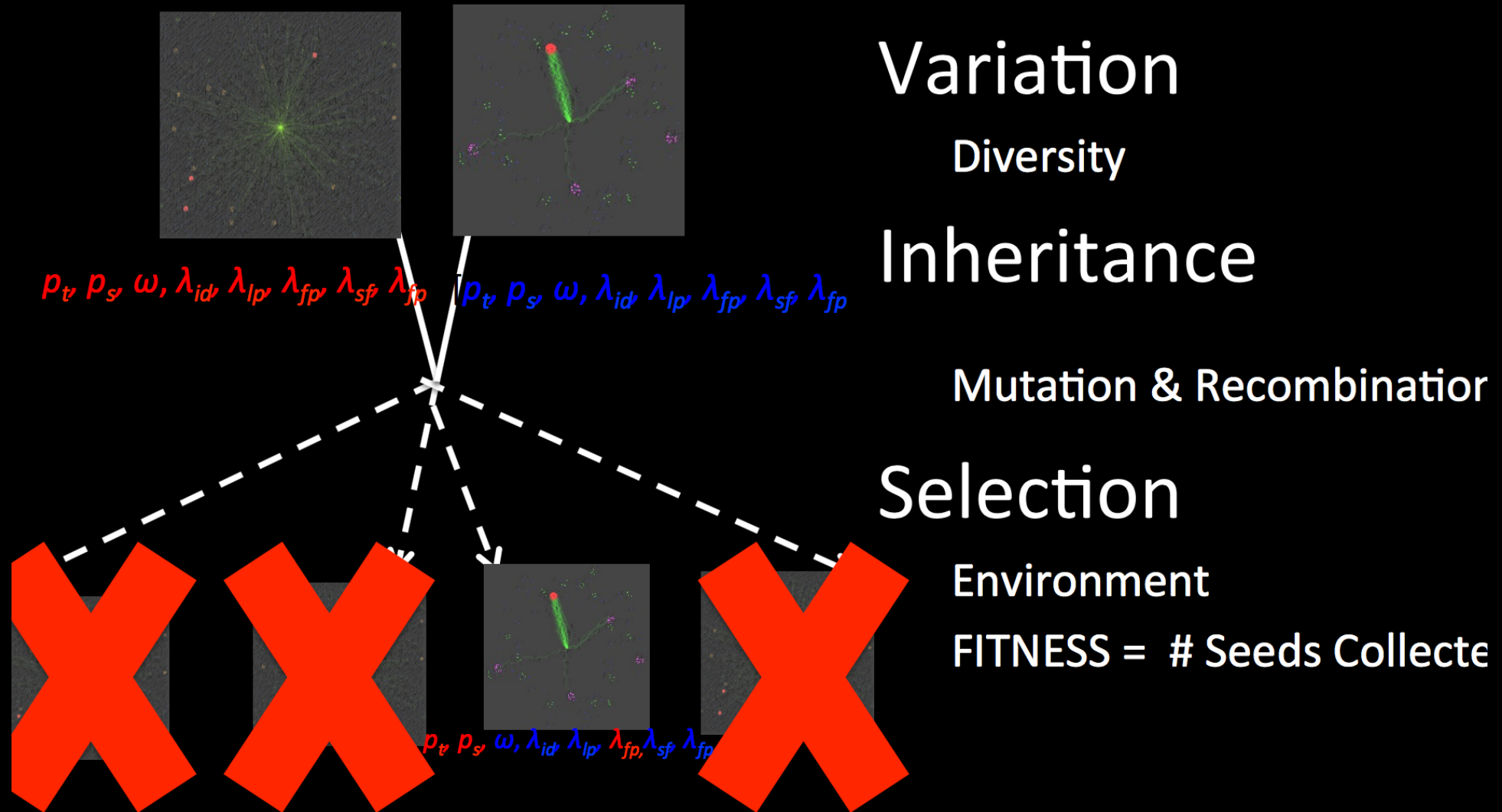
Collective Foraging success depends on **interactions**
among ants
and
between ants & their environment

Computer algorithms “evolve” ant behaviors
to maximize seed collection in fixed time

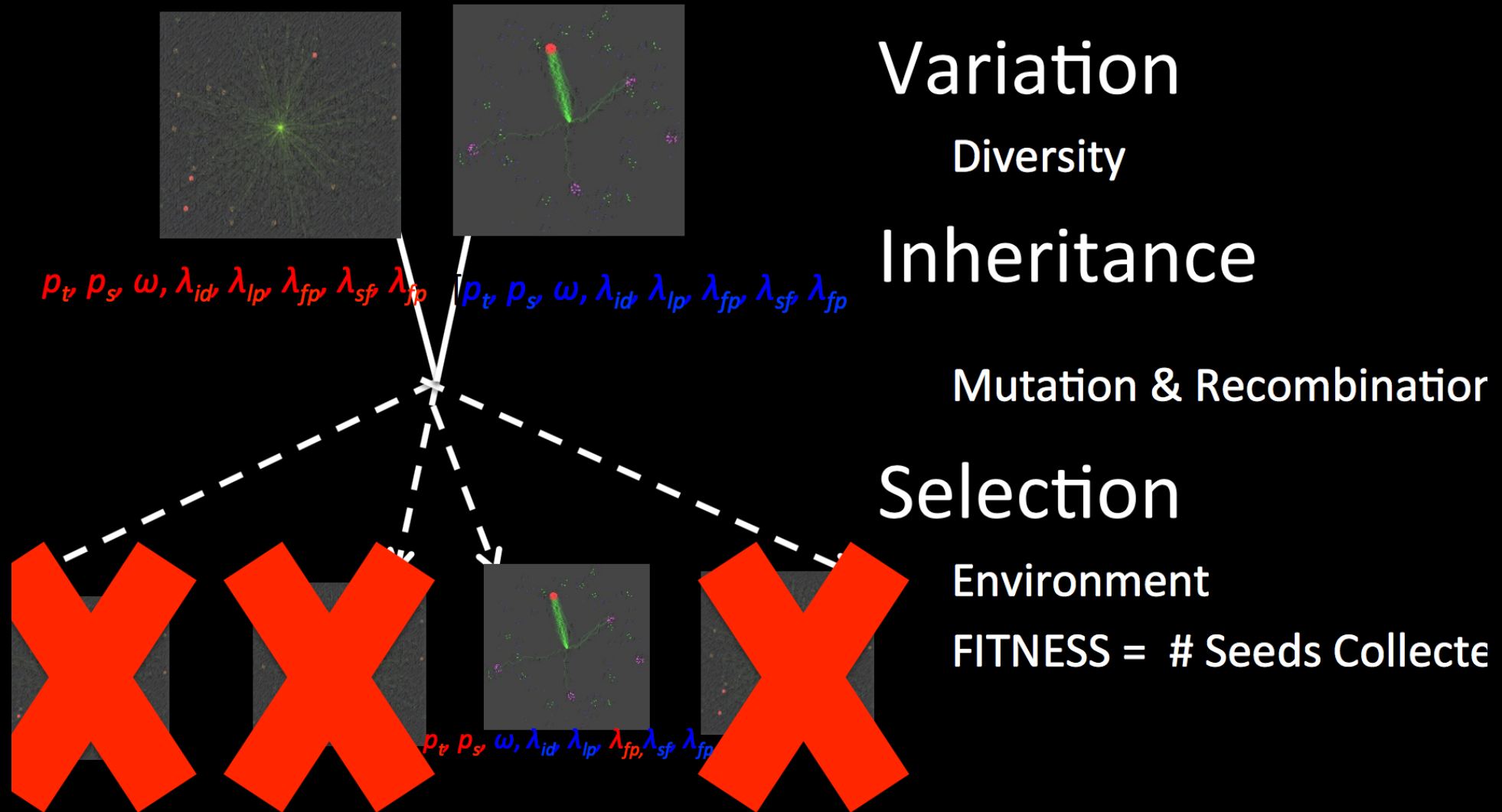


| Parameter | Description | Function |
|----------------|---------------------------------------|-------------------------------------------------------------|
| p_t | Probability of switching to traveling | — |
| p_s | Probability of switching to searching | — |
| ω | Uninformed search correlation | $\sigma = \omega$ |
| λ_{id} | Informed search decay | $\sigma = \omega + (4\pi - \omega) * e^{-\lambda_{id} * t}$ |
| λ_{lp} | Rate of laying pheromone | $F_{lp}(x) = 1 - e^{-\lambda_{lp} * (x+1)}$ |
| λ_{fp} | Rate of following pheromone | $F_{fp}(x) = 1 - e^{-\lambda_{fp} * (9-x)}$ |
| λ_{sf} | Rate of site fidelity | $F_{sf}(x) = 1 - e^{-\lambda_{sf} * (x+1)}$ |
| λ_{pd} | Rate of pheromone decay | $e^{-\lambda_{pd} * t}$ |

Genetic Algorithms



Genetic Algorithms



GA selects parameters to maximize seeds collected in fixed time

Group Selection Experiments *in silico*

Each model run requires a set of input parameters $[p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}]$

Each individual in a colony is identical

Cross over and mutation on parameters

G0: $[p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}] \times [p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}]$

G1: $[p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}]$

100 runs with different parameter sets (colonies) for 100 Generations

Each colony, each generation, evaluated on 8 grids for 20,000 time steps

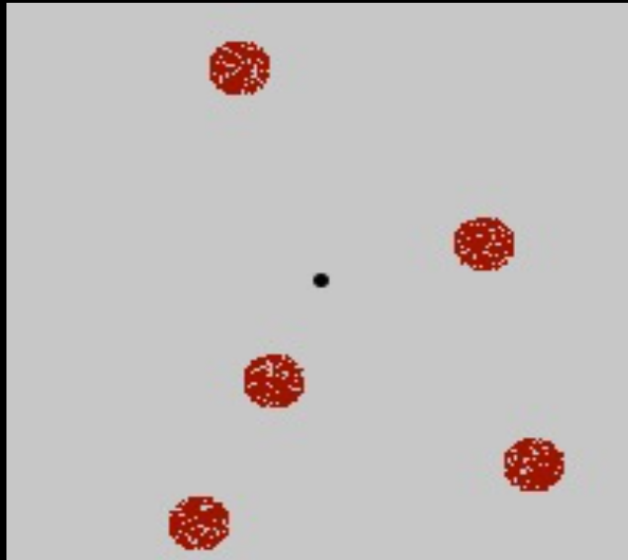
Colonies with highest 'fitness' (seeds collected) replicate into next generation

Run for colony sizes 10, 100, 1000, 10,000 foragers

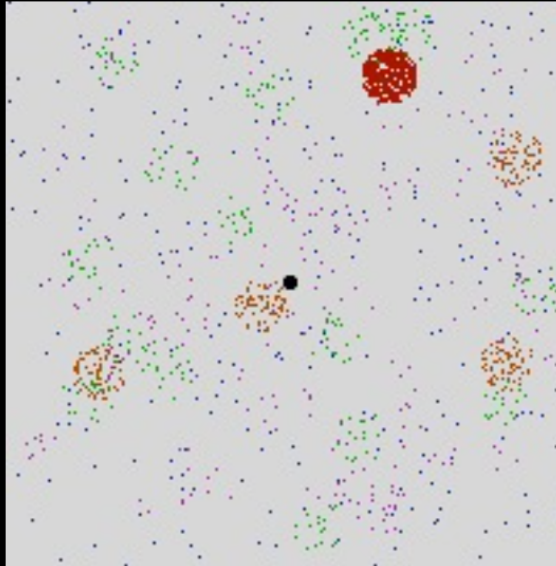
RESULT: Simulated colonies 'evolved' to maximize foraging rate

Simulated colonies evolve to collect from different environments

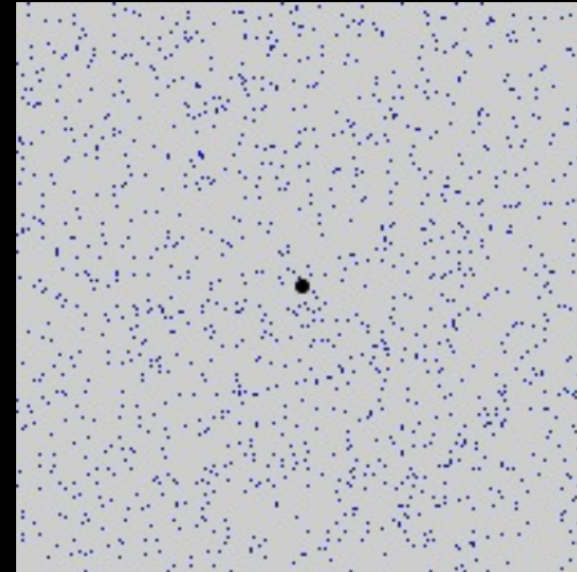
Big Piles



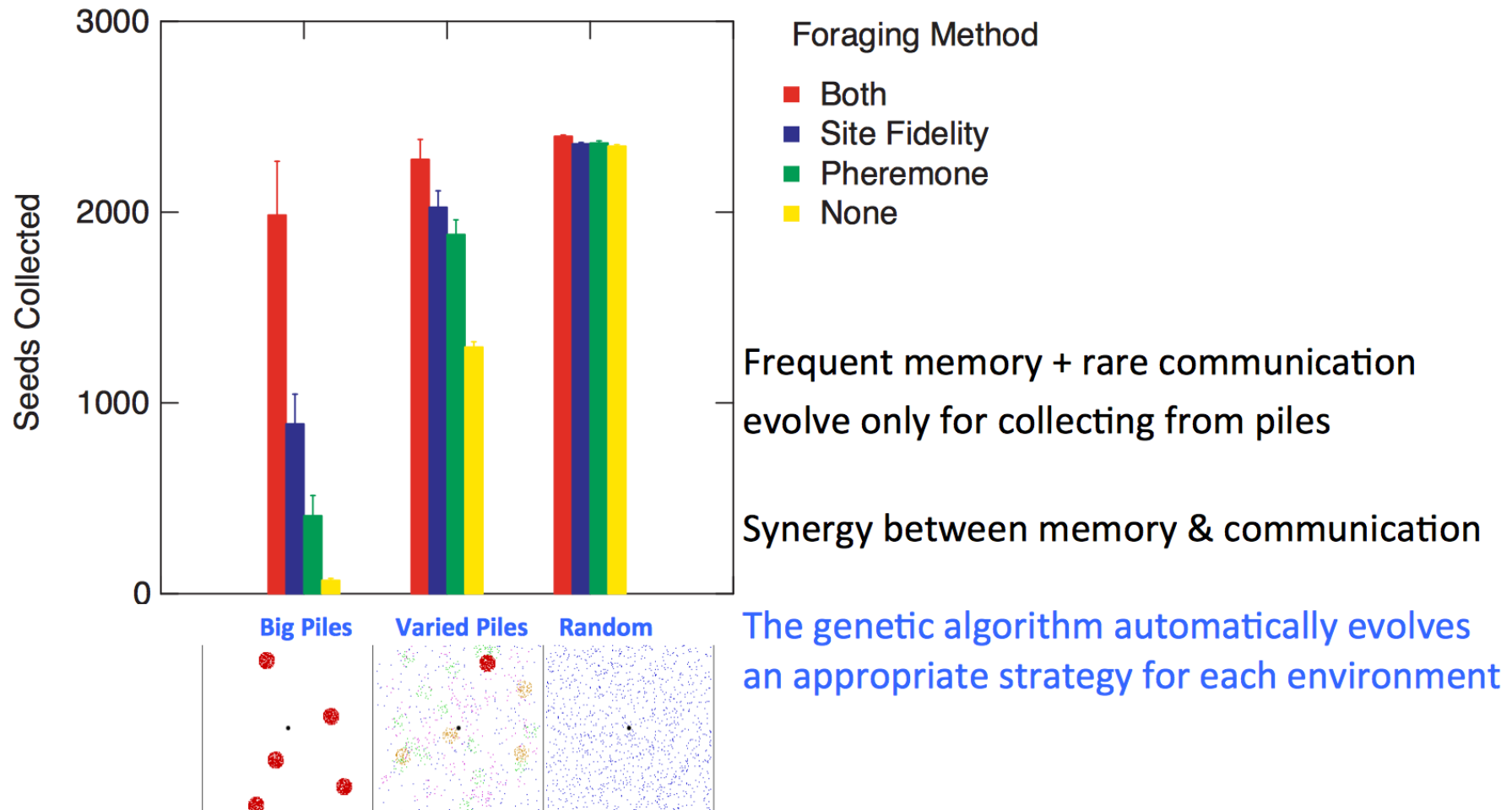
Varied Piles



Random

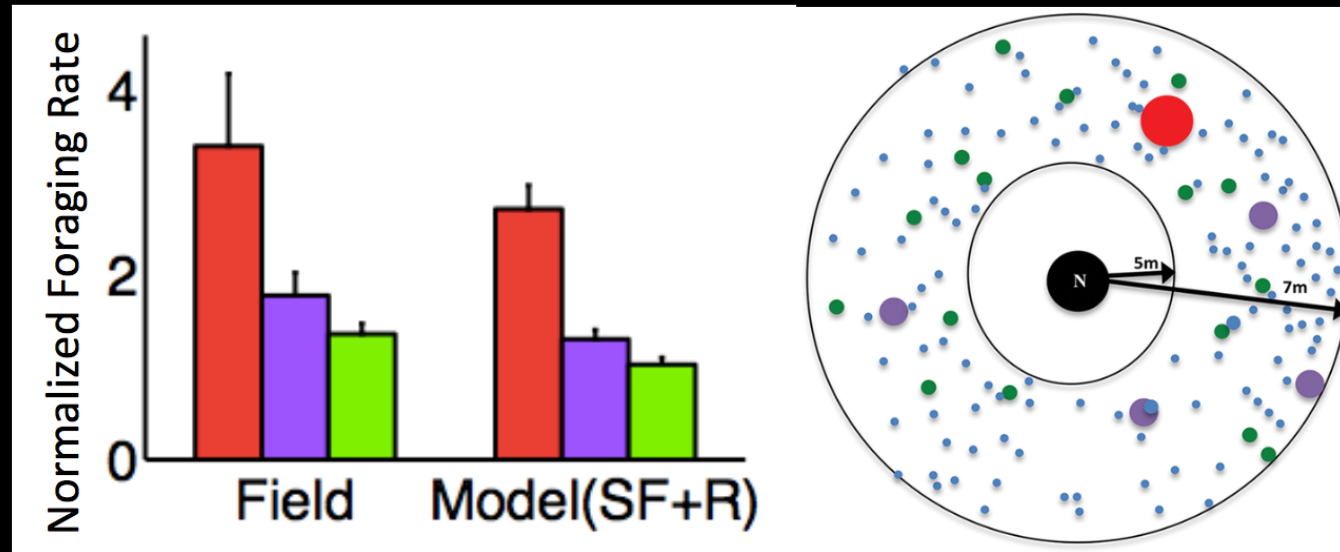


Different strategies are useful in different environments

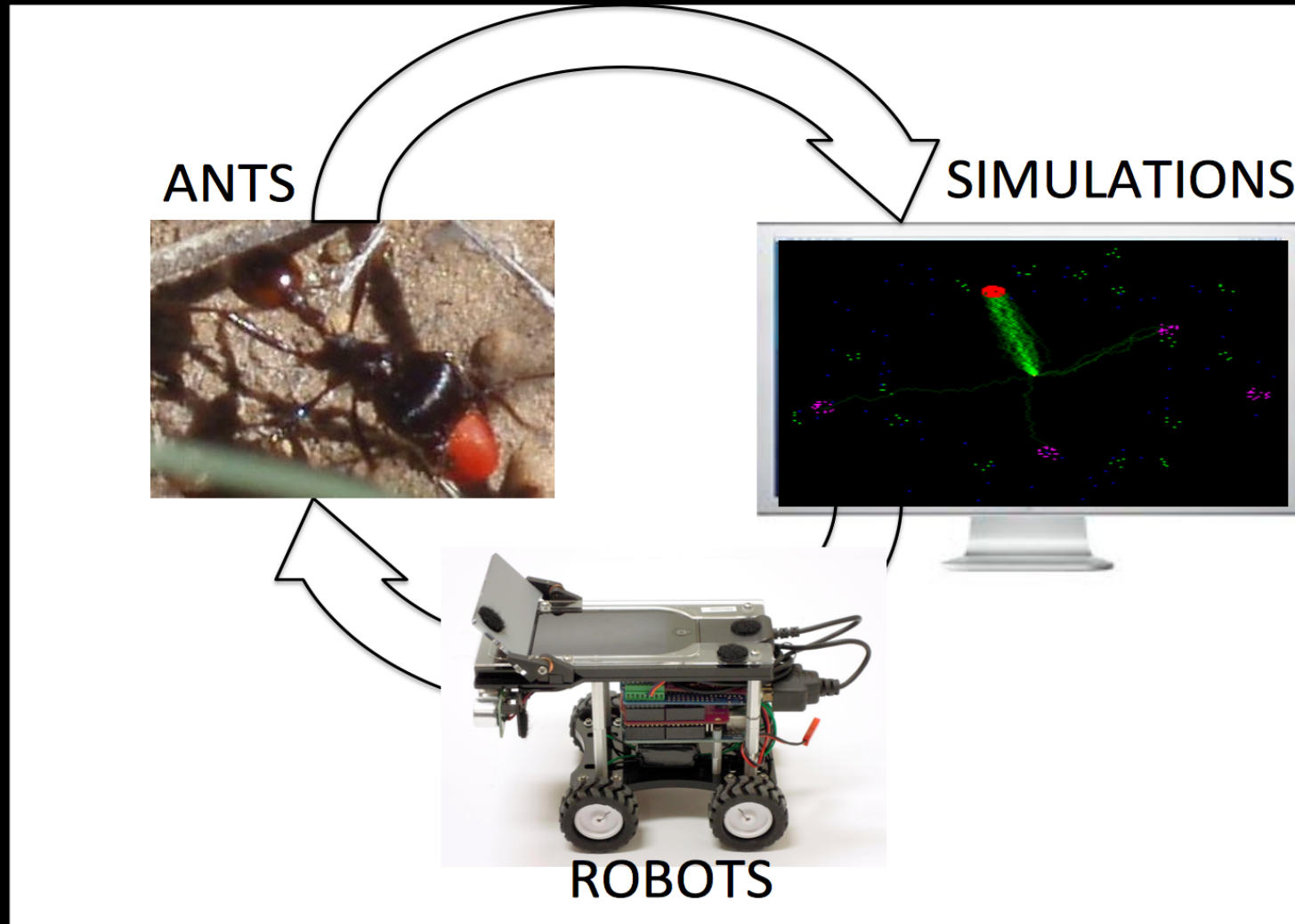


Real ants forage as efficiently as simulated ants

Simulations reveal interactions among ants and their environment that lead to efficient foraging



Program robots to cooperate using ant-like behaviors

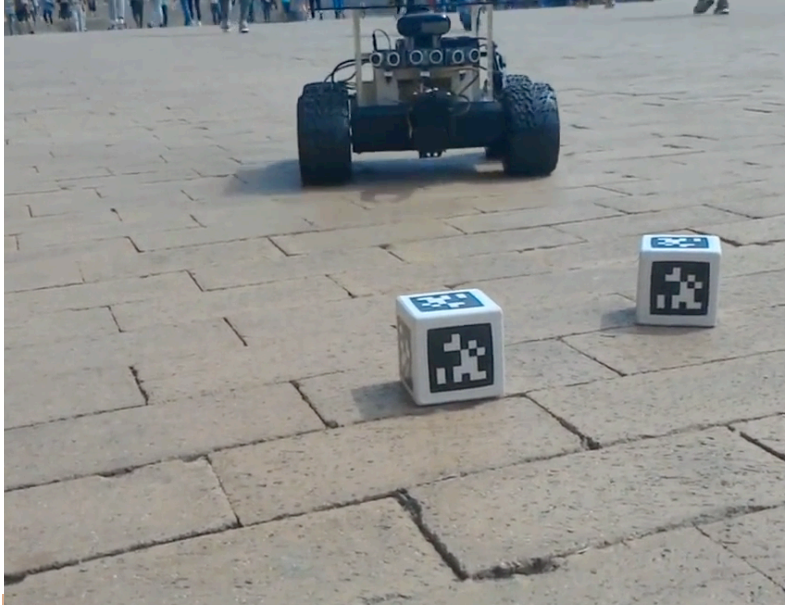


iANT SWARM ROBOTS

How can robots cooperate to search effectively
in variable environments with noise, error,
and no one in charge?



Problem we are trying to solve: **Central Place Foraging**

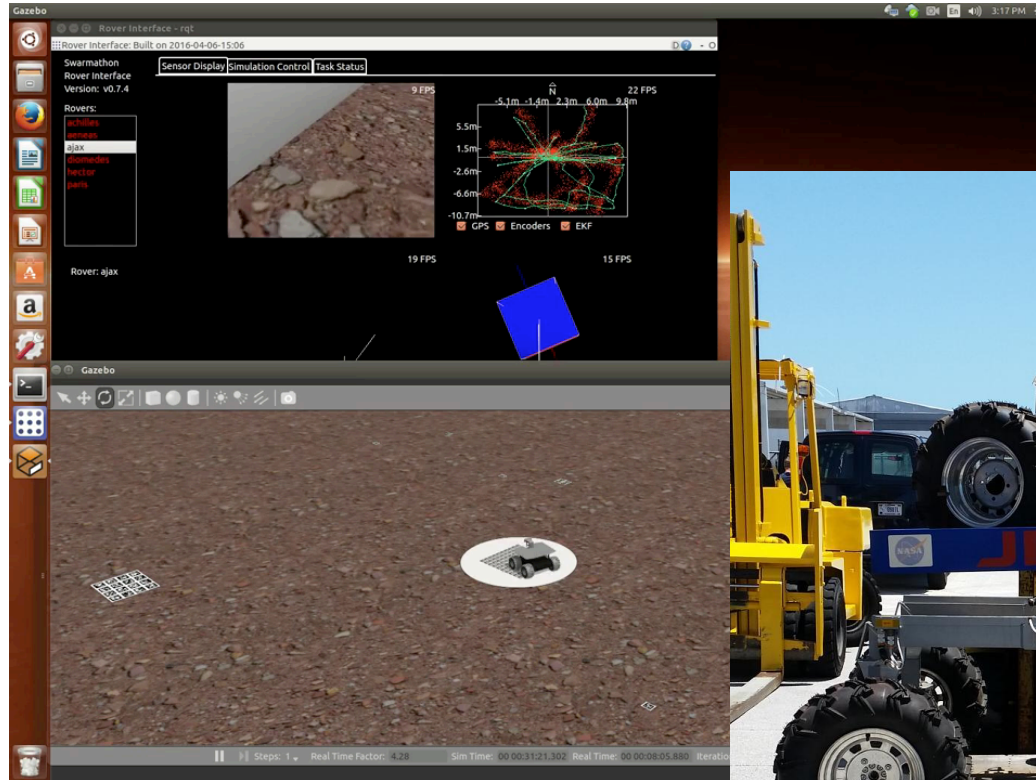


Introduction

‘Living off the land’ - Mars 2030



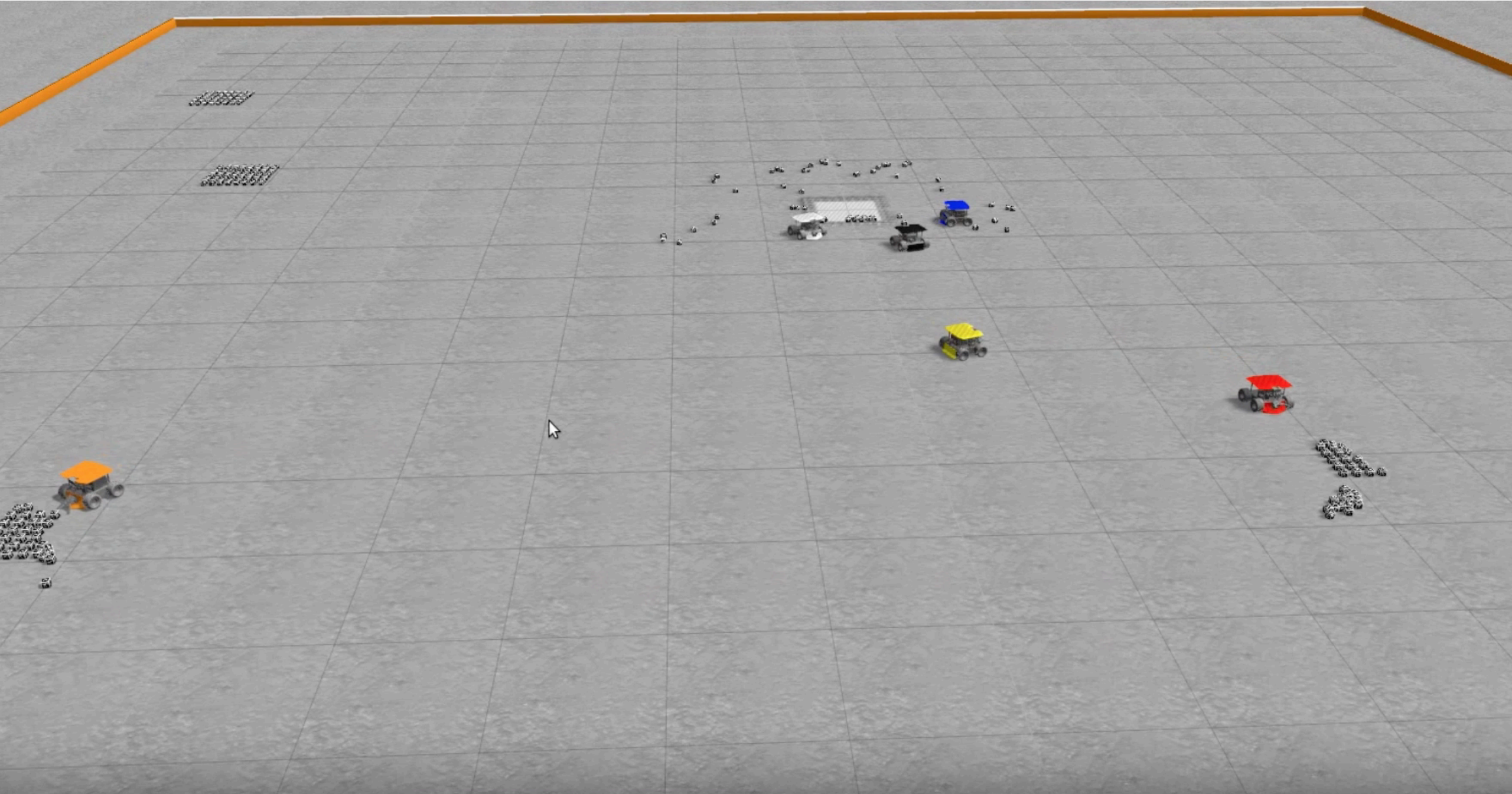
nasaswarmathon.com

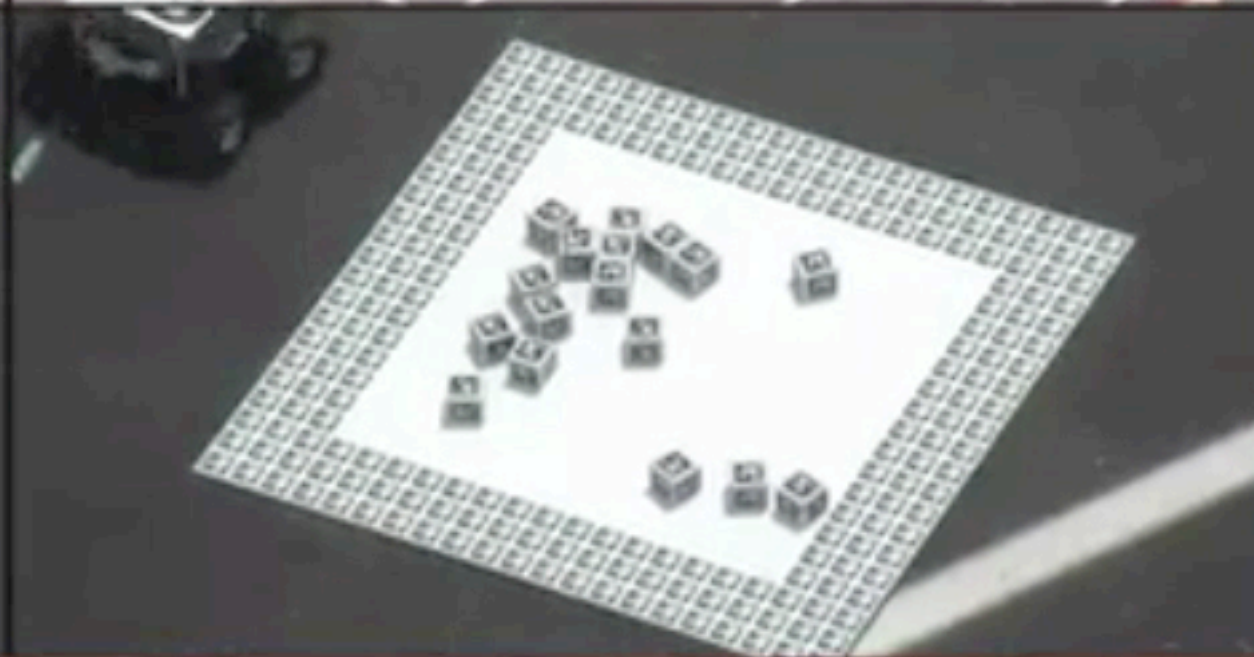
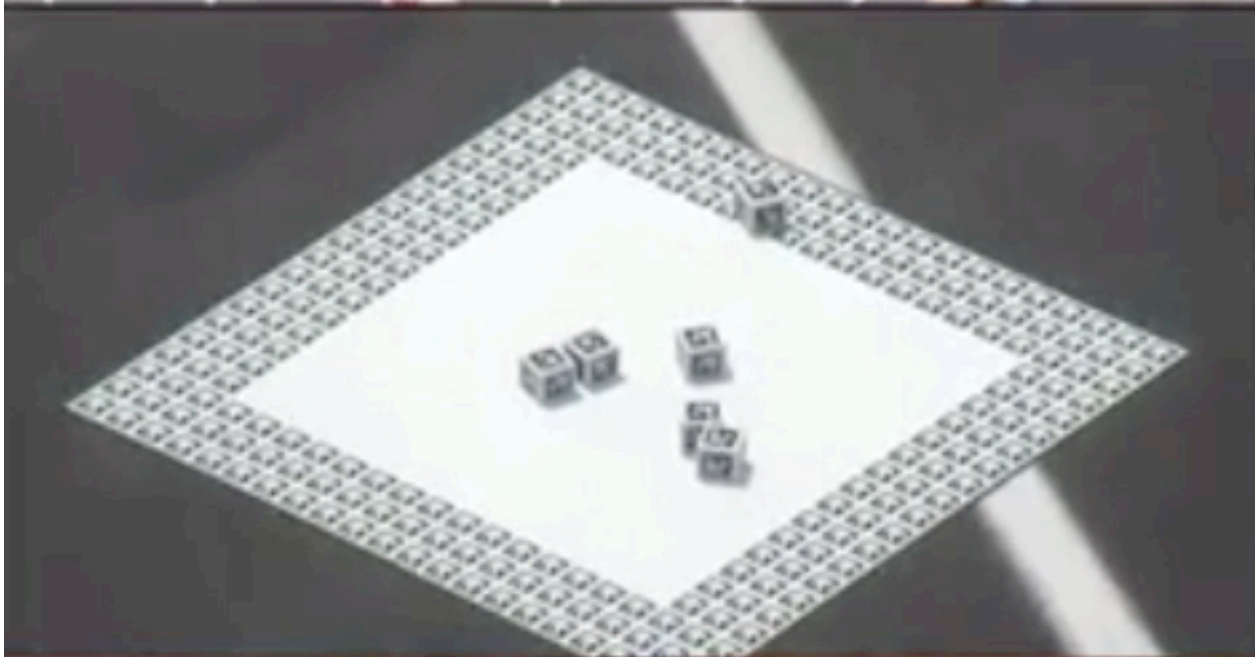


Managed by UNM, 40 colleges
and universities competed
Build ~100 robots so far...

Introduction





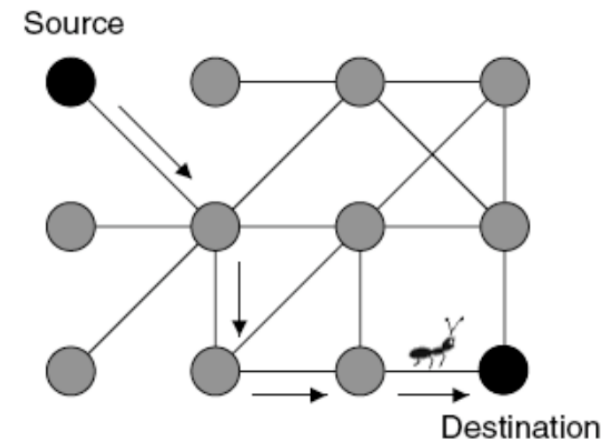


Ant Colony Optimisation (ACO)

Key Concepts From Dorigo's ACO

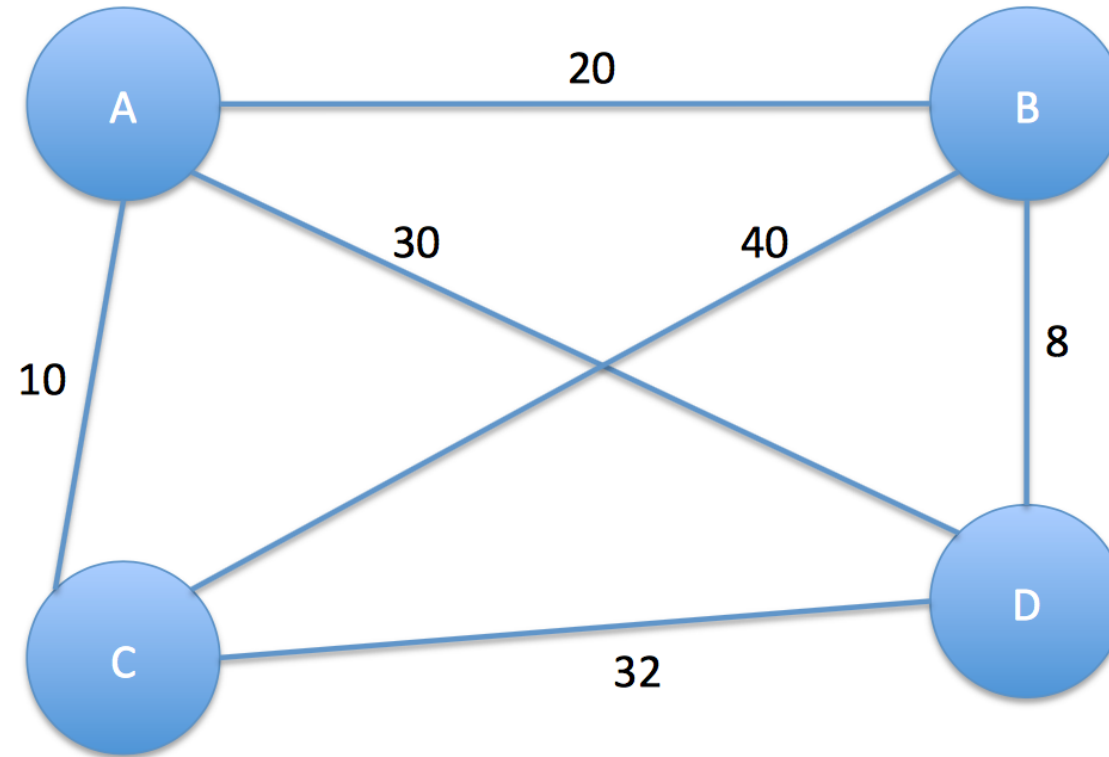
- Ant algorithms use 'self-organizing principles' to coordinate agents to solve computational problems
- Stigmergy: indirect communication and coordination through signals that modify the environment and stimulate other agents
- Pheromones: a chemical signal that triggers a response in another agent
 - Pheromone concentration increases the probability that an ant will follow a path
 - Evaporation removes stale solutions and mitigates premature convergence

Simple-ACO



- S-ACO modifications of previous models
 - Ants remember their paths
 - Only backward pheromone deposition
 - Deterministic backward path
 - Pheromone evaporation
 - Pheromone deposition rate depends on quality of solution (ants deposit more pheromone on shorter paths)
 - Loop avoidance

Use the Ant System ACO to solve this TSP



Ant System

- Pheromone is stored in a matrix
- Heuristic information (distances between nodes) is stored in another matrix
- Ants remember where they've been on a given tour and do not repeat cities

Initialize Pheromone

While termination condition not met

 Construct Ant Solutions

 For each ant,

 choose a start city,

 construct a tour, biasing steps by pheromone, until it returns home

 Optionally Apply local search

 Update Pheromone

endwhile

Variations: elitist, rank based, max-min: alter pheromone deposition and update

Ant System

- Ant cycle: pheromone deposit is determined globally (not very ant like) based on the length of the tour
- Initialization:

Initialize pheromone and

$$\tau_{i,j} = \frac{m}{C^{nn}} \quad m = \# \text{ ants}$$

heuristic information for all i,j:

$$\eta_{i,j} = \frac{1}{d_{i,j}} \quad \begin{array}{l} C^{nn} = \text{length of nearest neighbor CYCLE} \\ d_{i,j} = \text{distance from } i \text{ to } j \end{array}$$

We define the transition probability from town i to town j for the k-th ant as

- Tour construction formula
- What do alpha and beta represent?

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

Ant System

The amount of pheromone on edge (i,j) like) based on the length of the tour

- Initialization:

Initialize pheromone and

heuristic information for all i,j:



$$\tau_{i,j} = \frac{m}{C^{nn}} \quad m = \# \text{ ants}$$

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The attractiveness of an edge other than pheromone level. ant as
(Distance to city)

- What do alpha and beta represent?

$$p_{ij}^k(t) = \begin{cases} \frac{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

Ant System


- Ant cycle: pheromone deposit is determined globally (not very ant like) based on the length

α and β tune the relative importance of pheromone and local information.

How does this relate to GAs and the mutation rate?

· CYCLE

We define the transition probability from town i to town j for the k -th ant as


$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

- Tour construction formula
- What do alpha and beta represent?

Ant System

- Ant cycle: pheromone deposit is determined globally (not very ant like) based on the length of the tour
- Initialization:

Probability of ant following edge (i,j)

heuristic information for all i,j:

$$\eta_{i,j} = \frac{1}{d_{i,j}}$$

C^{nn} = length of nearest neighbor CYCLE

$d_{i,j}$ = distance from i to j

We define the transition probability from town i to town j for the k-th ant as

- Tour construction formula

- What do alpha and beta represent?

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

- Pheromone update

$$\tau_{ij} \leftarrow \tau_{ij} + \Delta\tau^k.$$

$$\Delta\tau_{i,j}^k = \begin{cases} \frac{1}{C^k} & \text{C}^k \text{ is tour length of } k^{\text{th}} \text{ ant} \\ & \text{If } (i,j) \text{ are on the tour of the } k^{\text{th}} \text{ ant} \\ 0 & \text{otherwise} \end{cases}$$

- Pheromone evaporation

$$\tau_{ij} \leftarrow (1 - \rho)\tau_{ij}, \quad \forall (i, j) \in A,$$

where $\rho \in (0, 1]$ is a parameter.

- AS parameter settings:

- alpha = 1
- beta = 2 to 5
- rho = 0.5
- m = n (number of ants = number of cities)
- τ_{ij} initialization = m/C^{nn}

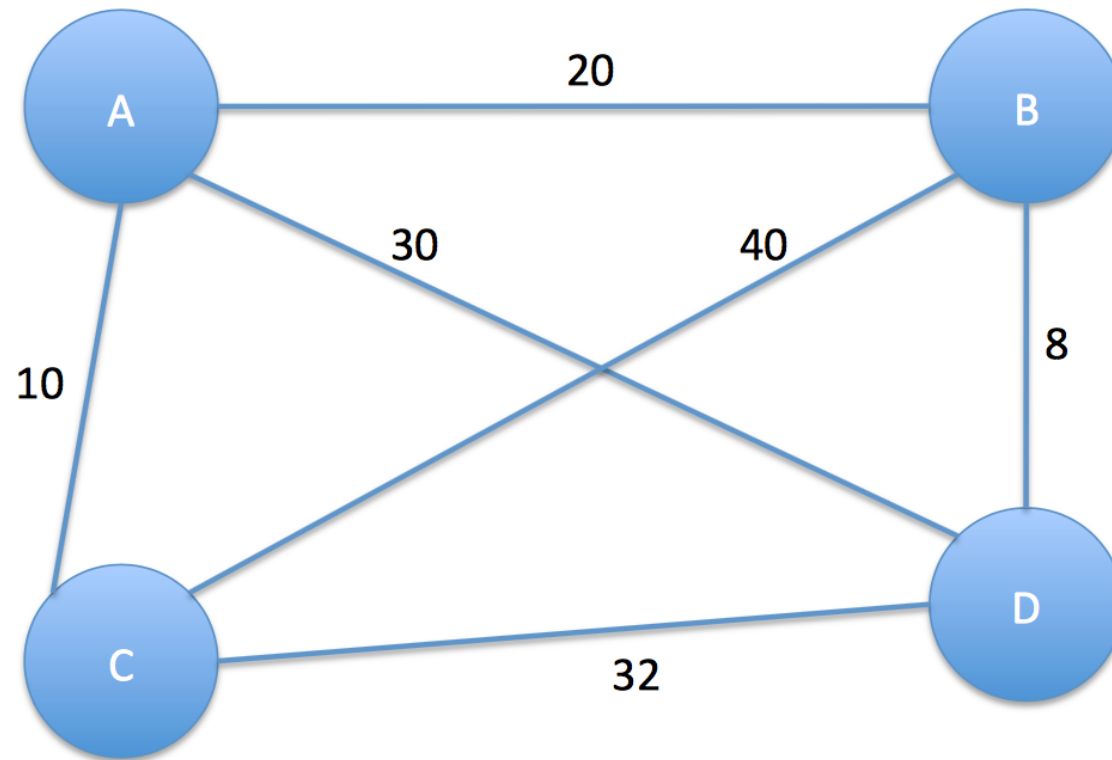
- Ant Cycle: pheromone update depends on tour length,

So it is updated only after a completed tour

- Elitist AS: Reinforce T^{bs} (best so far tour)

$$\tau_{i,j} = \tau_{i,j} + \sum_{k=1}^m \Delta\tau_{i,j}^k + e\Delta\tau_{i,j}^{bs}$$

$$\Delta\tau_{i,j}^{bs} = \frac{1}{C^{bs}}$$



Initialize

$$\tau_{i,j} = \frac{m}{C^{nn}}$$
$$\eta_{i,j} = \frac{1}{d_{i,j}}$$

C^{nn} = length of nearest neighbor CYCLE

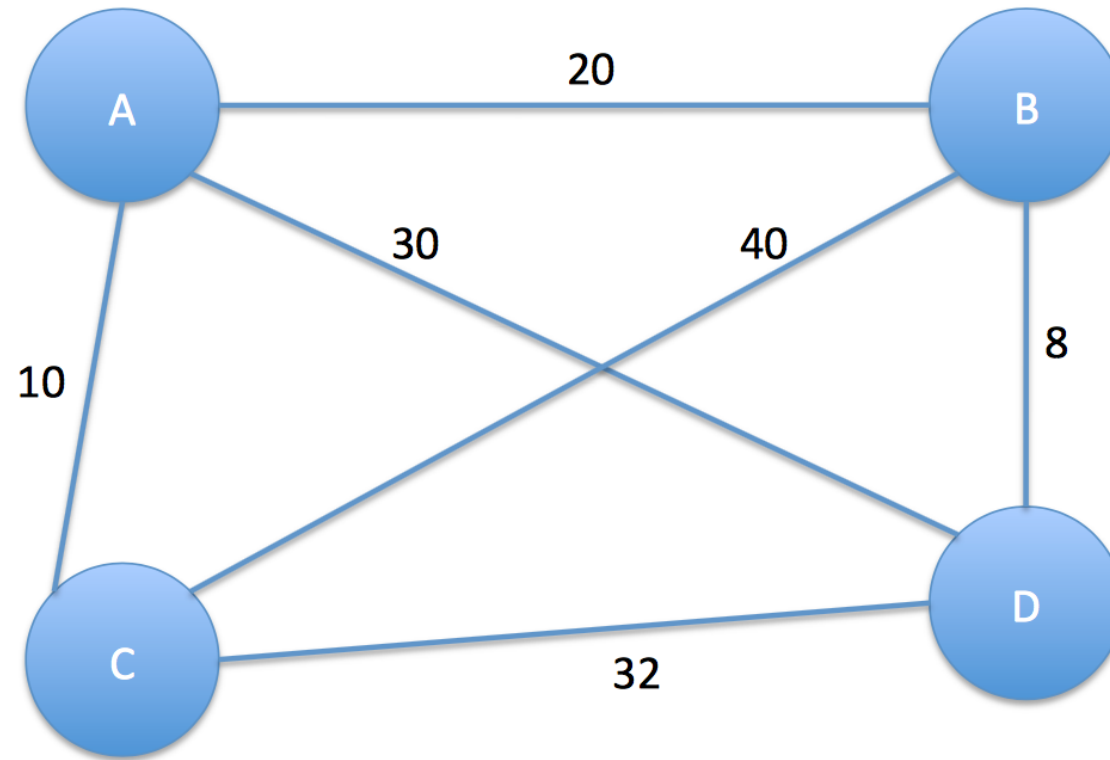
$d_{i,j}$ = distance from i to j

Start at A

$$C^{nn} = 10 + 32 + 8 + 20 = 70$$

A, C, D, B

m = # cities = # ants = 4



Initialize

$$\tau_{i,j} = \frac{m}{C^{nn}}$$
$$\eta_{i,j} = \frac{1}{d_{i,j}}$$

C^{nn} = length of nearest neighbor CYCLE

$d_{i,j}$ = distance from i to j

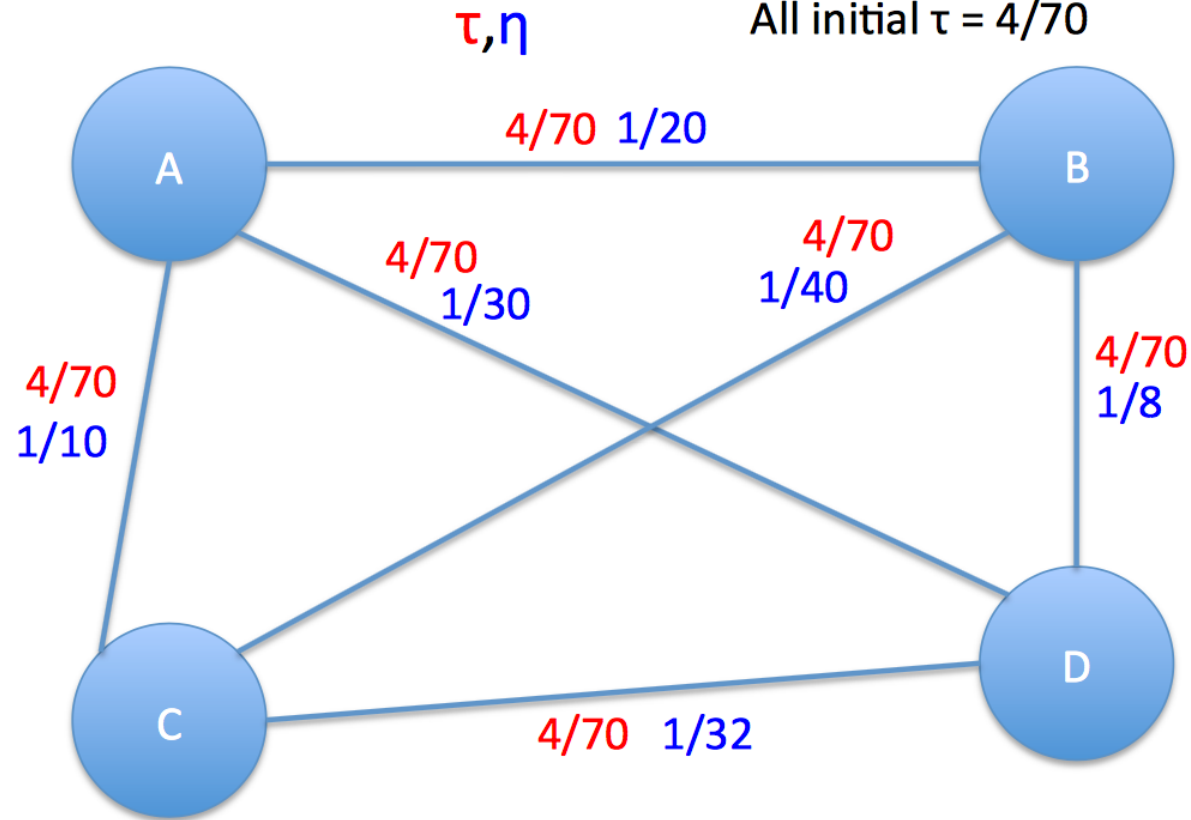
Start at A

$$C^{nn} = 10 + 32 + 8 + 20 = 70$$

A, C, D, B

m = # cities = # ants = 4

All initial $\tau = 4/70$



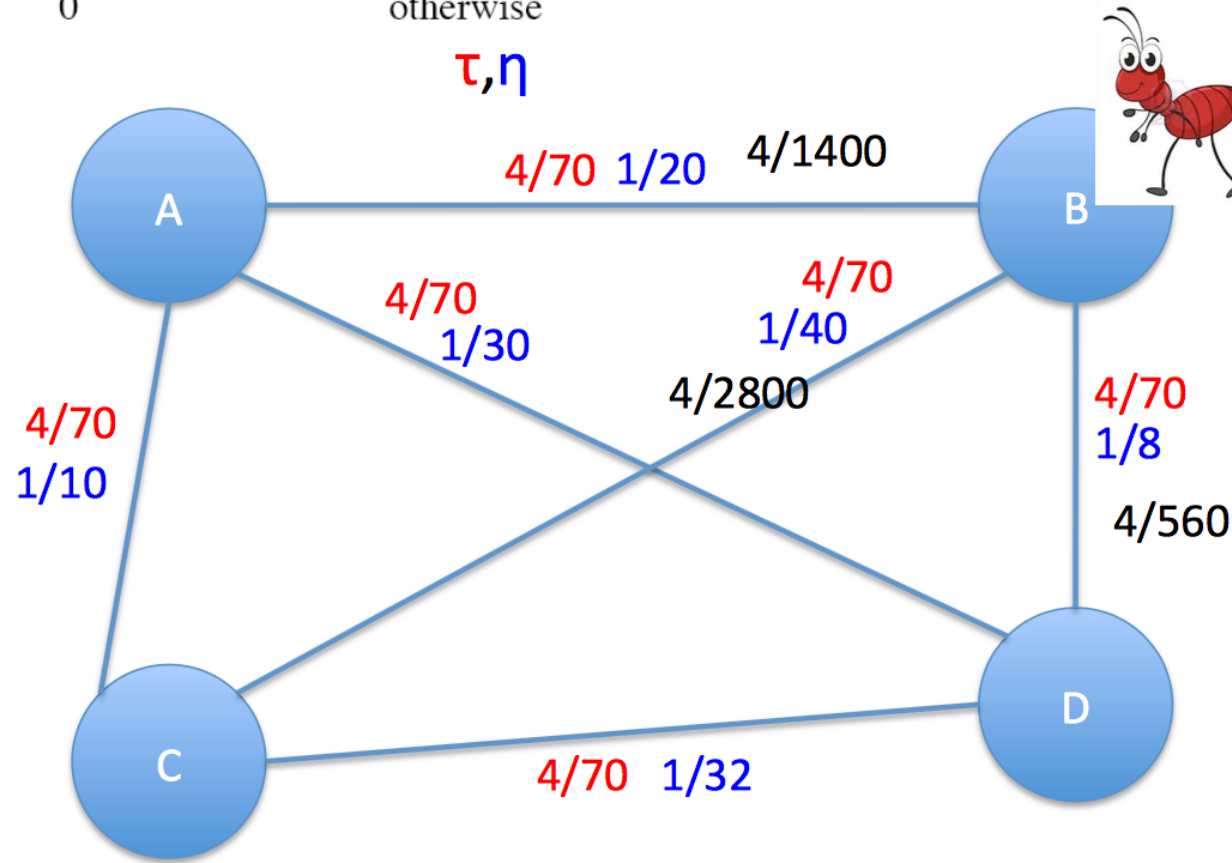
We define the transition probability from town i to town j for the k-th ant as

TRAVERSE

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

denominator=(8+4+20)/2800 $\alpha = 1$
 $\beta = 1$ (usually 2 – 5)

τ, η



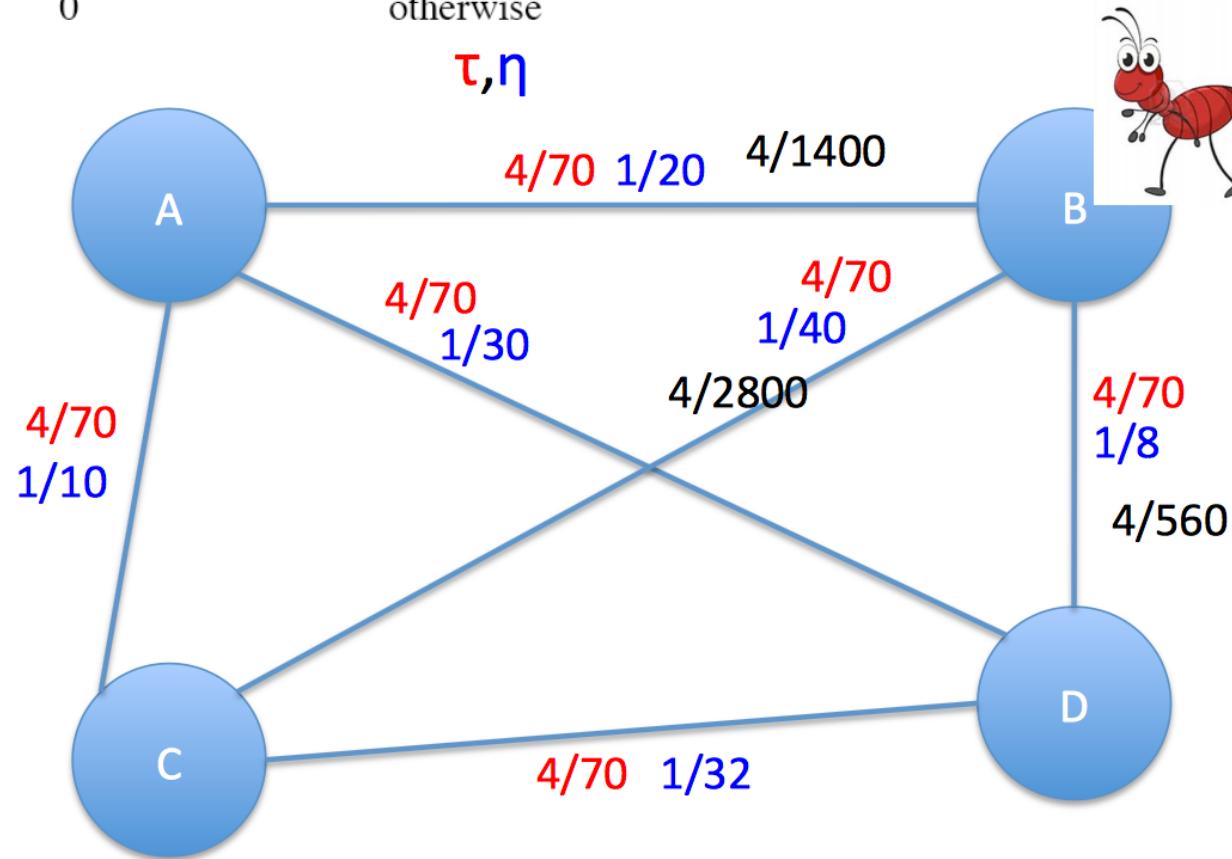
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denominator=(8+4+20)/2800

$\alpha = 1$
 $\beta = 1$ (usually 2 – 5)



Usually : B, D, A, C, B: Cycle = 8+30+10 +40 = 88

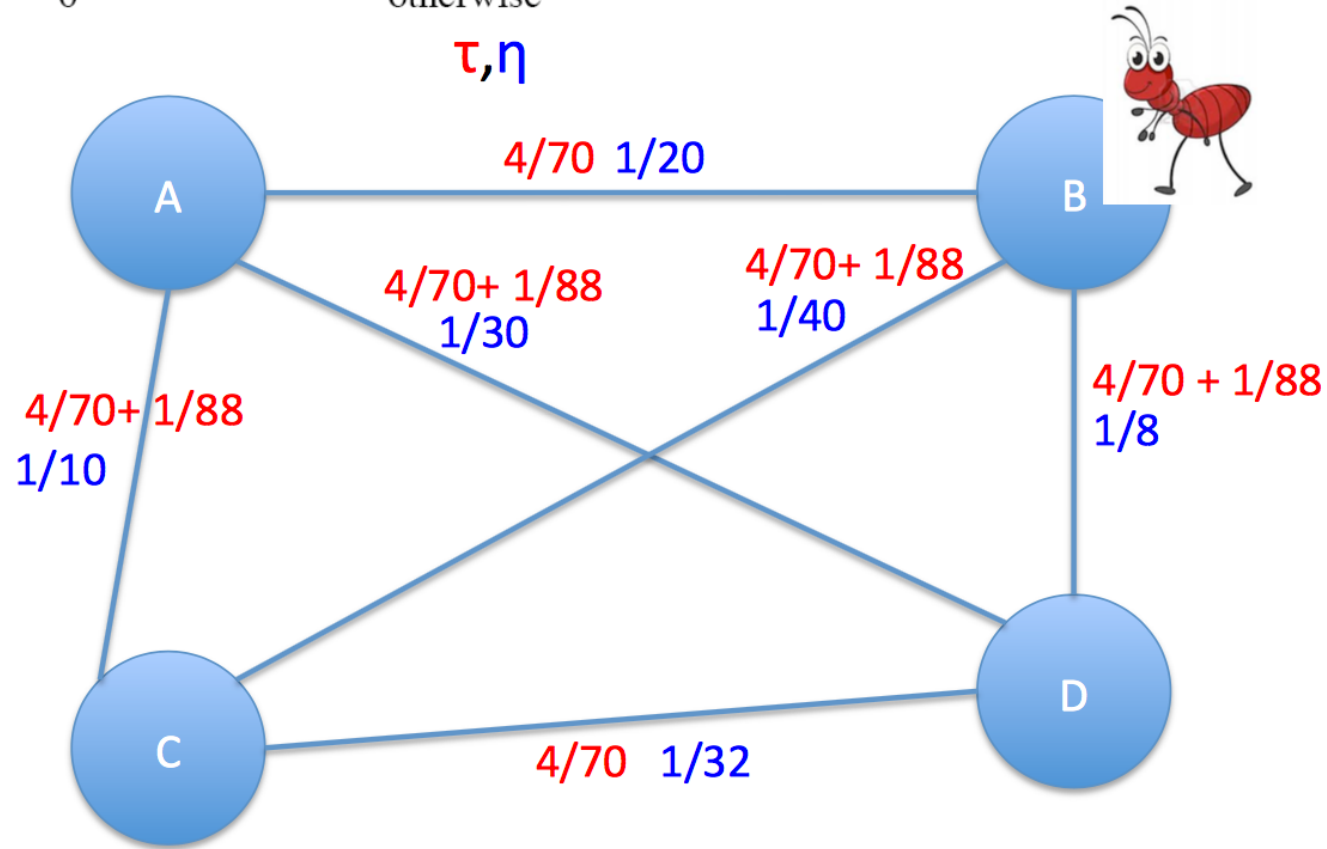
Rarely: B,D,C,A, B: Cycle = 8+32+10 + 20 = 70

We define the transition probability from town i to town j for the k-th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

UPDATE Pheromone

$$\Delta\tau_{i,j}^k = \frac{1}{C^k}$$

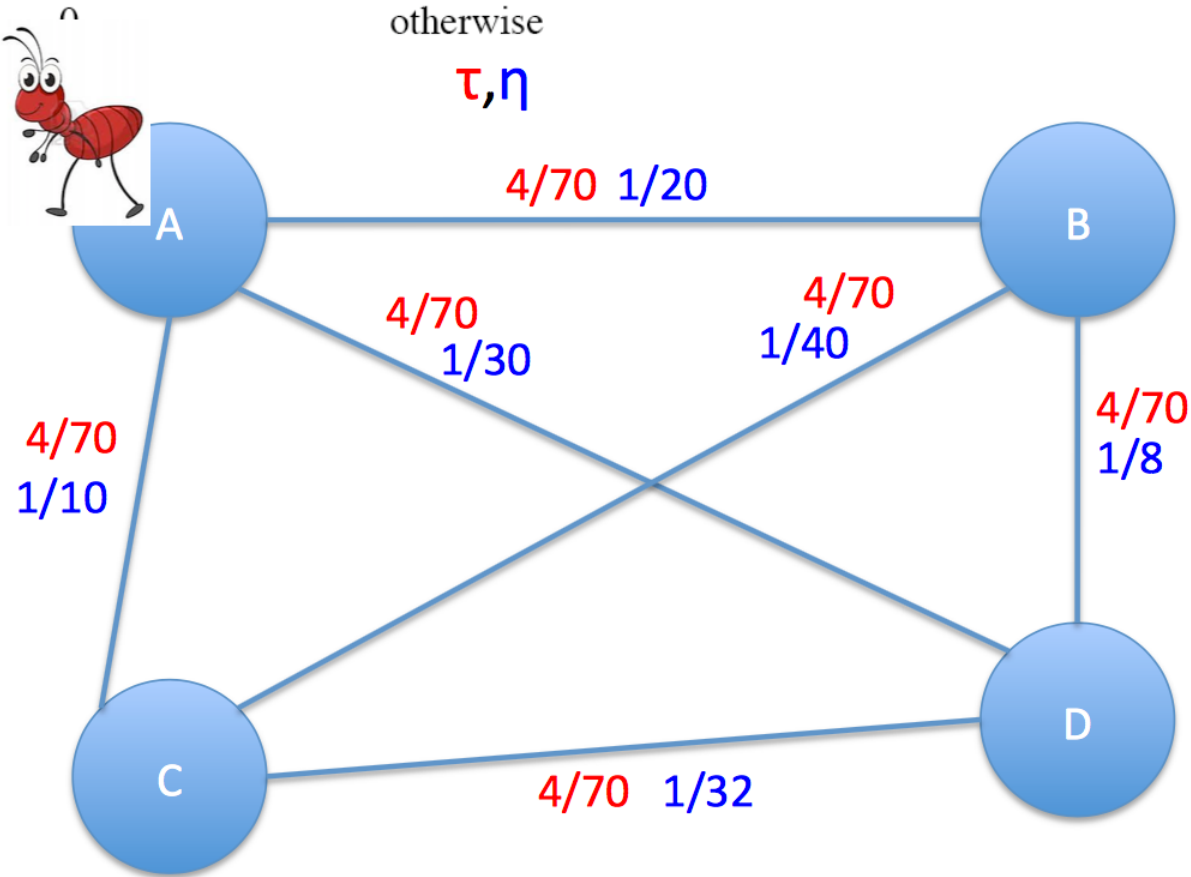


Usually : B, D, A, C, B: Cycle = 8+30+10 +40 = 88

Rarely: B,D,C,A, B: Cycle = 8+32+10 + 20 = 70

We define the transition probability from town i to town j for the k -th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases} \quad \begin{matrix} \alpha = 1 \\ \beta = 1 \end{matrix}$$

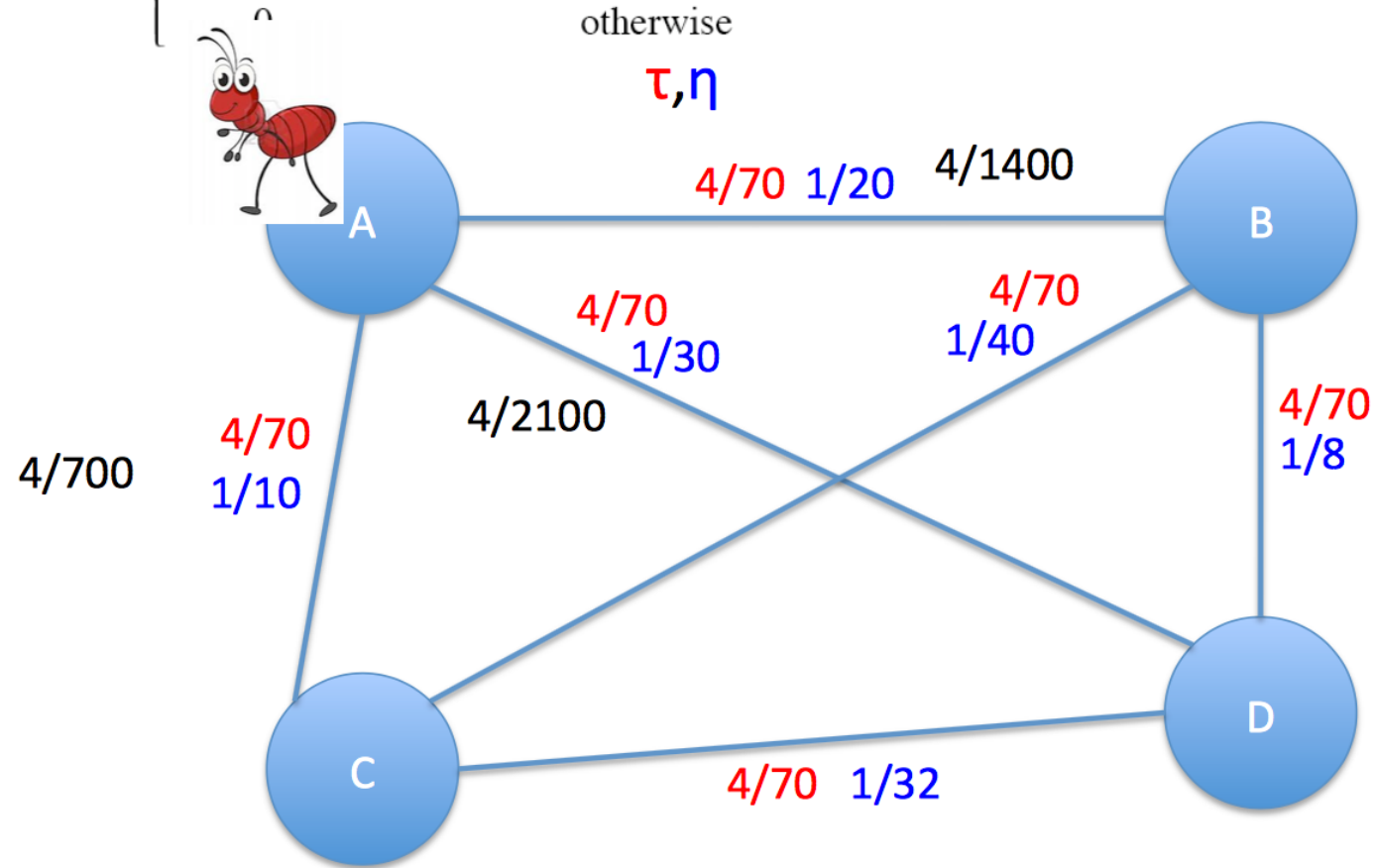


We define the transition probability from town i to town j for the k-th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

$\alpha = 1$

$\beta = 1$ (usually 2 – 5)

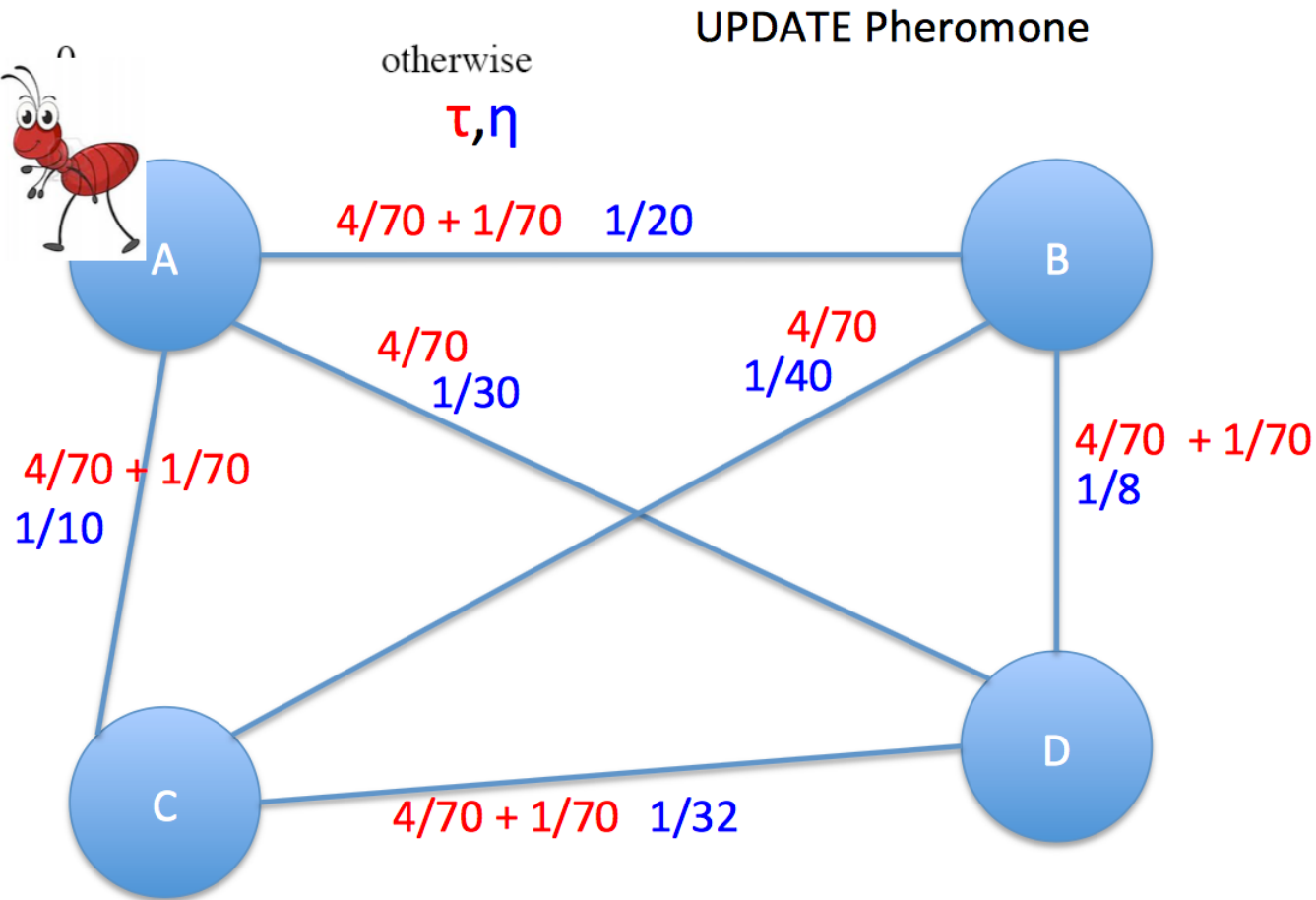
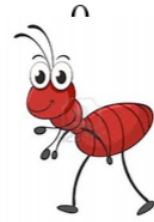


Usually : A, C, D, B,A Cycle = $10+32+8+20=70$

Very Rarely: A,D, C, B, A Cycle = $30+32+40+20=122$

We define the transition probability from town i to town j for the k-th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

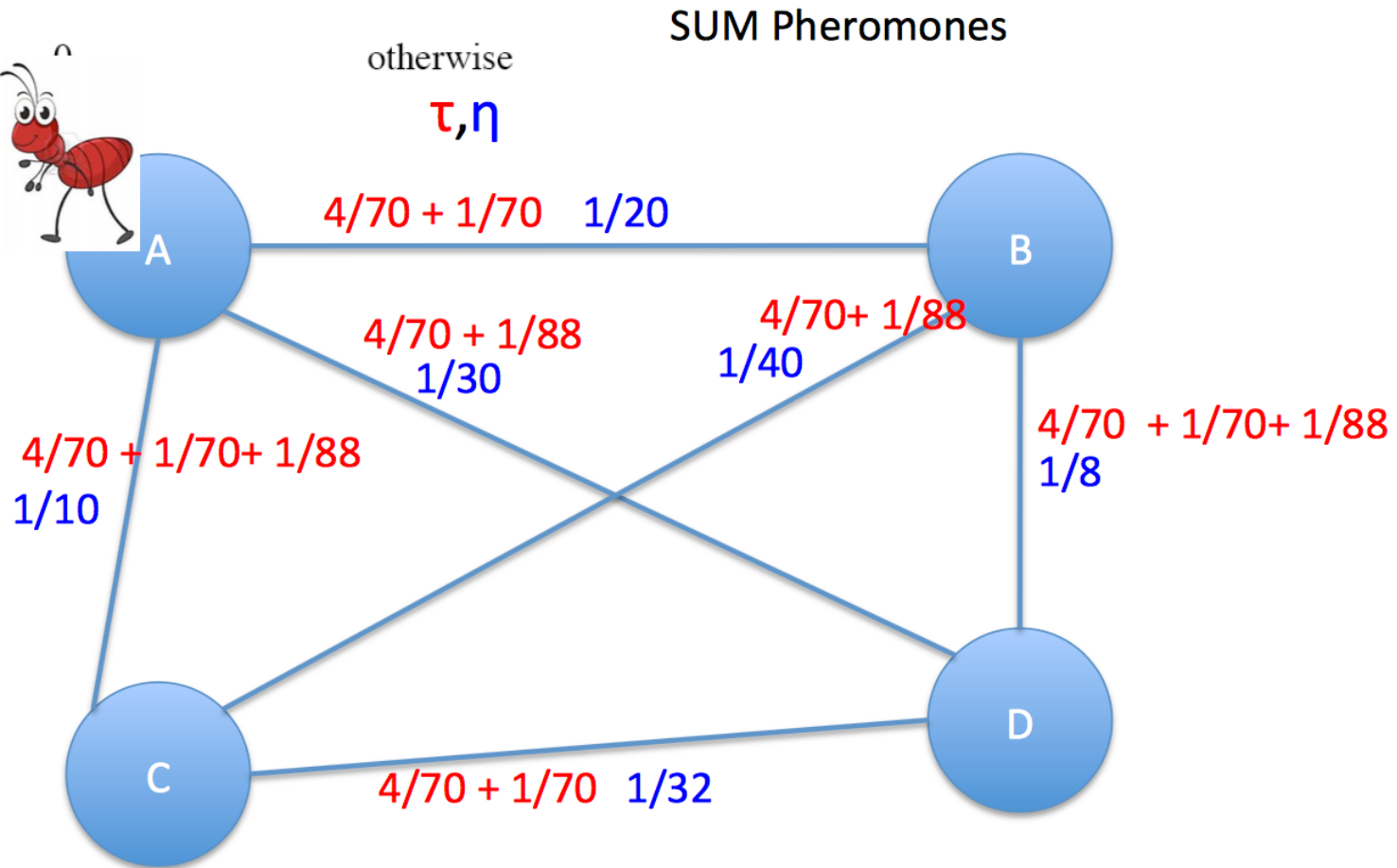


Usually : A, C, D, B, A Cycle = $10+32+8+20=70$

Rarely: A,D, B, C, A Cycle = $30+8+40+10=88$

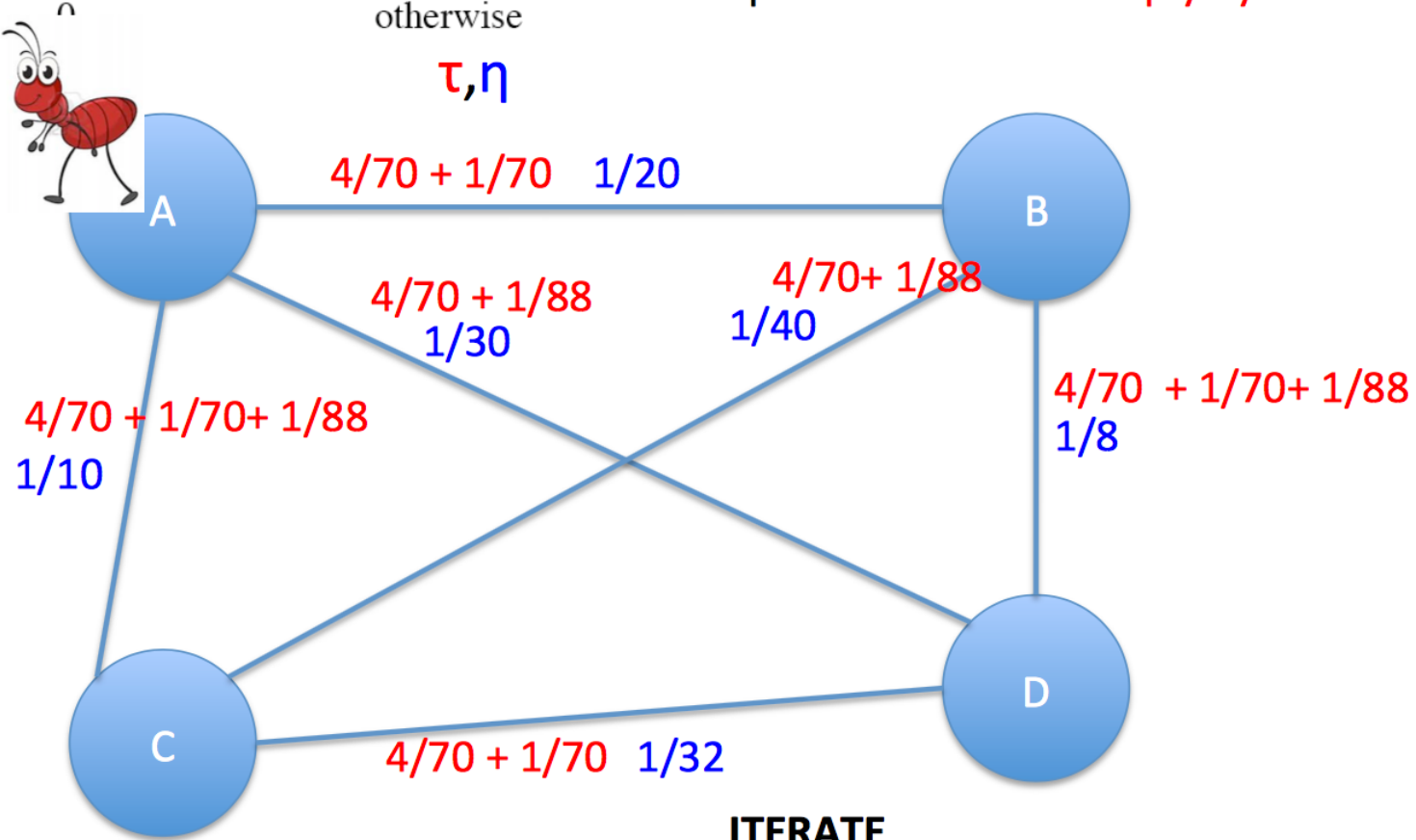
We define the transition probability from town i to town j for the k -th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$



We define the transition probability from town i to town j for the k-th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$



ITERATE

η doesn't change

τ varies as ants choose and assess tours

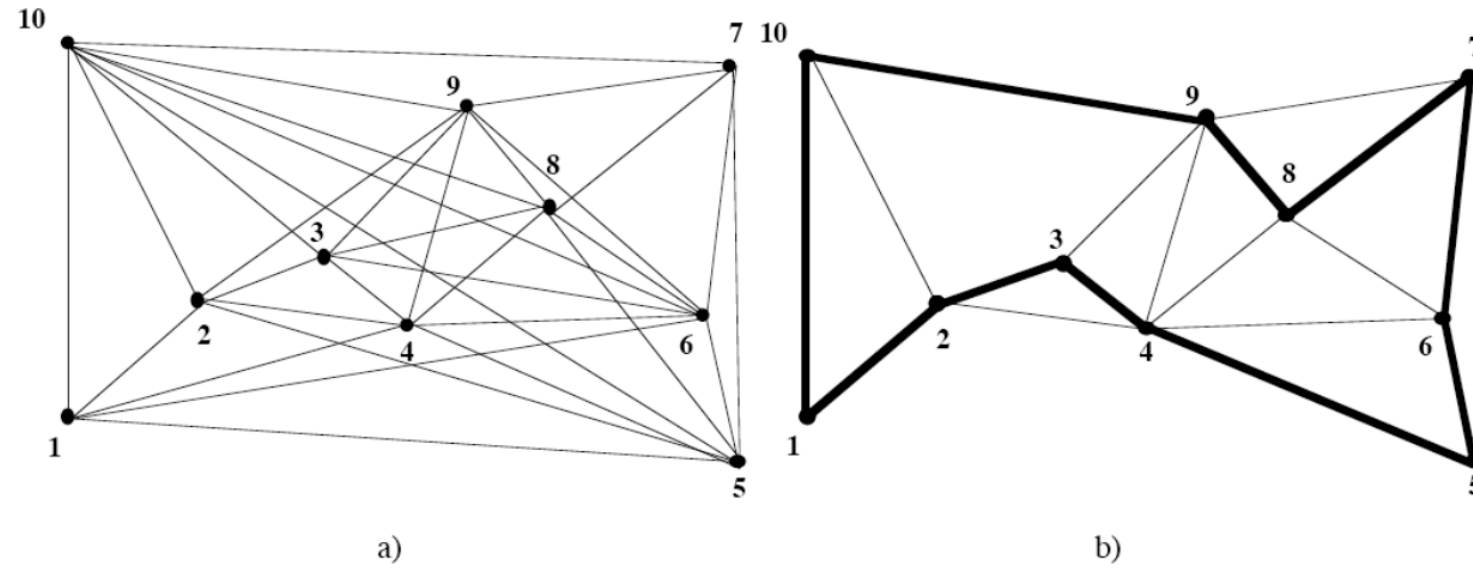
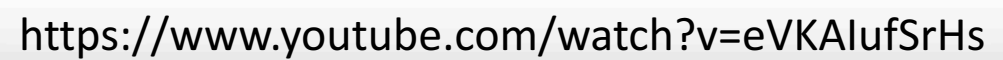
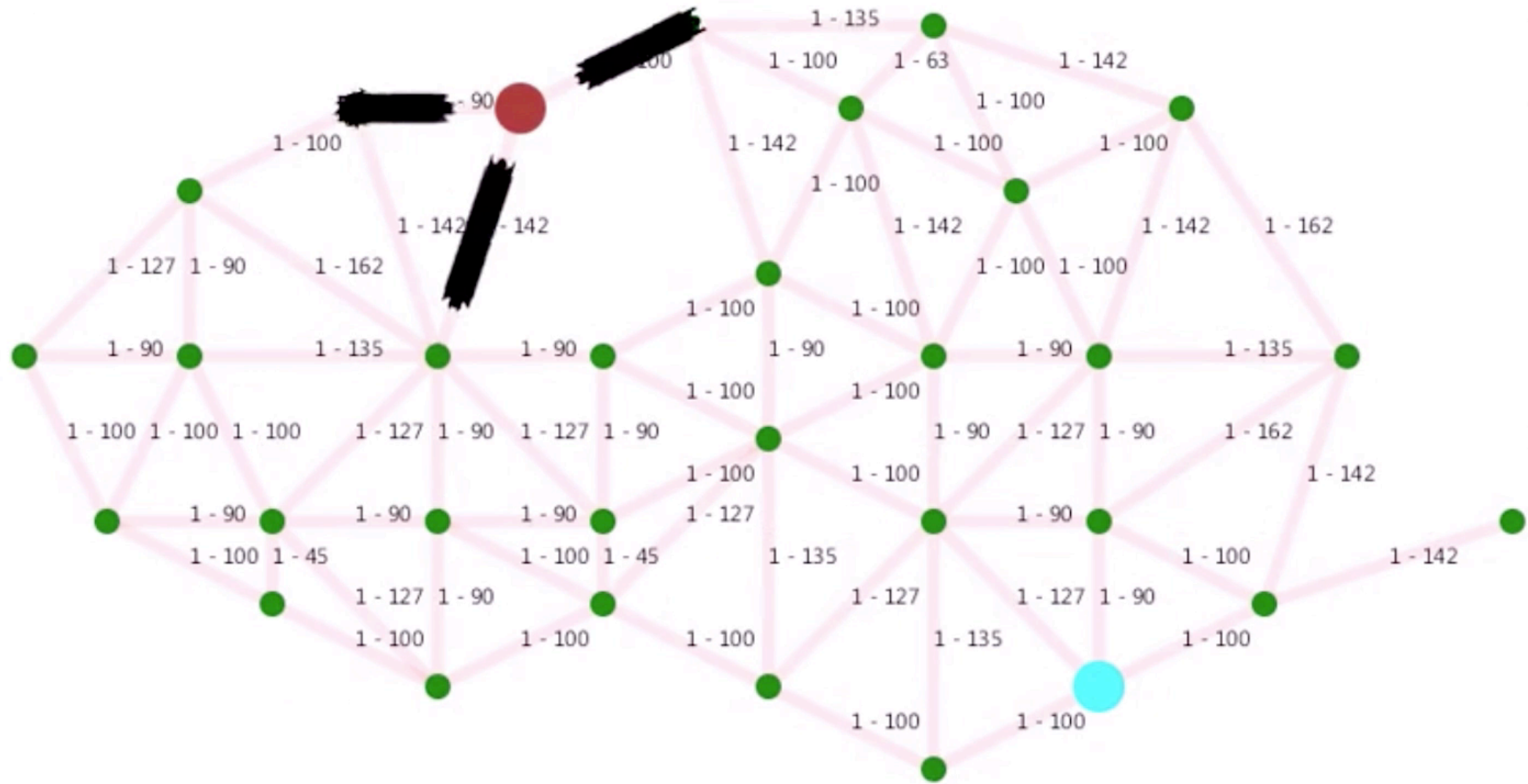


Fig. 6. Evolution of trail distribution for the CCA0 problem.
a) Trail distribution at the beginning of search.
b) Trail distribution after 100 cycles.

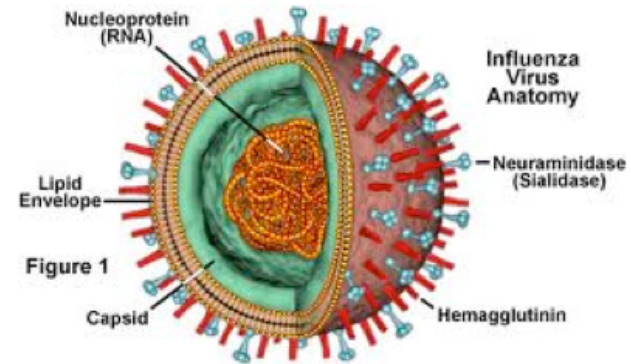




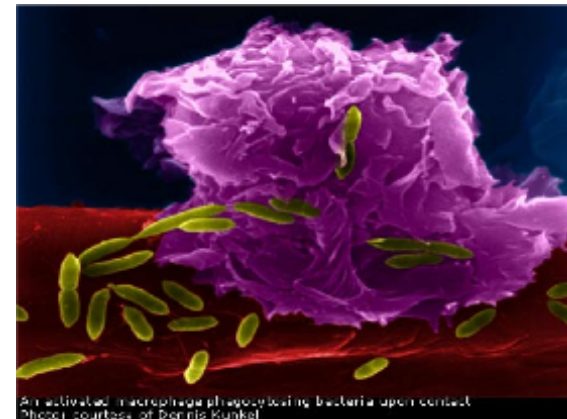
The Immune System

Introduction

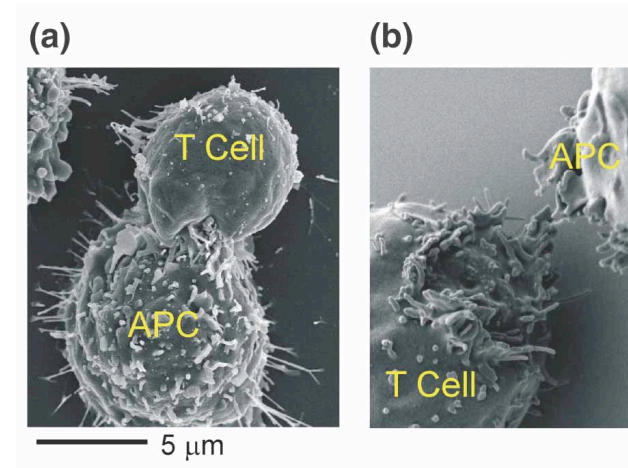
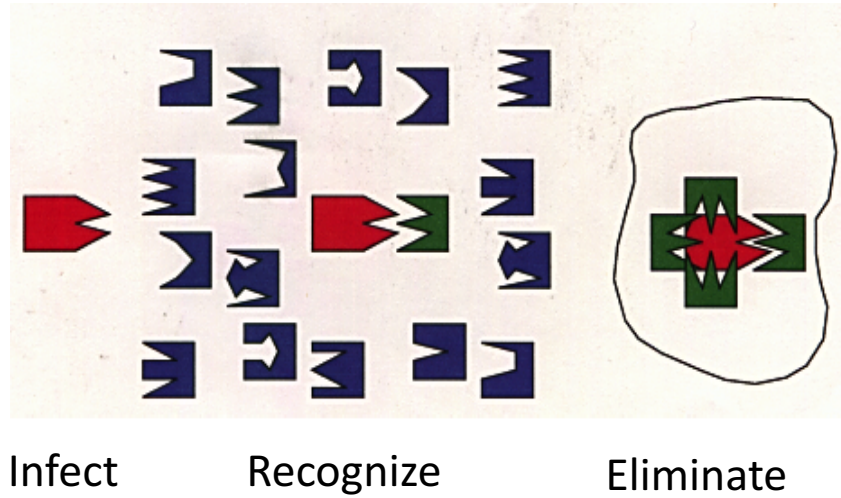
- Immune systems protect the body against foreign pathogens
 - Viruses
 - Bacteria
 - Parasites



Downloaded from micro.magnet.fsu.edu (2010)



A Brief Introduction to the Immune System



<http://wires.wiley.com/WileyCDA/WiresArticle/wisId-WNAN1195.html>

- Cells and molecules
- Recognition implemented as binding
- Specific recognition to avoid autoimmunity

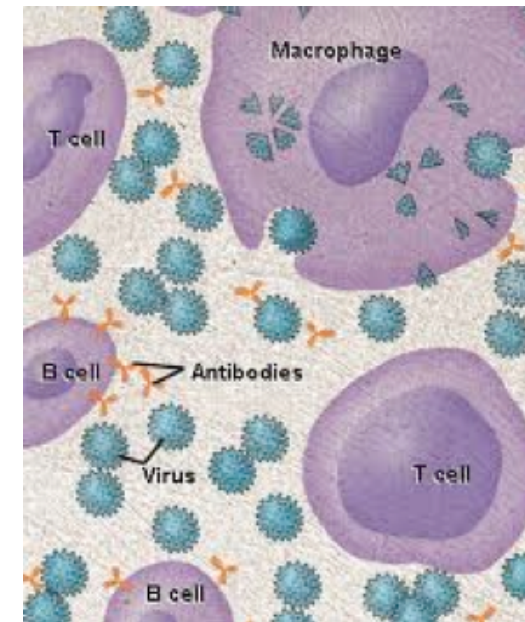
An Information Processing Perspective

- Immune systems **learn** to recognize relevant patterns:
 - Primary response to new foreign antigen
 - Evolved biases towards common pathogens
 - Learned distinction between self and dangerous other
- Immune systems **remember** patterns seen previously
 - Secondary response
 - Cross-reactive memory
- **Combinatorics** to construct pattern detectors
 - $10^{11} - 10^{16}$ different foreign patterns from 30,000 genes
- Massive **parallelism** and **distributed** control

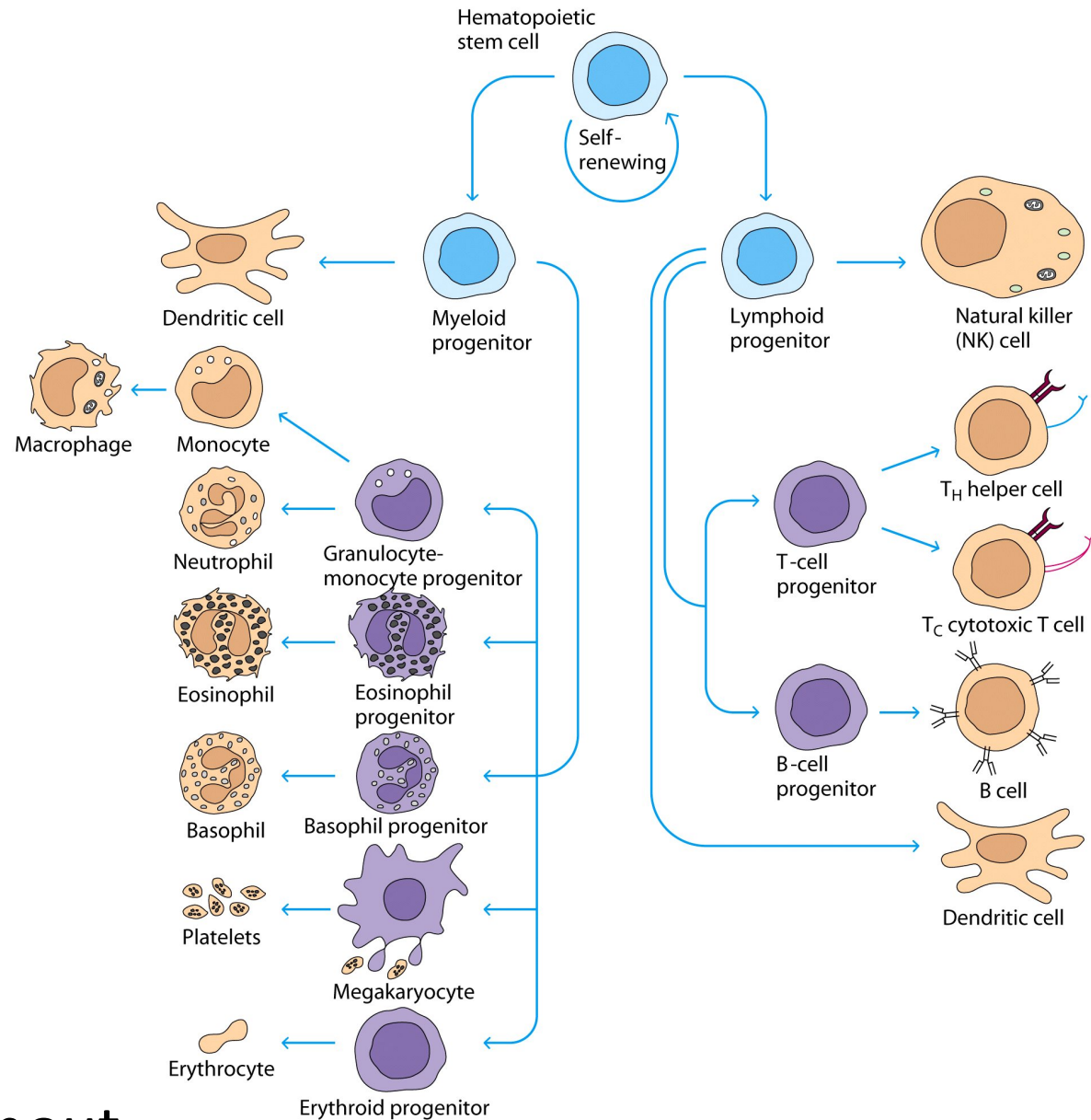
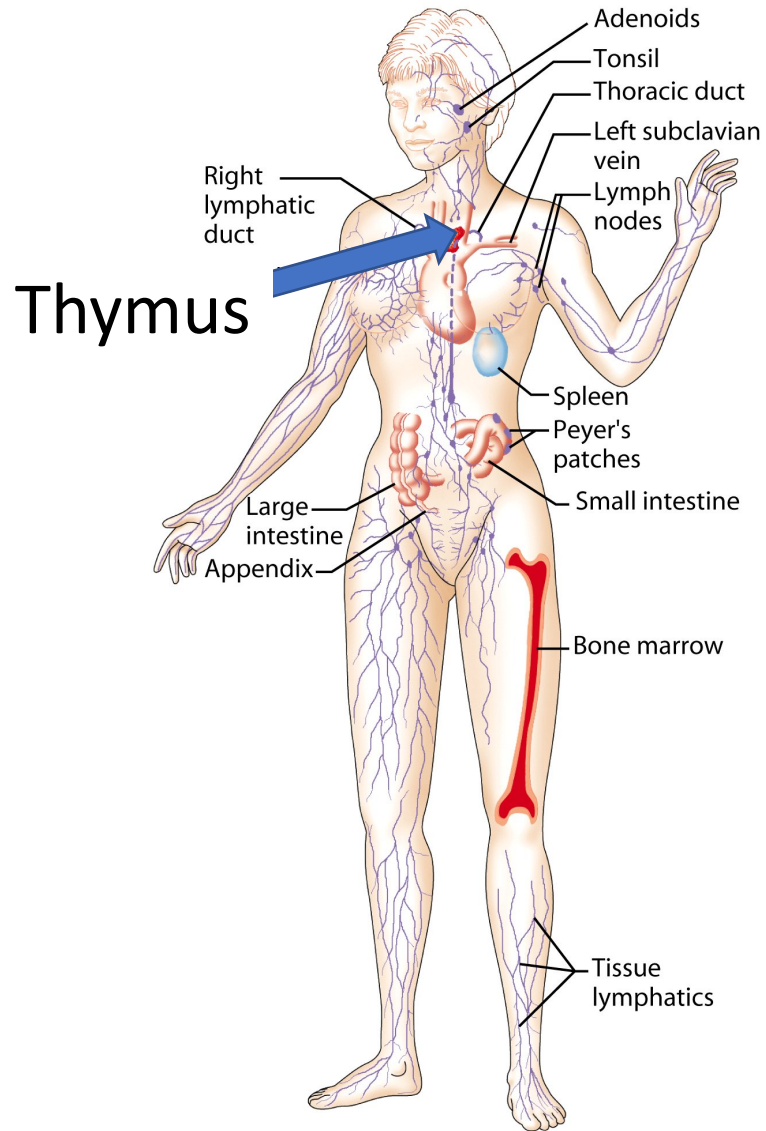
- Innate response
 - Generic
 - Inflammation
- Adaptive response
 - Specific
 - Self-tolerant
 - Learning, memory



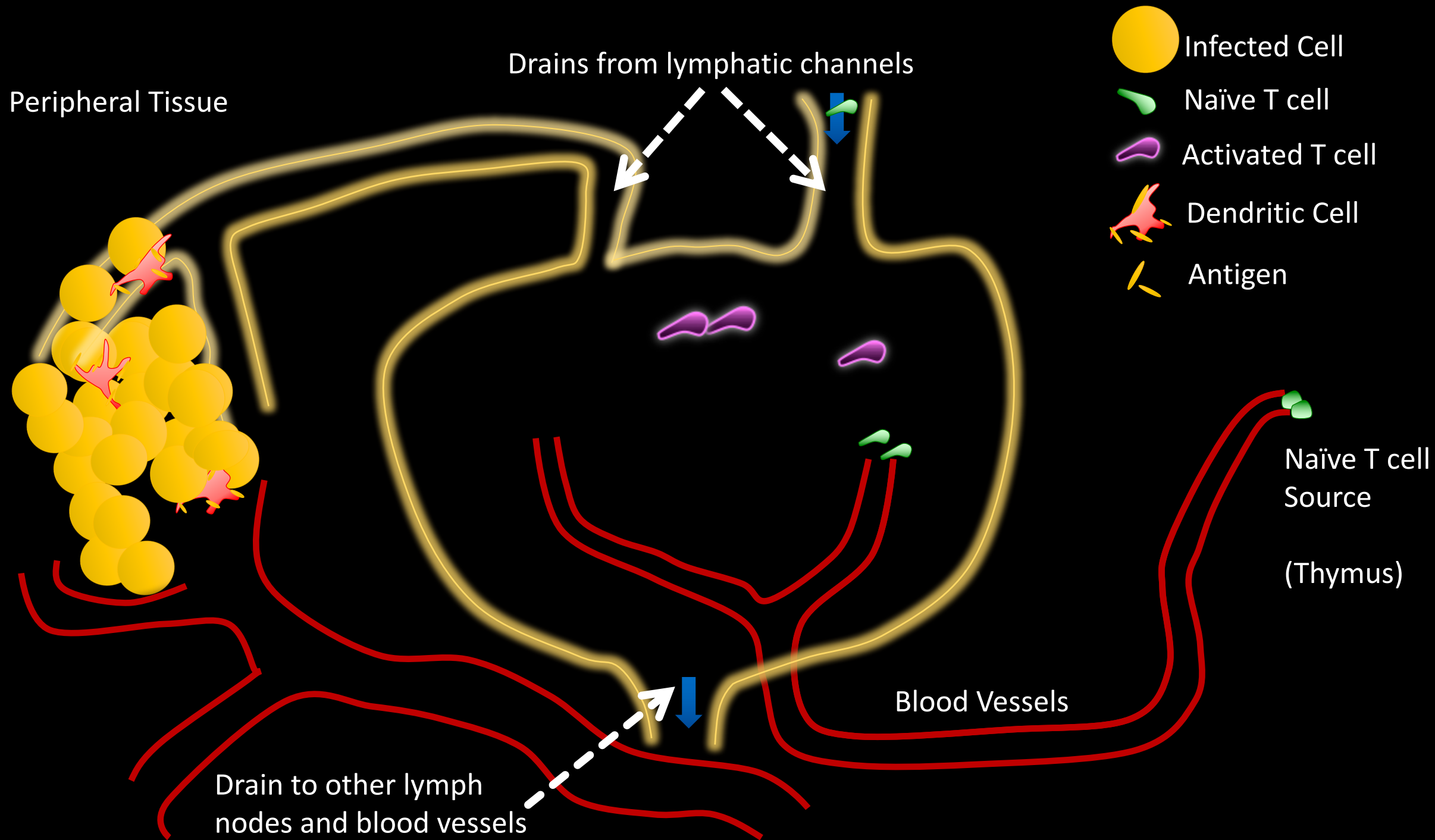
Figure 2-8a
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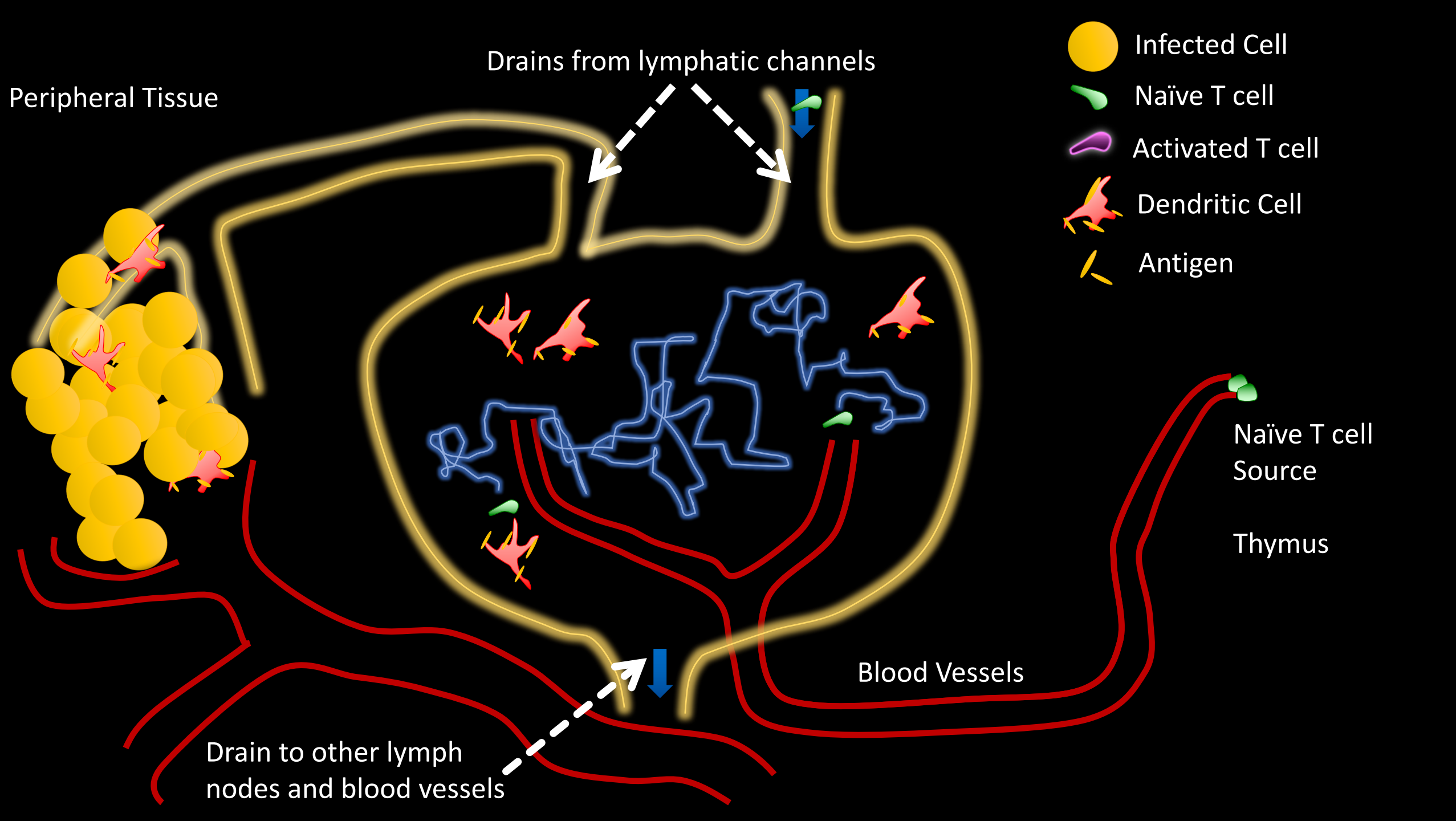


How is it implemented?



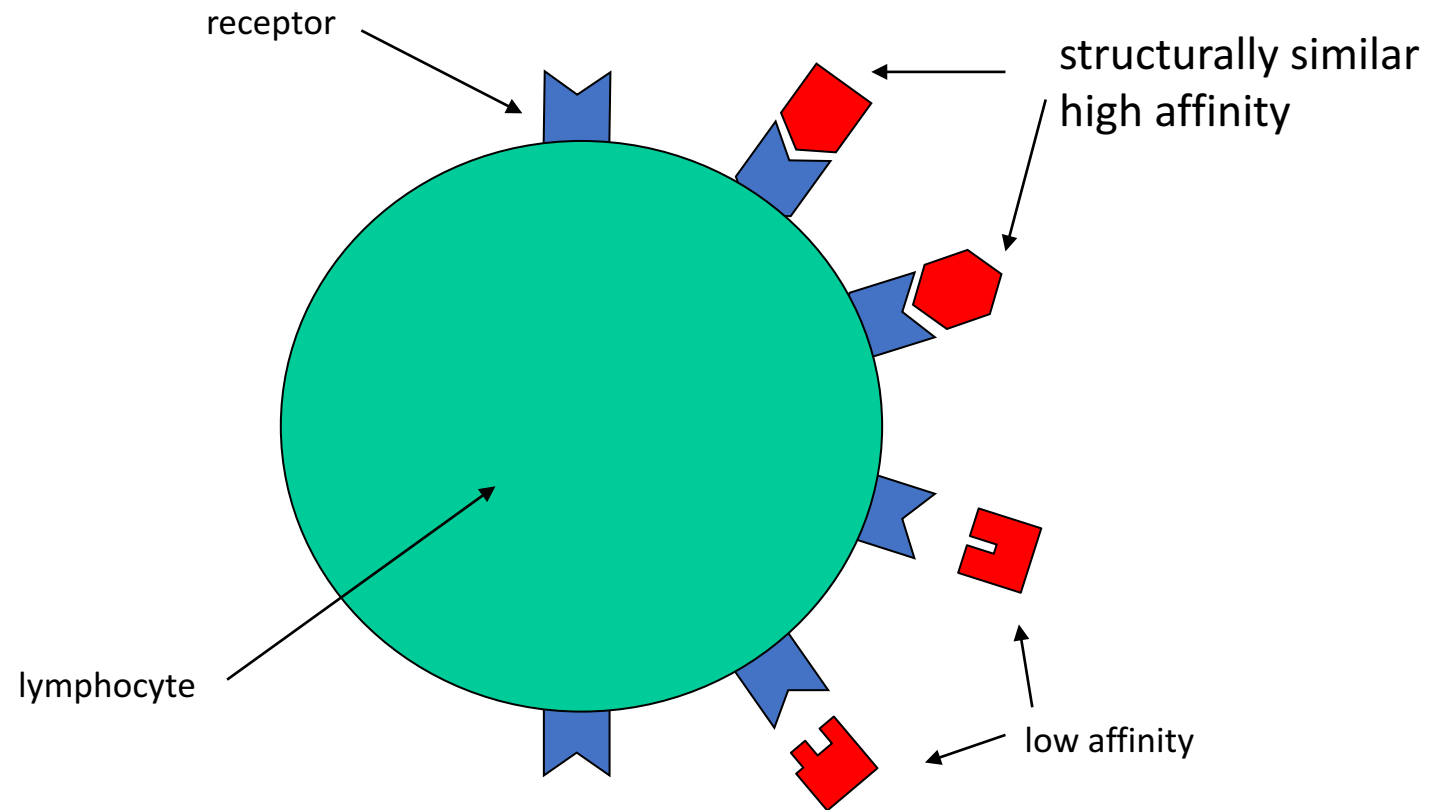
Lymph Nodes distributed throughout



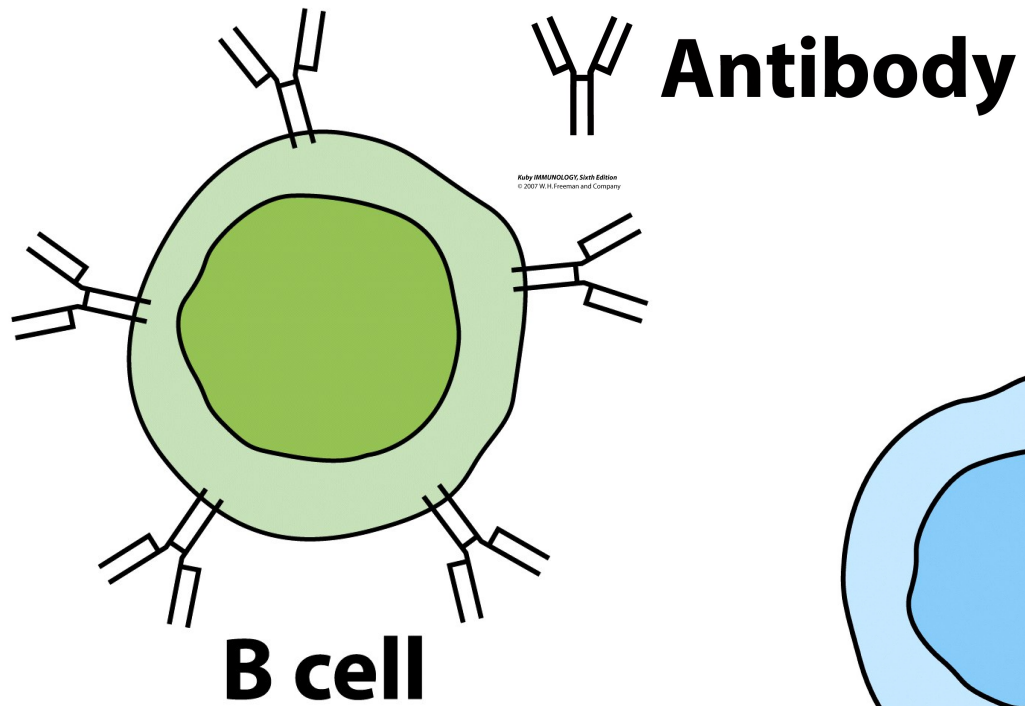


Detection

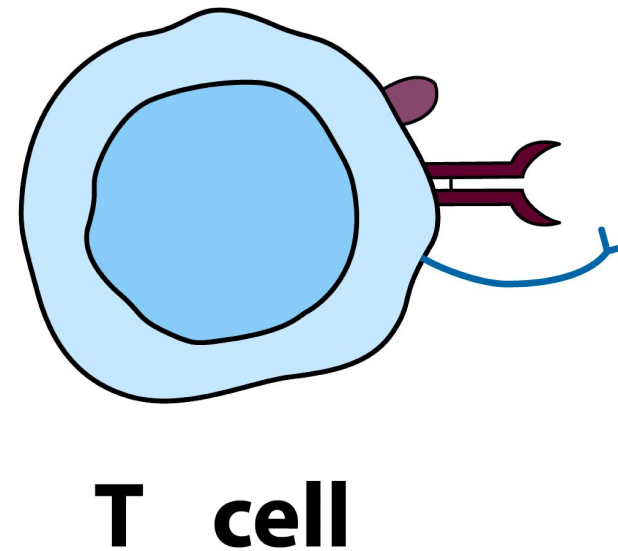
Lymphocyte Binding and Cross-reactivity



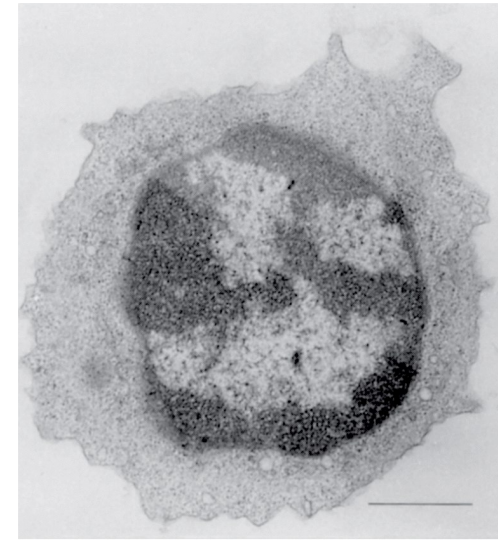
B-cells and T-cells



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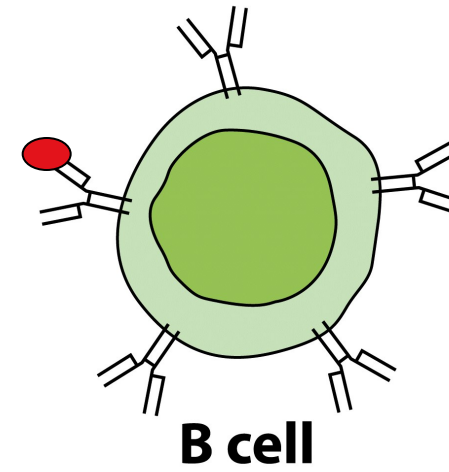


**Small lymphocyte (T or B)
6 μ m diameter**

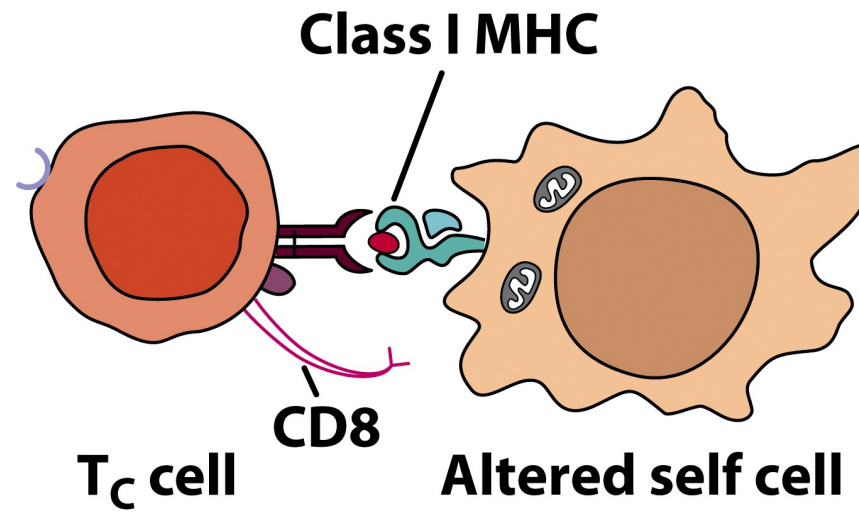
Figure 2-6b part 1
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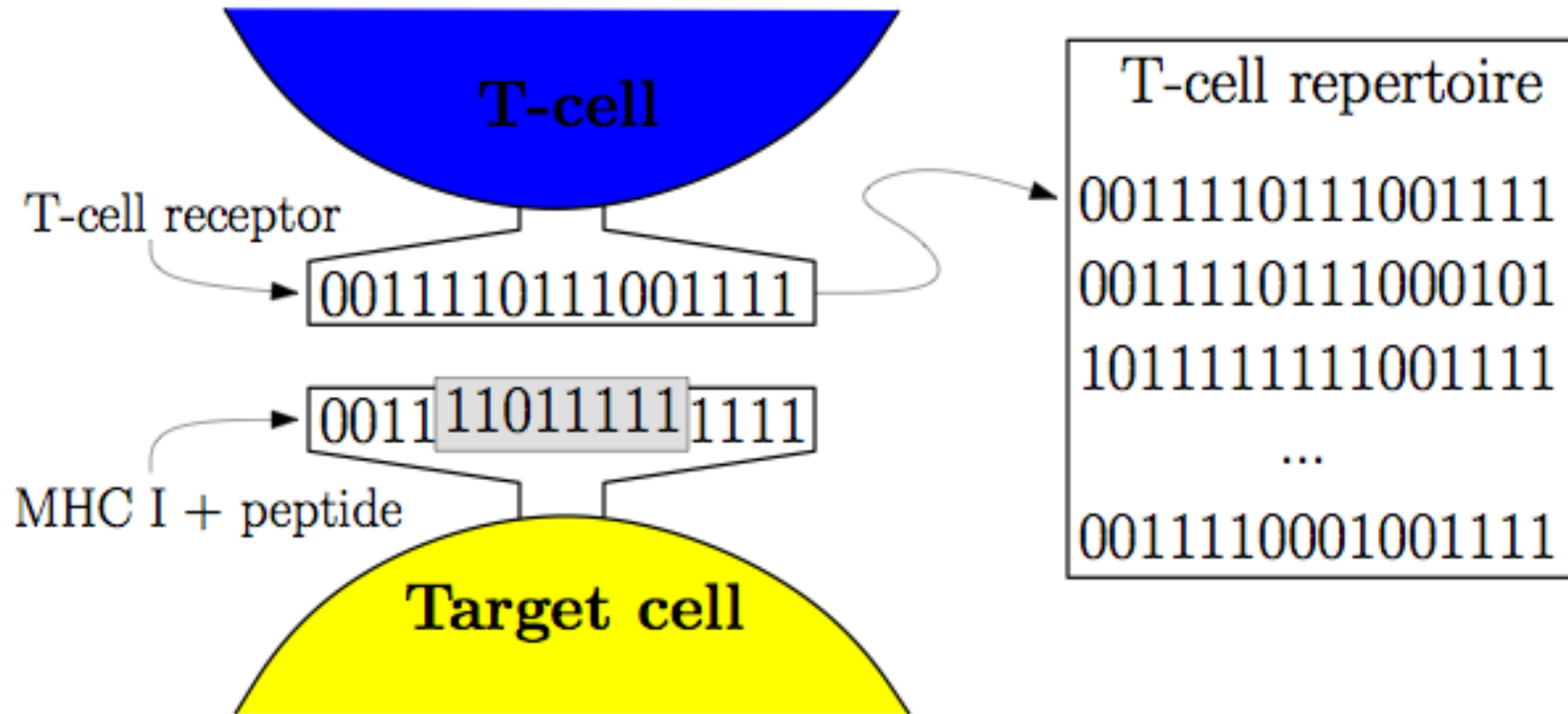


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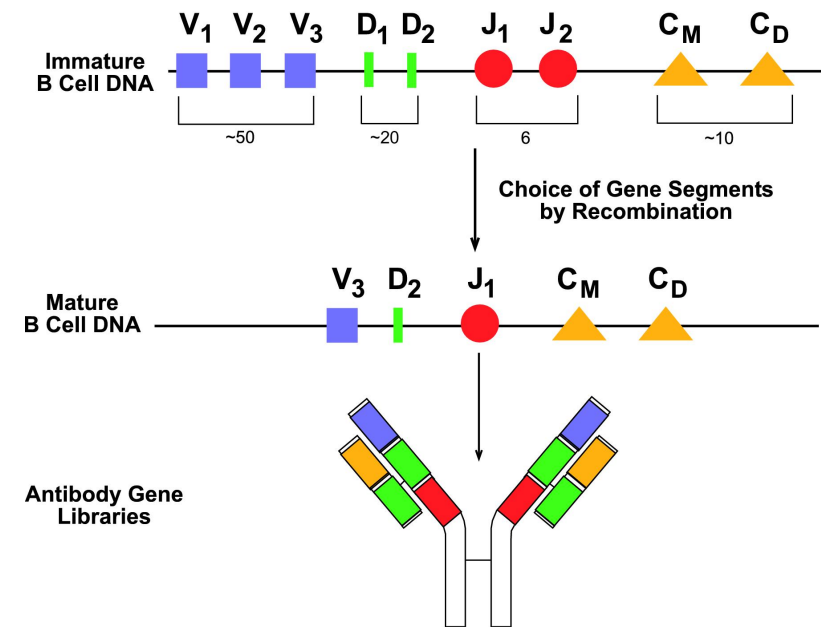
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Fundamental Modeling Abstraction

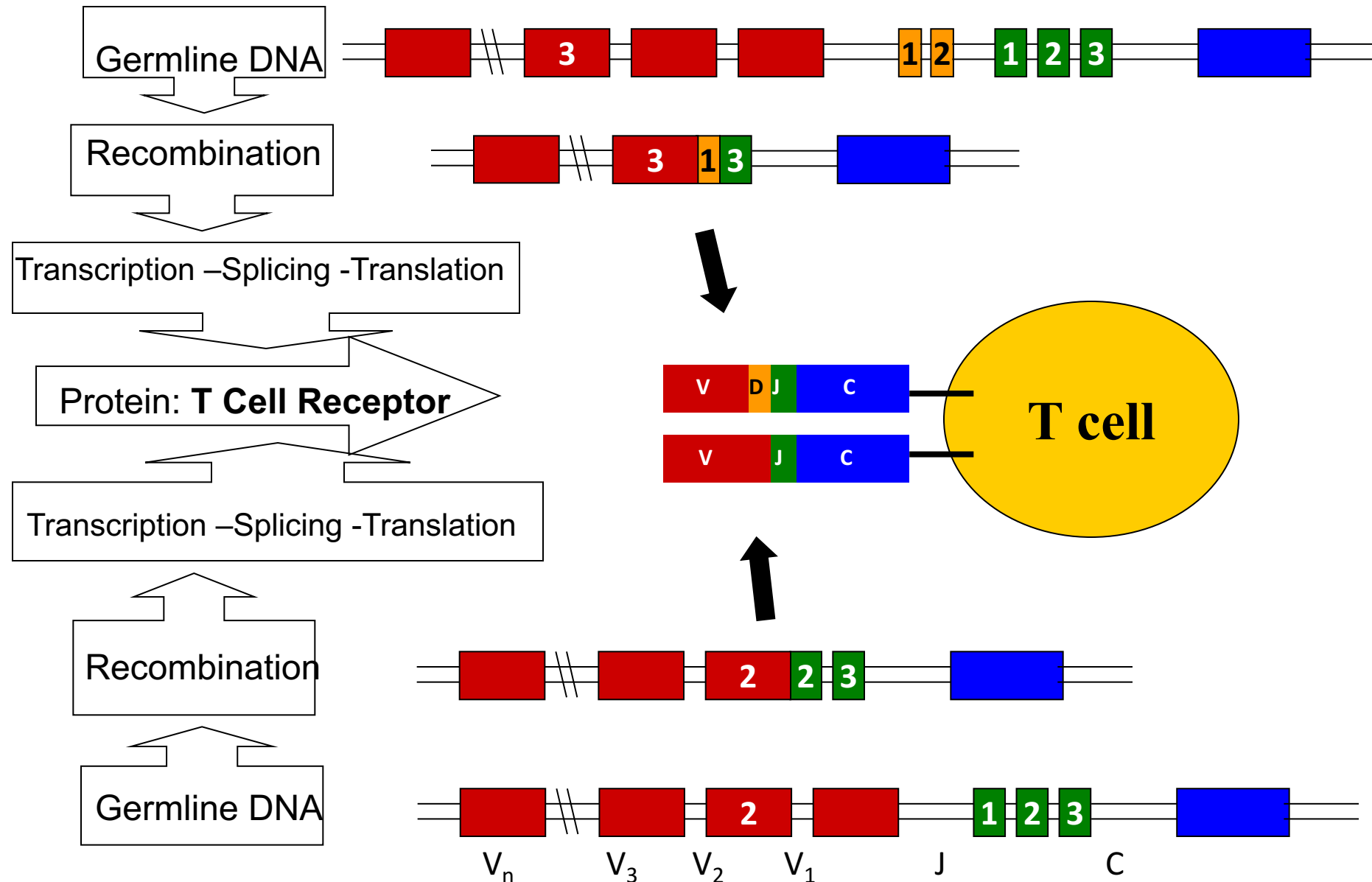


How does the I.S. make so many different receptor patterns?

- Recombination of gene fragments
- Junctional diversity
- Diploid genetics
- Somatic mutation



Generation of Diversity in Antigen Receptors



| Element | Immunoglobulin | | $\alpha:\beta$ receptors | |
|-----------------------------------|----------------------|------------------------------|--------------------------|----------|
| | H | $\kappa+\lambda$ | β | α |
| Variable segments (V) | 65 | 70 | 52 | ~70 |
| Diversity segments (D) | 27 | 0 | 2 | 0 |
| D segments read in 3 frames | rarely | – | often | – |
| Joining segments (J) | 6 | 5(κ) 4(λ) | 13 | 61 |
| Joints with N- and P- nucleotides | 2 | 50% of joints | 2 | 1 |
| Number of V gene pairs | 3.4×10^6 | | 5.8×10^6 | |
| Junctional diversity | $\sim 3 \times 10^7$ | | $\sim 2 \times 10^{11}$ | |
| Total diversity | $\sim 10^{14}$ | | $\sim 10^{18}$ | |

Fig 4.13 © 2001 Garland Science

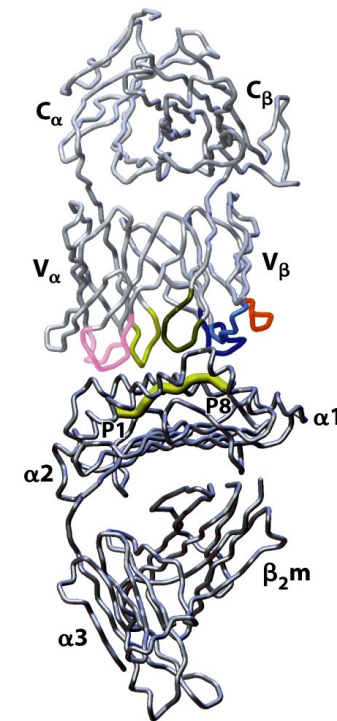


Figure 9-14b
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How much diversity?

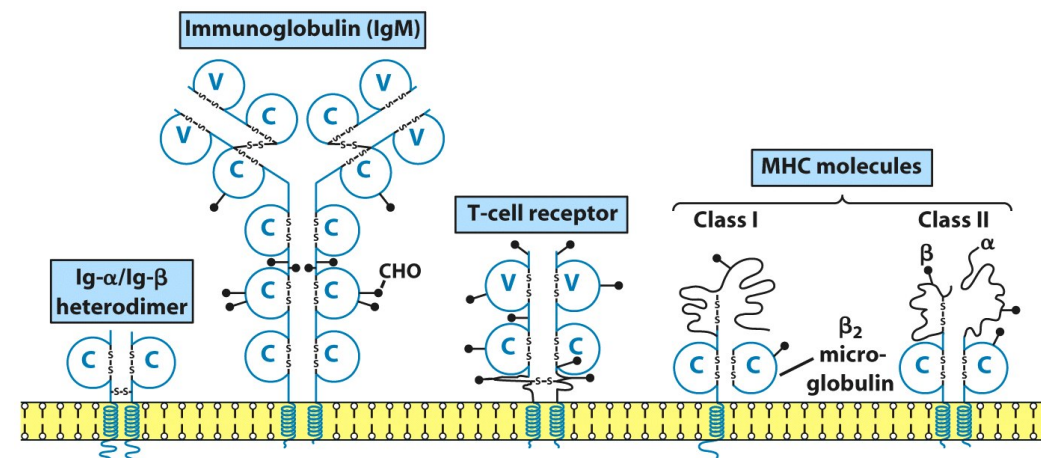


Figure 4-24 part 1
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How does the I.S. make a diverse set of receptors that avoids autoimmunity?

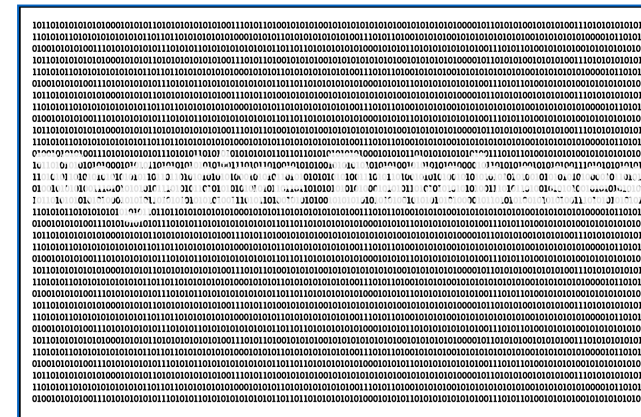
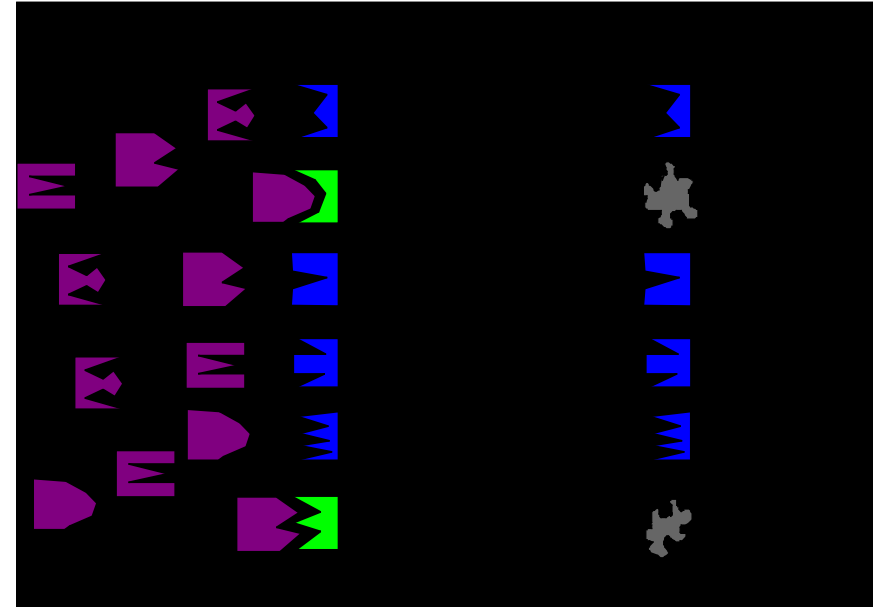
- Clonal Selection Theory
- Believed that any correct theory must explain:
 - How antigen selects correct specificity
 - Why only a single specificity is produced
 - How self tolerance is maintained
 - Why second response to same antigen is so much larger than the first



Frank Macfarlane Burnet
Nobel Prize, 1958

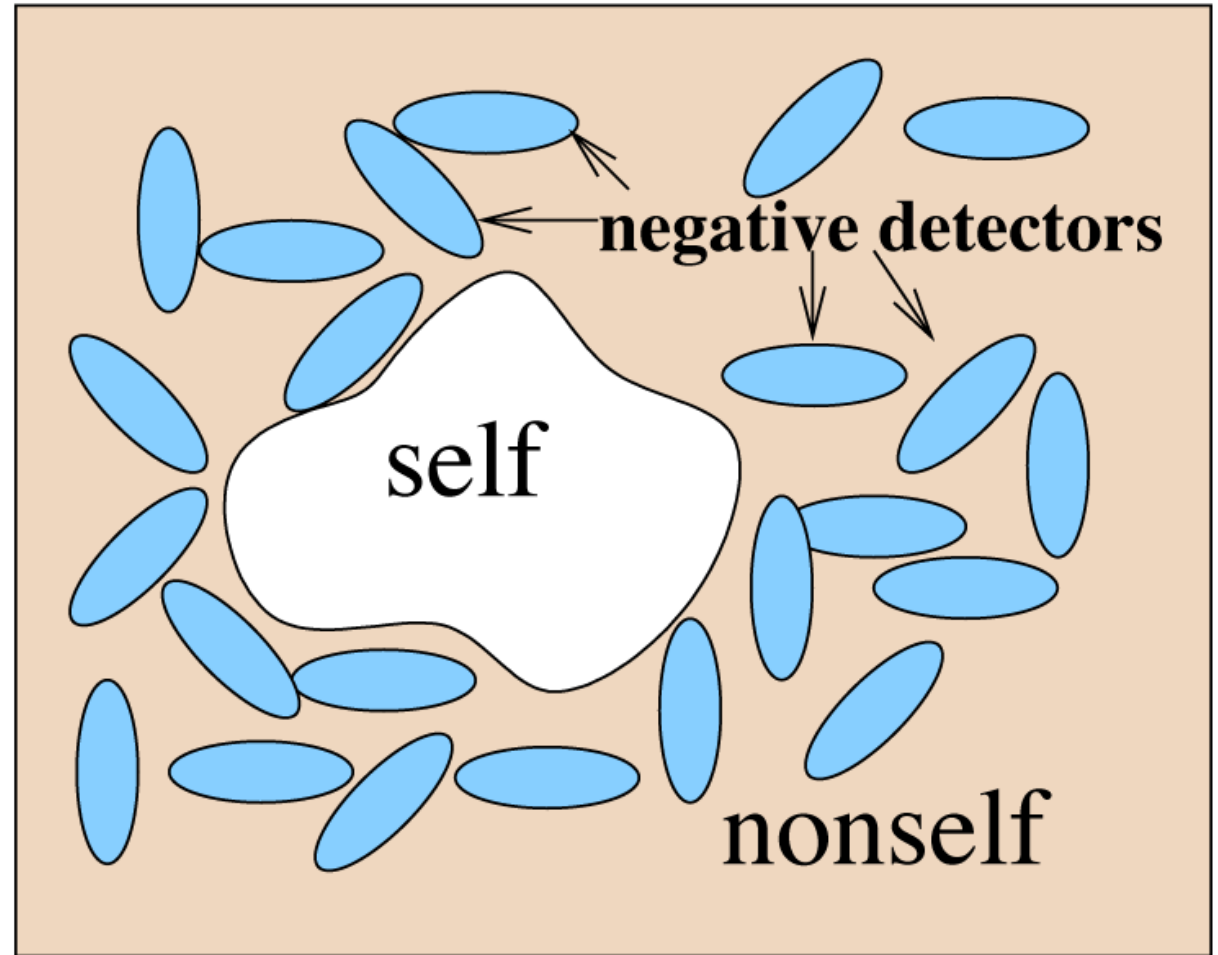
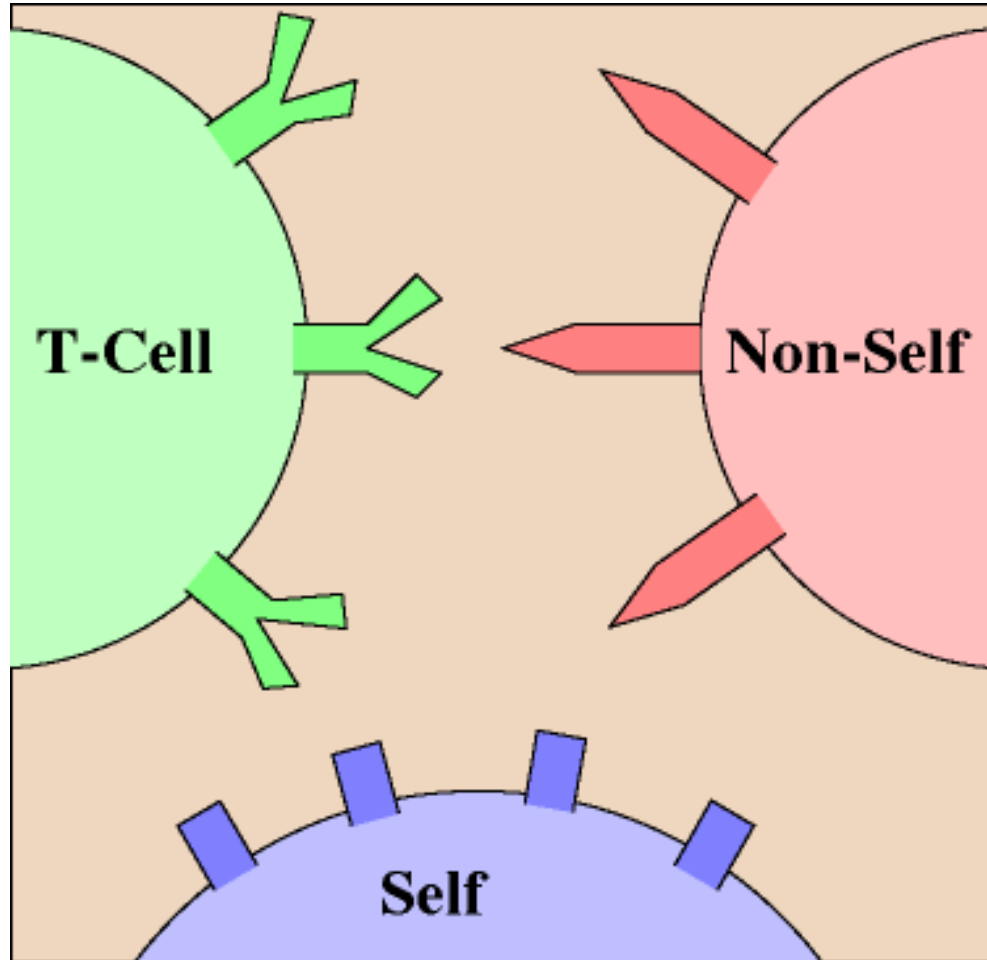
Clonal Selection Theory

- Each lymphocyte is a unique clone with its own specificity
- Negative selection
 - If an immature lymphocyte binds Ag^* , it dies
 - Mature pool of cells represents those that did not bind to Ag during development
- A mature lymphocyte is stimulated to divide when it encounters Ag^*
 - Clonal expansion



* Ag stands for antigen.

Negative Selection



Positive and Negative Selection

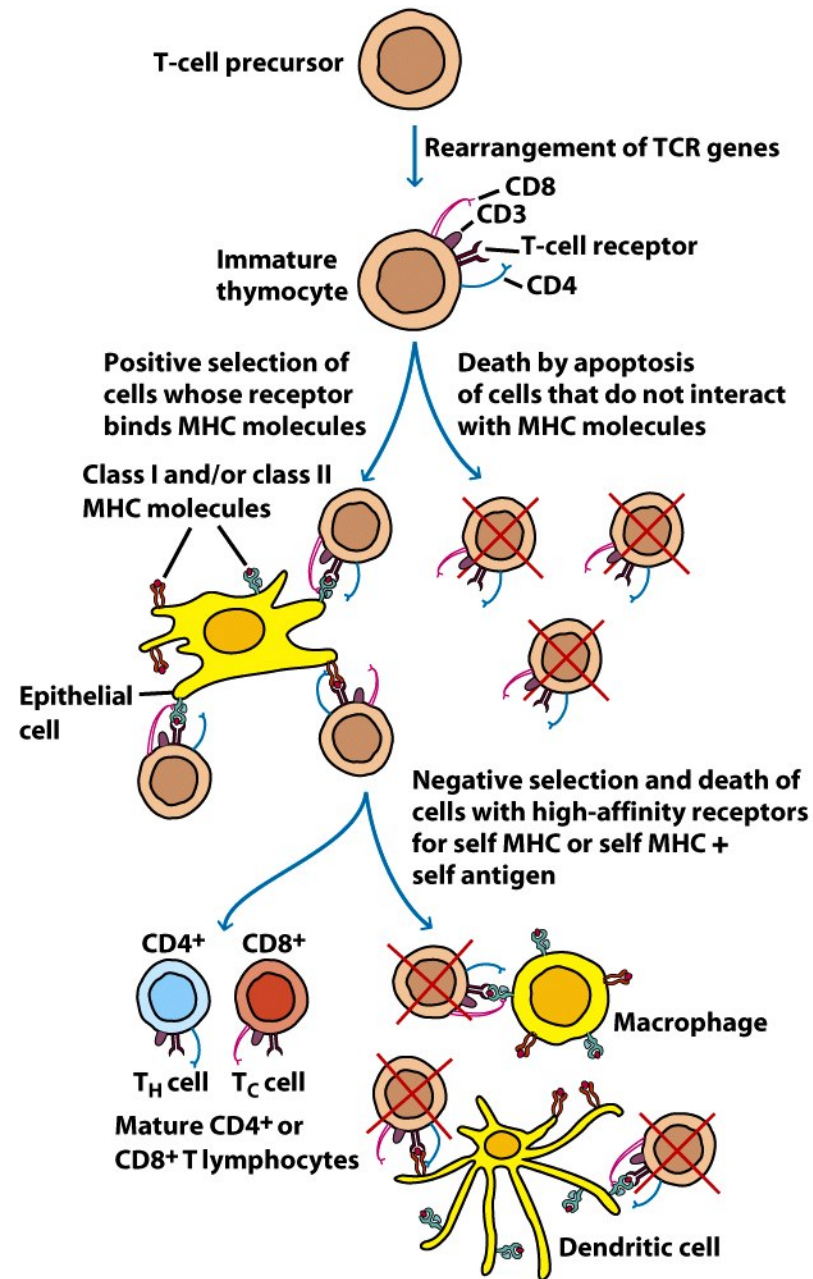
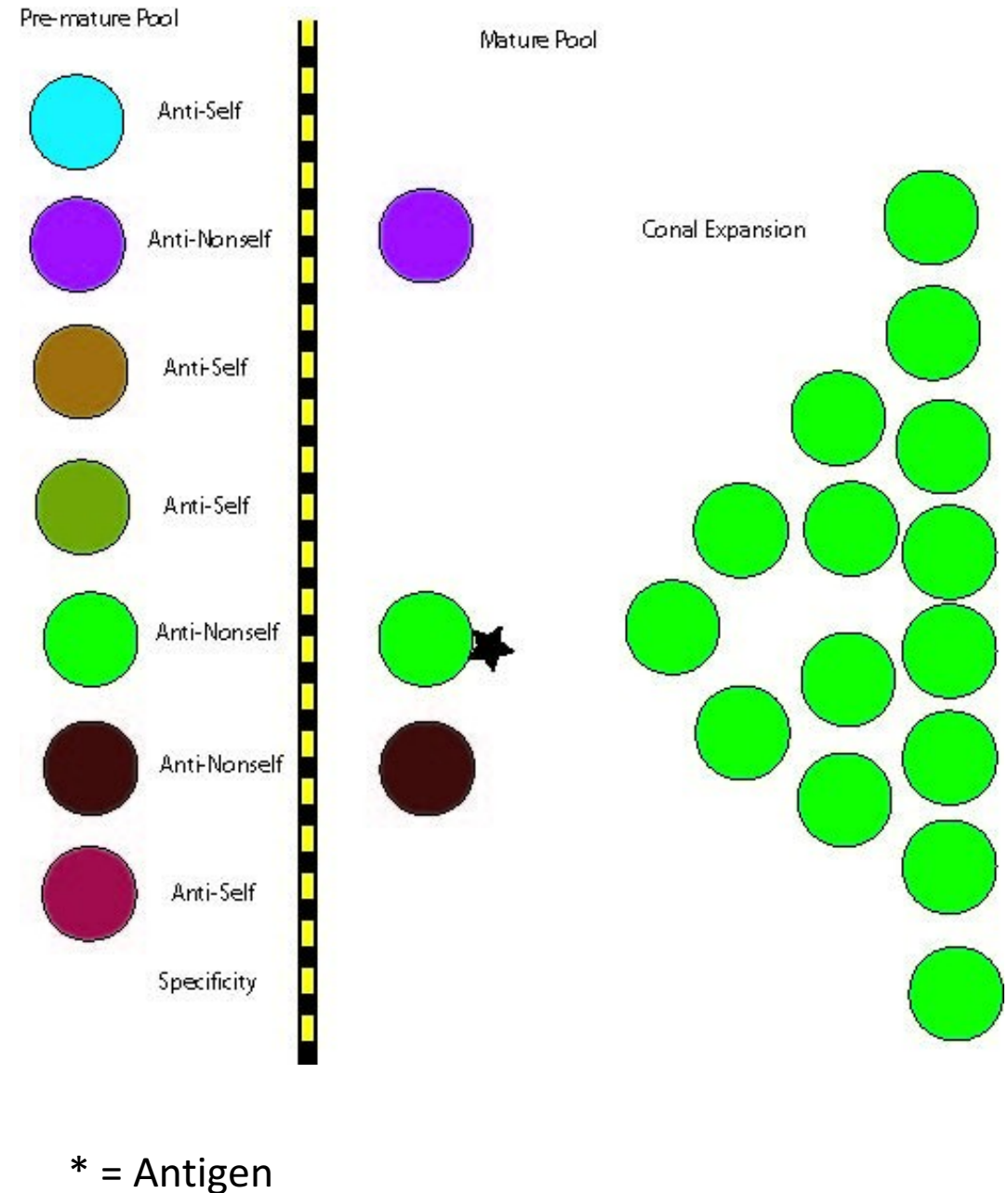
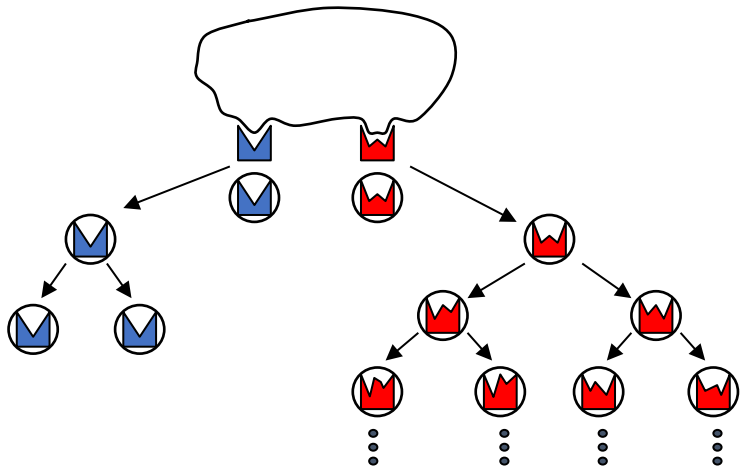


Figure 10-6
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Clonal Expansion

- B-cells compete for antigen
 - Affinity (binding strength)
 - Avidity (average affinity over all)
- Proliferation phase in LN
- Somatic hypermutation



Managing the Immune Response

- How does the immune system know what to respond to?
 - How does the immune system choose the type of response?
 - How does the immune system adjust the magnitude of response?
 - How does the response terminate?
-
- Experimentalists generally focus on the specific cell and molecule types required
 - A more abstract view focuses on general pattern matching and distributed control principles

Managing the Immune Response

- Complex network of signaling molecules, called cytokines
 - Interleukin, interferon, etc.
- Every cytokine type affects multiple cells
 - ~100 different cytokine types
- Every function (immune response) is affected by multiple cytokines
- Immune cells secrete a mixture (vector) of cytokines
- Signals are molecules, and therefore distributed (locally) by diffusion
- Signals can be subverted (e.g., viruses can evolve to avoid or interfere with cytokines, e.g., by blocking receptors), so there is an evolutionary pressure towards robust, secure networks
- Current state of knowledge
 - Many points of light
 - No systematic theory

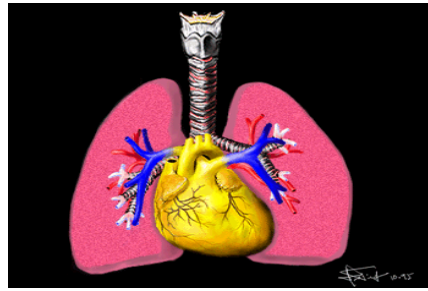
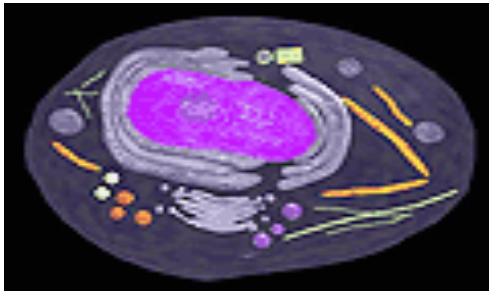
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 - No systematic theory

Compare to the foraging
strategies of ants

Modeling the Immune System

- Intracellular
- Organ
- Systemic

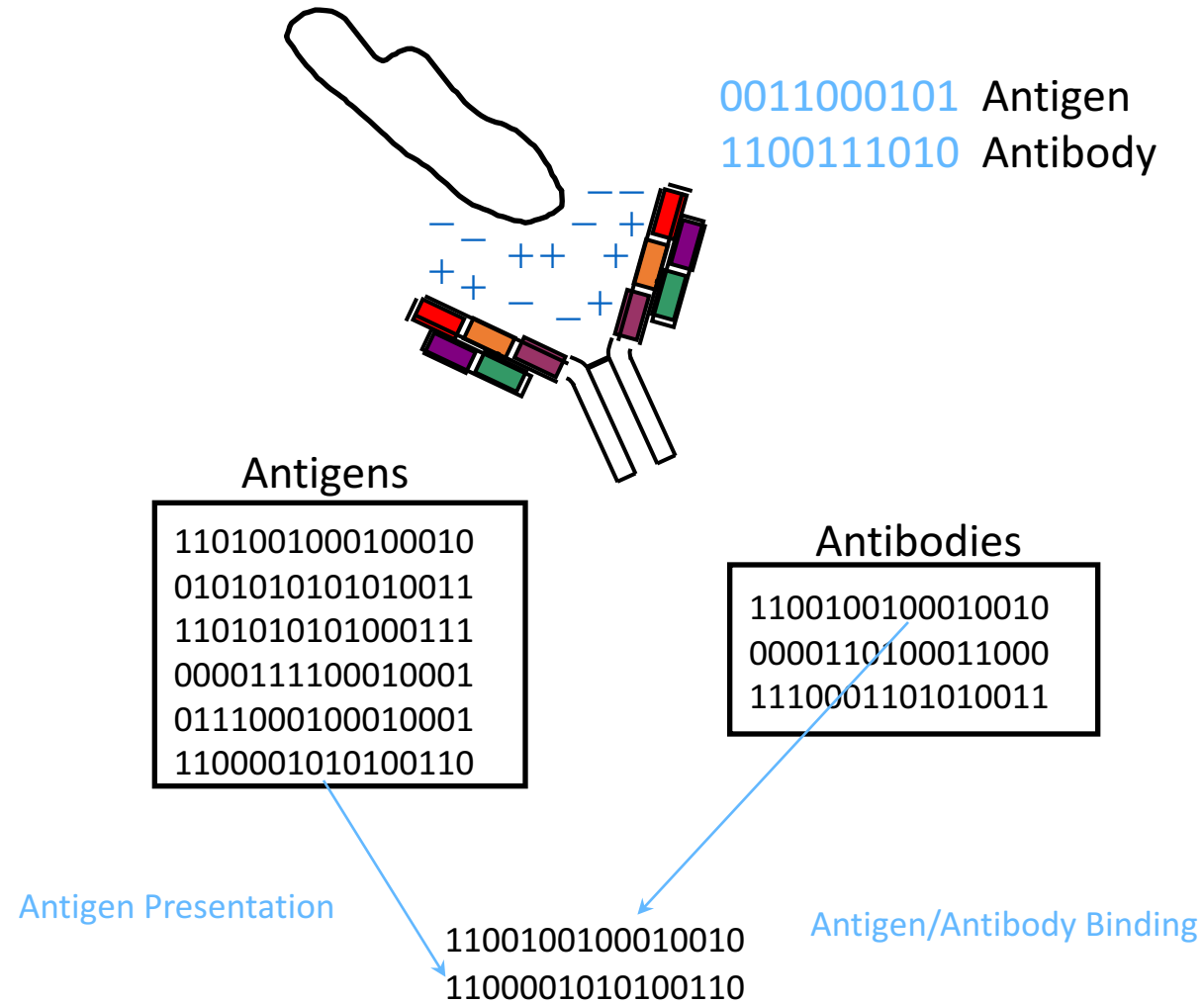


Approaches to Modeling Immune Systems

- Differential equations
 - Each equation describes the concentration of a different antibody/cell type
- Molecular dynamics simulations
- Agent-based models
 - E.g., cellular automata, genetic algorithms, and Smith's B-cell model
- Focus on informational aspects of immune systems

Artificial Immune Systems

Immune System Models



Mapping

Immune System

- Lymphocytes (b-cells, t-cells, antibodies)
- Pathogens (antigens)
- Proteins (nucleic acids)
- Inter-molecular binding
- Antibody/pathogen binding

Computer Science

- Detectors
- Intruders, foreign code
- Strings
- Partial string matching
- Pattern matching

Example AIS Application Areas

- Data mining and clustering
- Computer security
- Other anomaly detection problems
- Fault isolation and tolerance
- Recommenders and filterers
- Robotics
- Data storage

Aickelin, Uwe, Dipankar Dasgupta,
and Feng Gu.
"Artificial immune systems."
Search Methodologies. Springer
US, 2014. 187-211.

Hofmeyr, Steven A., and Stephanie
Forrest. "Architecture for an artificial immune system."
Evolutionary computation 8.4 (2000): 443-473.

