

# Complex Adaptive Systems

Examples from Biology with Computer Science Applications

Lecture 14

# Ant Colonies

Evolution of Altruism (compare Axelrod and The prisoners dilemma)

Is Altruism a Nash Equilibrium?

Ant defection.

Ants evolved from wasps about 100 million years ago.

There are an estimated 22,000 species.



E. O. Wilson  
Harvard University

Bert Hölldobler  
University of Würzburg

*The Superorganism: The Beauty, Elegance, and Strangeness of Insect Societies*

*The Ants*

*Insect Societies*



Deborah Gordon  
Stanford University  
Compares ant foraging  
To TCP/IP throttling  
(Desert Harvester and Argentine Ants)

# Planet of the Ants



10,000,000,000,000  
ants

10 quadrillion ants.



7,000,000,000  
humans

7 billion humans.

“Lean on a tree almost anywhere, and the first creature to crawl on you will probably be an ant.”

Holldobler & Wilson, *Journey to the Ants*

## QUEEN ANT



Queen ants are the founders of all colonies. Once mated, she can stay fertilized for many years laying millions of eggs. Some queens can lay thousands of eggs each day. They really are egg laying machines. In some species live up to 30 years. Some species have multiple queens.

## Worker Ants



Worker ants are sterile females. Can live up to 5 years. In *Pogonomyrmex* sp. the jobs the workers do depend on age not caste.

## Winged Princess | Alate | Virgin Queen



Mate with a drone during the nuptial flight. Stores enough sperm for the rest of her life. Her job is to find a good place for the colony, clip her own wings off and burrow as quickly as possible. Once underground she starts producing workers.

## Winged Drone | Alate | Male Ant



These are the only males in the colony. Males are haploid (only one set of chromosomes). Leave the colony during the nuptual flight and then die.

# Basic Ant Biology

- All ants are **eusocial**
  - The colony is the unit of selection
    - Queen(s): reproducers, not masterminds
    - Reproductives: winged male and female alates
    - Workers: female, short lived compared to queens
  - Genetic sex determination
    - Haplodiploidy
    - Sociobiology
  - Division of labor:
    - All males are reproductive
    - Female **caste** determined by environment & larval feeding
    - Assignment to task groups is determined by colony need
    - Emergence of cooperative foraging, learning, farming, herding..
- Communication through **pheromones and antennal contact**
- **Self organization** (dumb ants, smart colonies)



# Haplodiploid sex determination

- Sex is determined by the number of sets of chromosomes
  - Females are diploid: usual case in sexual reproduction: genes are inherited from mother + father
  - Males are unfertilized: all genes come from the egg (mother)
  - Males have  $\frac{1}{2}$  the number of chromosomes as females (haploid)
  - Males have no fathers and can only produce daughters
  - The queen determines\* how many males and females to make
- Female workers could produce sons, however, females are more related to their sisters (queens produced by her colony) than to their sons

<u>Sex</u>	Daughter	Son	Mother	Father	Full Sister	Full Brother	
<b>F</b>	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{4}$	
<b>M</b>	1	-	1	-	$\frac{1}{2}$	$\frac{1}{2}$	

This depends on all the offspring of the queen resulting from a single mating.

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How does this relate  
To Nash Equilibrium?

<u>Sex</u>	Daughter	Son	Mother	Father	Full Sister	Full Brother	
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This depends on all the offspring of the queen resulting from a single mating.

20 ants per colony

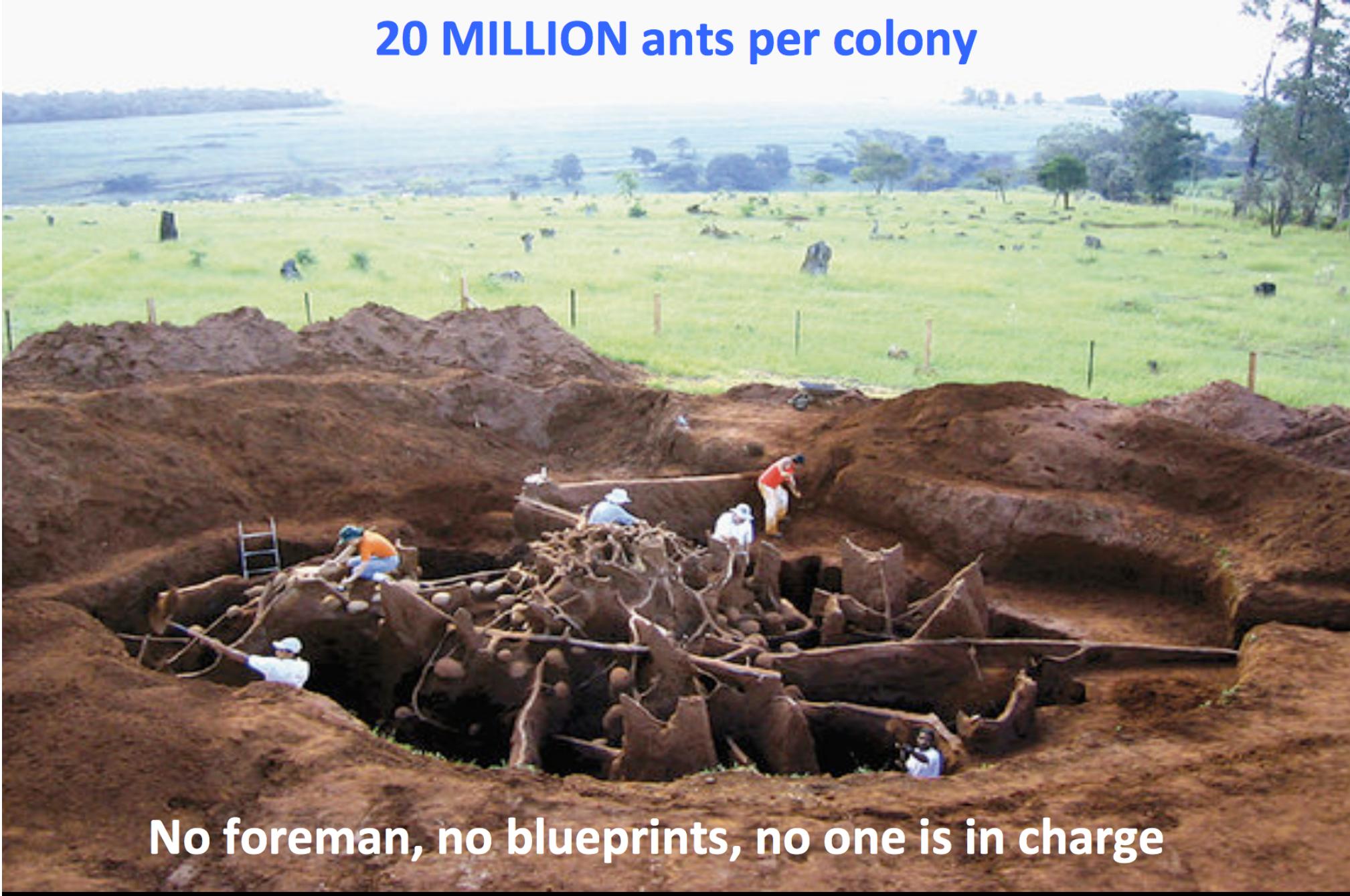


© alexanderwild.com

**20 MILLION ants per colony**



**20 MILLION ants per colony**

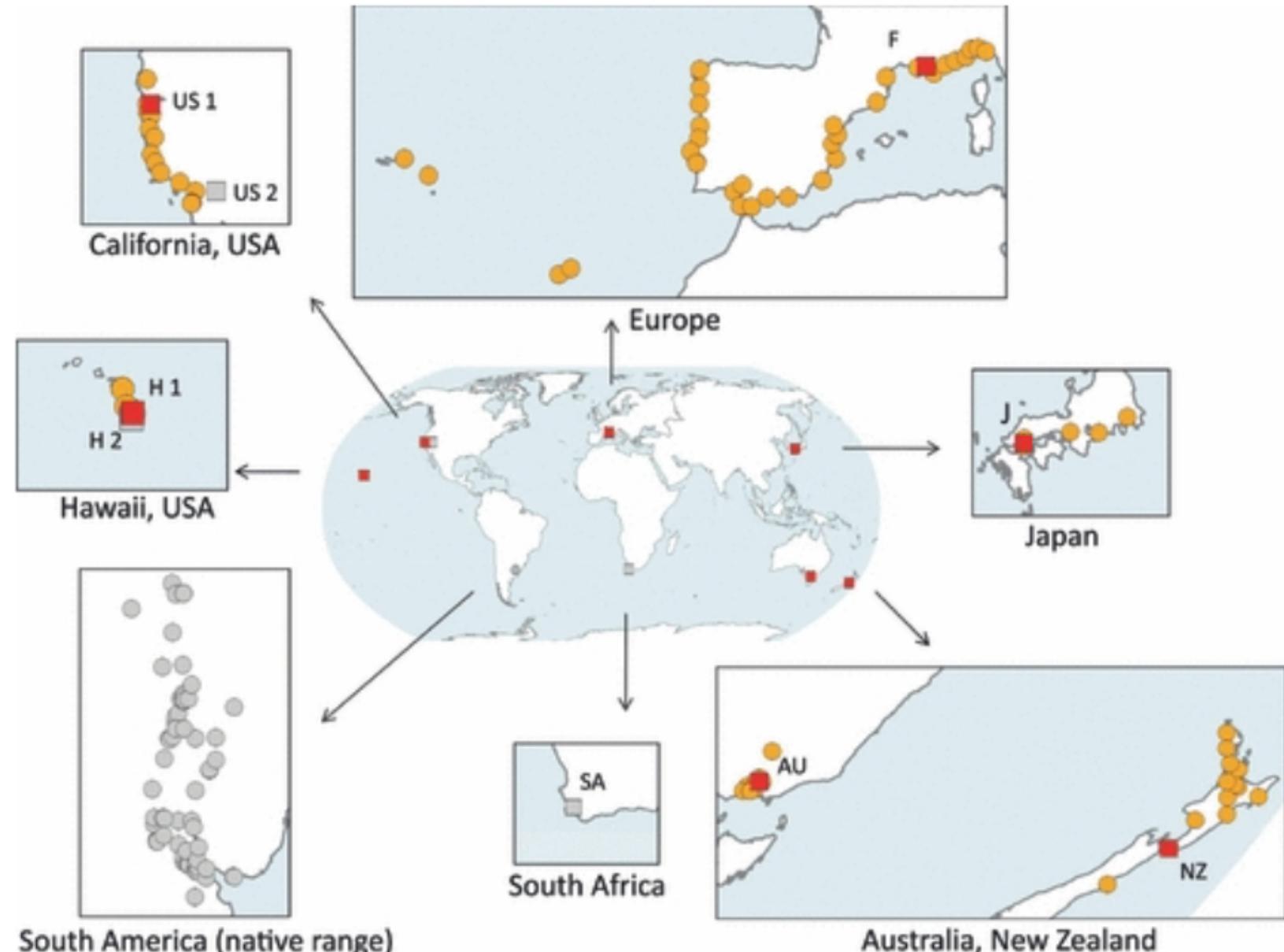


**No foreman, no blueprints, no one is in charge**

# Cooperation

- Most ants use chemical signals to mark divisions between colonies.
- Argentine ants create multiple nests.
- Humans accidentally transported colonies of ants from South America around the world
- . Since there were no other Argentine ant colonies to compete with those founder ants have expanded one giant colony in each region.
- These are called super or mega-colonies.

The largest of these Argentine ant Supercolonies is 6,000 km long (Europe).



Van Wilgenburg, Ellen, Candice W. Torres, and Neil D. Tsutsui. "The global expansion of a single ant supercolony." *Evolutionary Applications* 3.2 (2010): 136-143.

# Cooperation in Superorganisms



# 4 simple behaviors → cooperative foraging

- Count
- Remember
- Communicate
- Move



Seeds



Steps



Interactions

# 4 simple behaviors → cooperative foraging

- Count
- **Remember**
- Communicate
- Move

## Site Fidelity

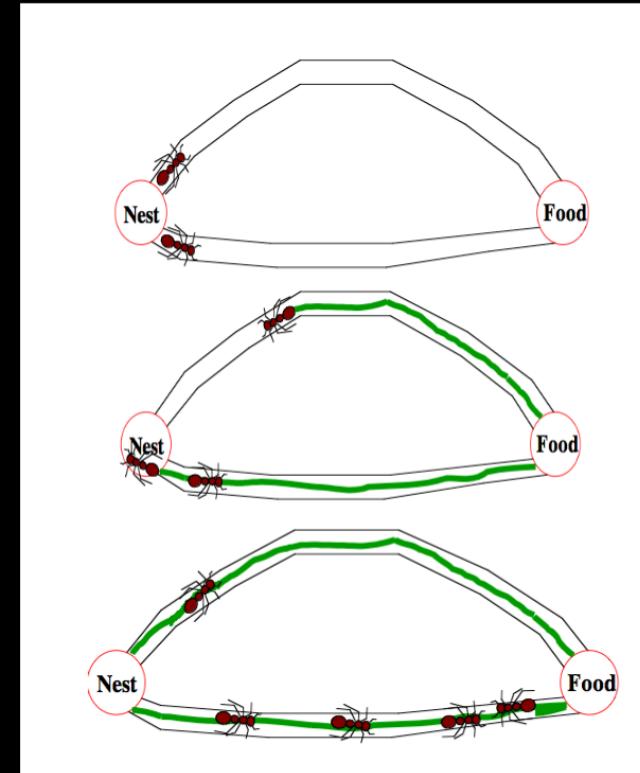
*There and back again...and again*



# 4 simple behaviors → cooperative foraging

- Count
- Remember
- **Communicate**
- Move

Pheromones

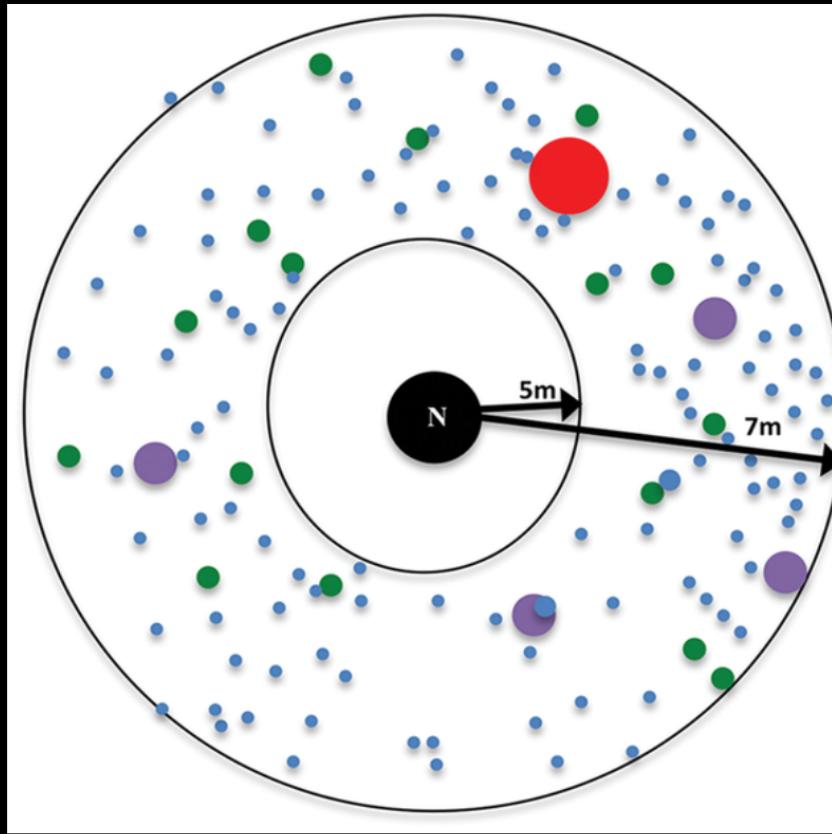


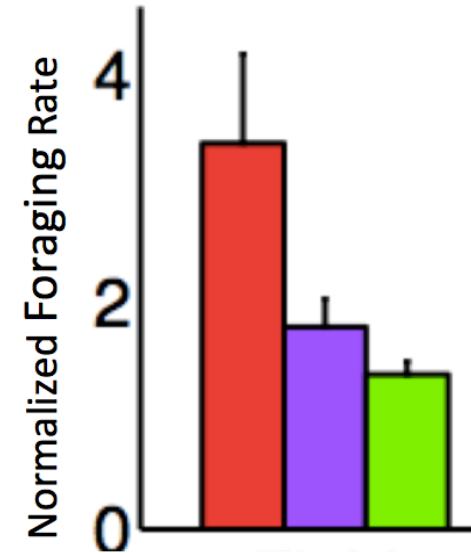
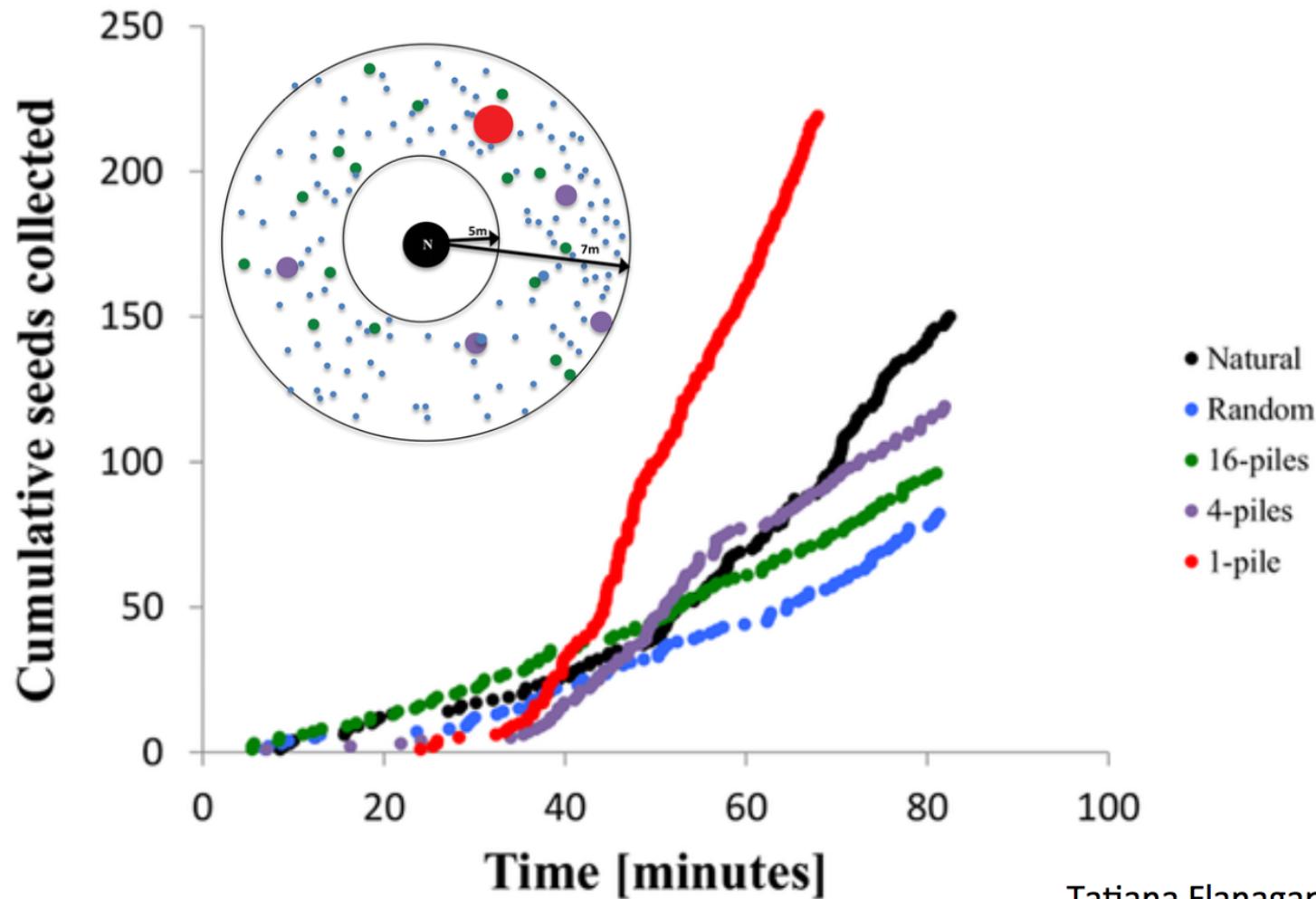
# 4 simple behaviors → cooperative foraging

- Count
- Remember
- Communicate
- **Move**
  - Travel
  - Search
    - Thoroughly
    - Broadly



# How does complex foraging emerge from interactions among these 4 behaviors?

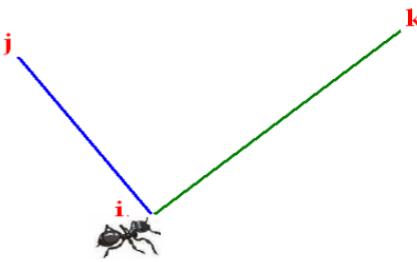
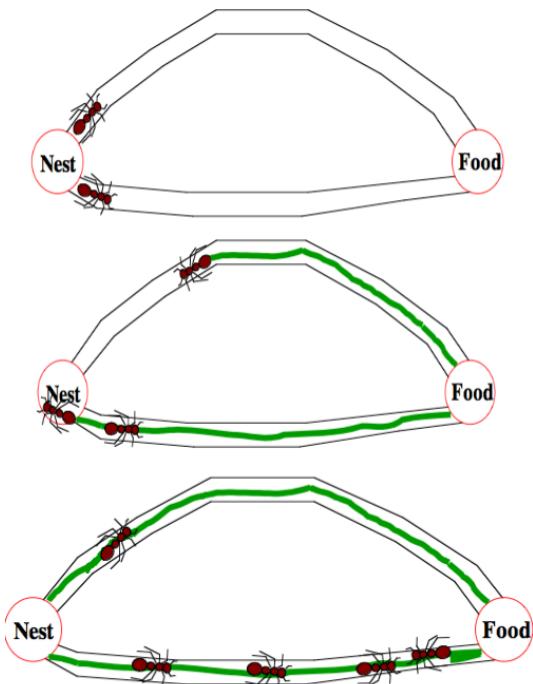




Tatiana Flanagan et al Alife 2011, PLoS ONE 2012

How should ants behave to collect seeds as fast as possible?

# Pheromone recruitment: a well-studied emergent behavior



$$p_{ij}^k(t) = \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{l \in N_i^k} [\tau_{il}(t)]^\alpha \cdot [\eta_{il}]^\beta} \quad \text{if } j \in N_i^k$$

Ant colony optimization

# Memory vs. Communication

## Site Fidelity

*There and back again*



# Memory vs. Communication

private vs. public information

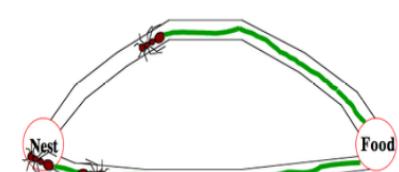
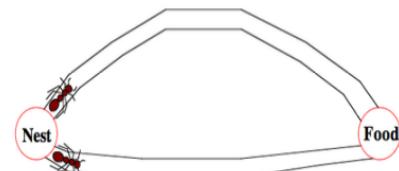
## Site Fidelity

*There and back again*



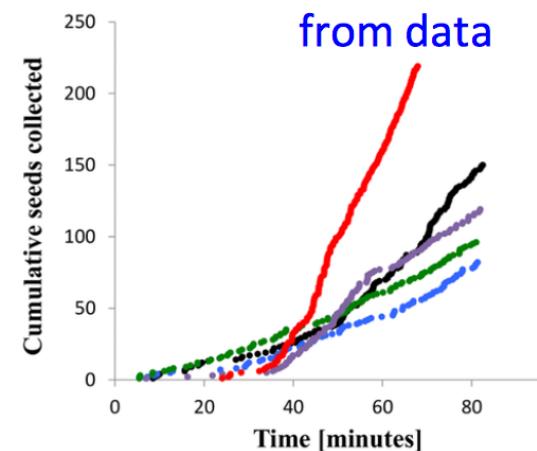
## Pheromone Communication

*Recruit nestmates*



$$p_{ij}^k(t) = \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{l \in N_i^k} [\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta} \quad \text{if } j \in N_i^k$$

Both processes are  
indistinguishable  
from data



# Agent Based Model

How important is remembered vs. communicated information?

Ants search for food on a grid

Travel from the nest

Move with directed & random walks

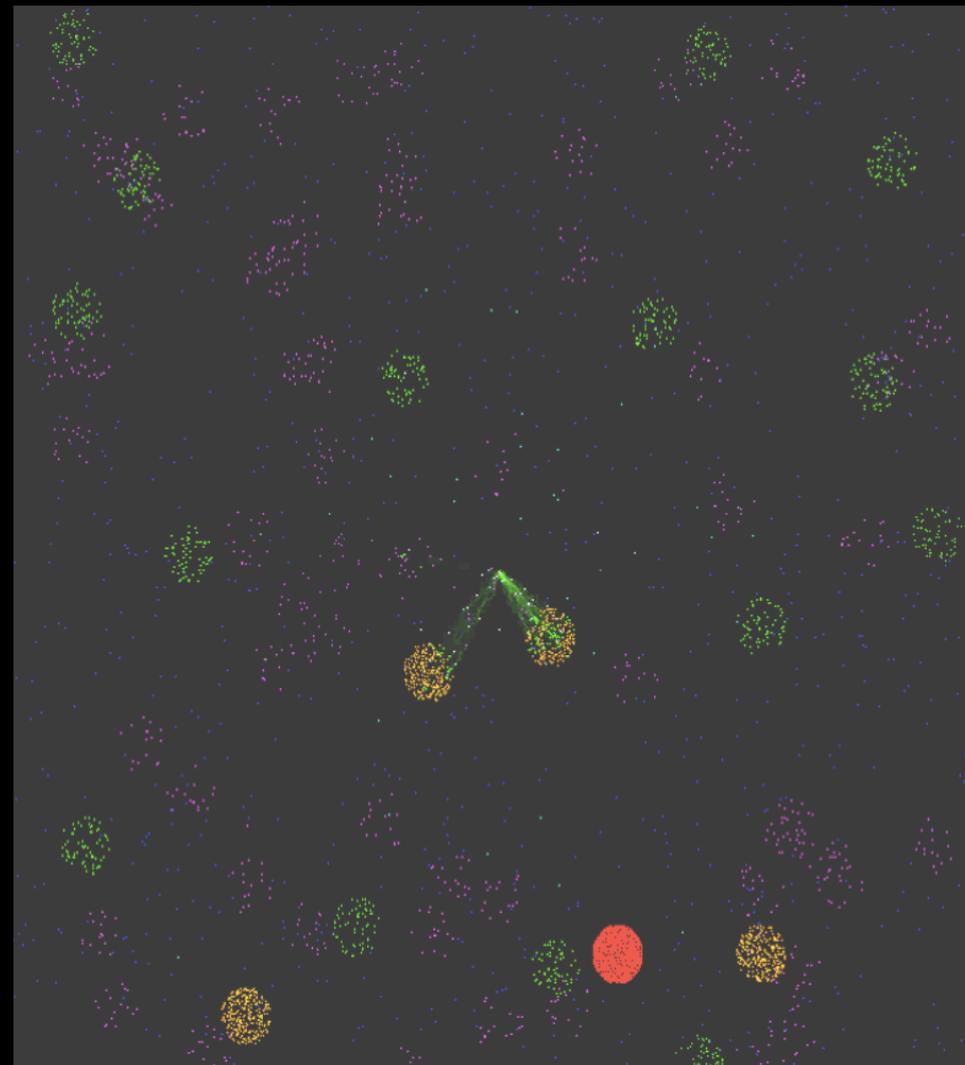
Upon finding food, ants

Count the seeds nearby

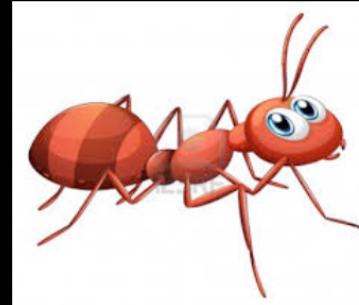
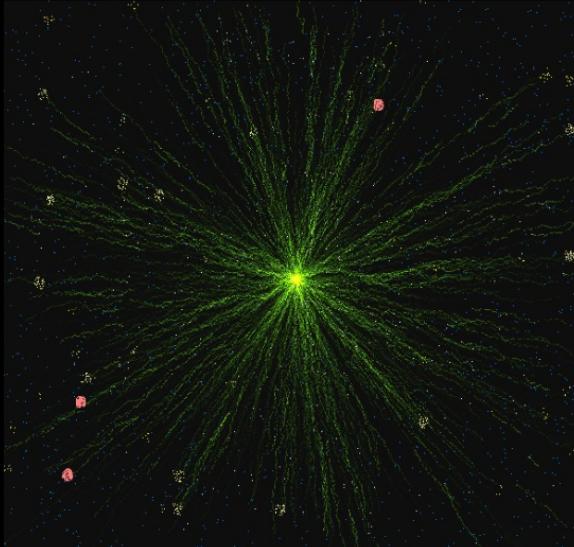
Decide whether to use

- memory (site fidelity) or
- communication (pheromones)

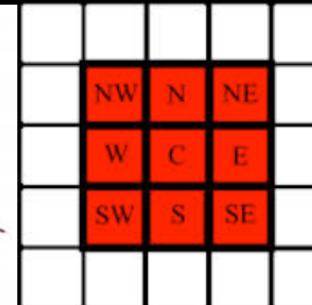
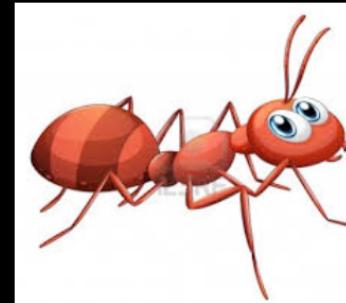
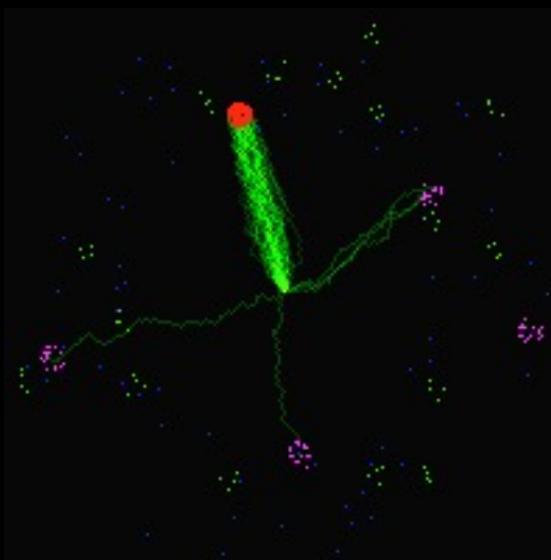
GOAL: Combine behaviors in individuals  
to maximize seeds collected by colony



# Foraging success depends on interactions among behaviors

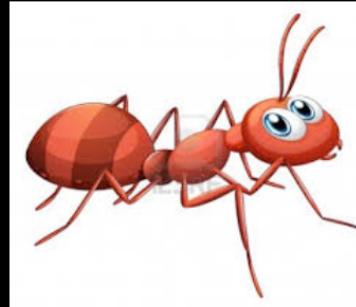
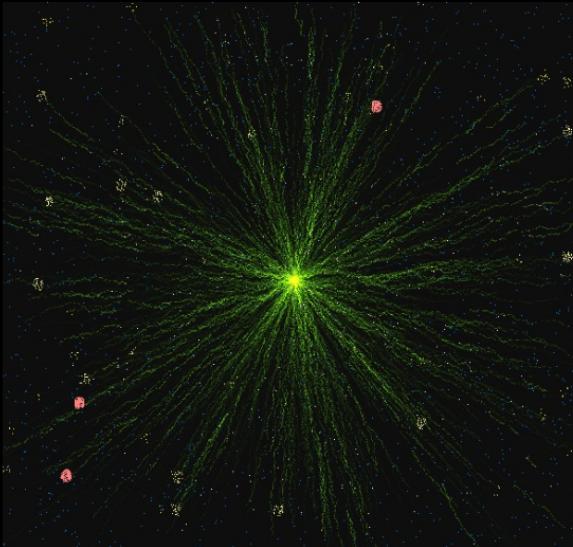


Lay pheromone  
Whenever I find a seed



Lay pheromone  
Only if count > 5

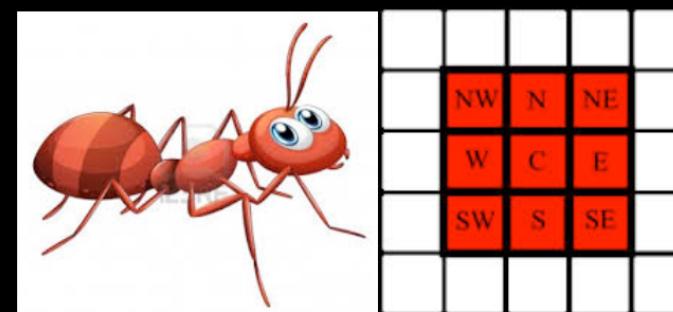
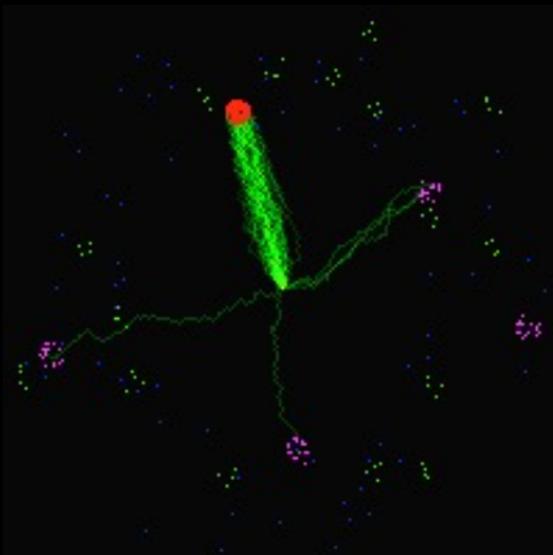
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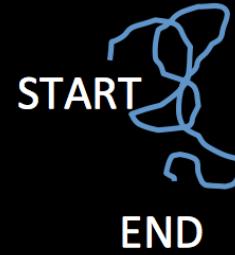
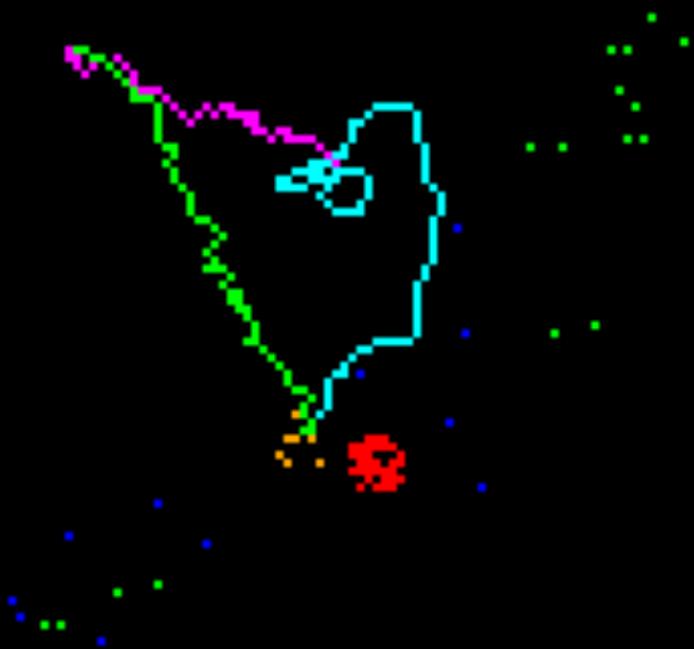
Decision to lay pheromones or use site fidelity  
depends on seed density in the current pile

Communication & memory interact with counting



Lay pheromone  
Only if count > 5

# Foraging success depends on interactions among behaviors

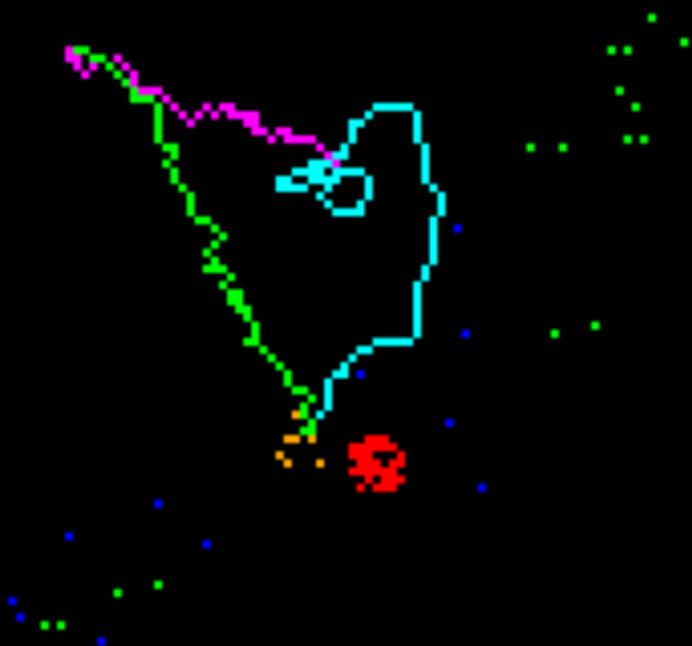


**Informed  
Walk**

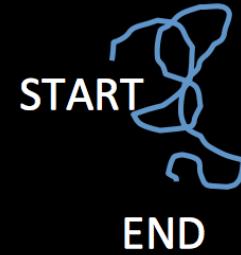
After returning via site fidelity or  
following a pheromone trail  
turn often to search thoroughly

Movement interacts with  
communication & memory

# Foraging success depends on interactions among behaviors



Movement interacts with communication & memory



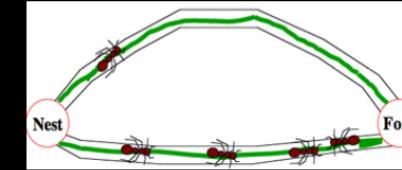
**Informed Walk**

After returning via site fidelity or following a pheromone trail turn often to search thoroughly



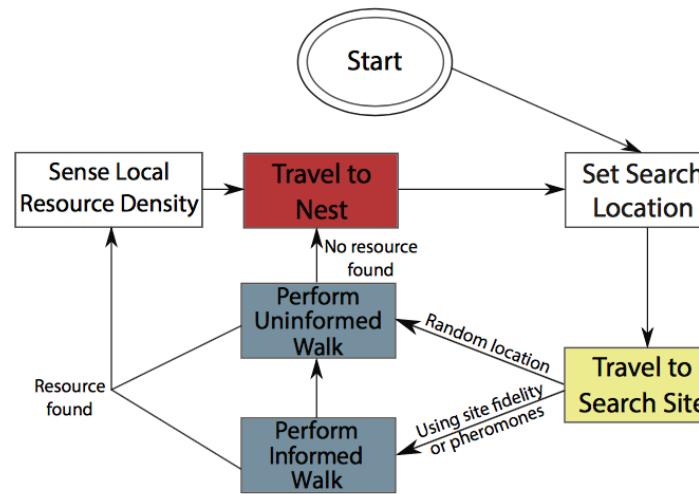
**Uninformed Walk**

When searching at random, walk in persistent directions to search widely



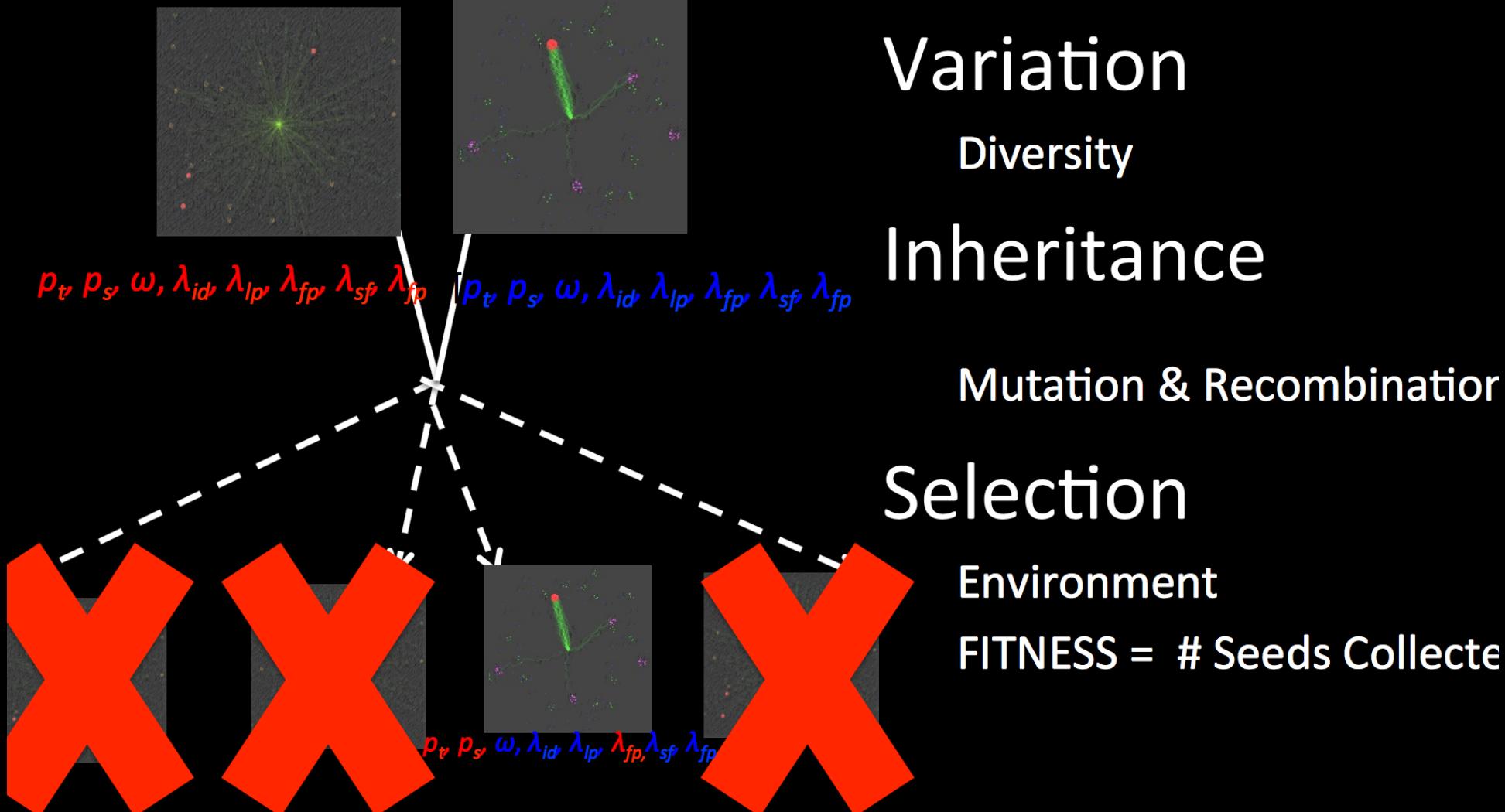
Collective Foraging success depends on **interactions**  
among ants  
*and*  
between ants & their environment

Computer algorithms “evolve” ant behaviors  
to maximize seed collection in fixed time

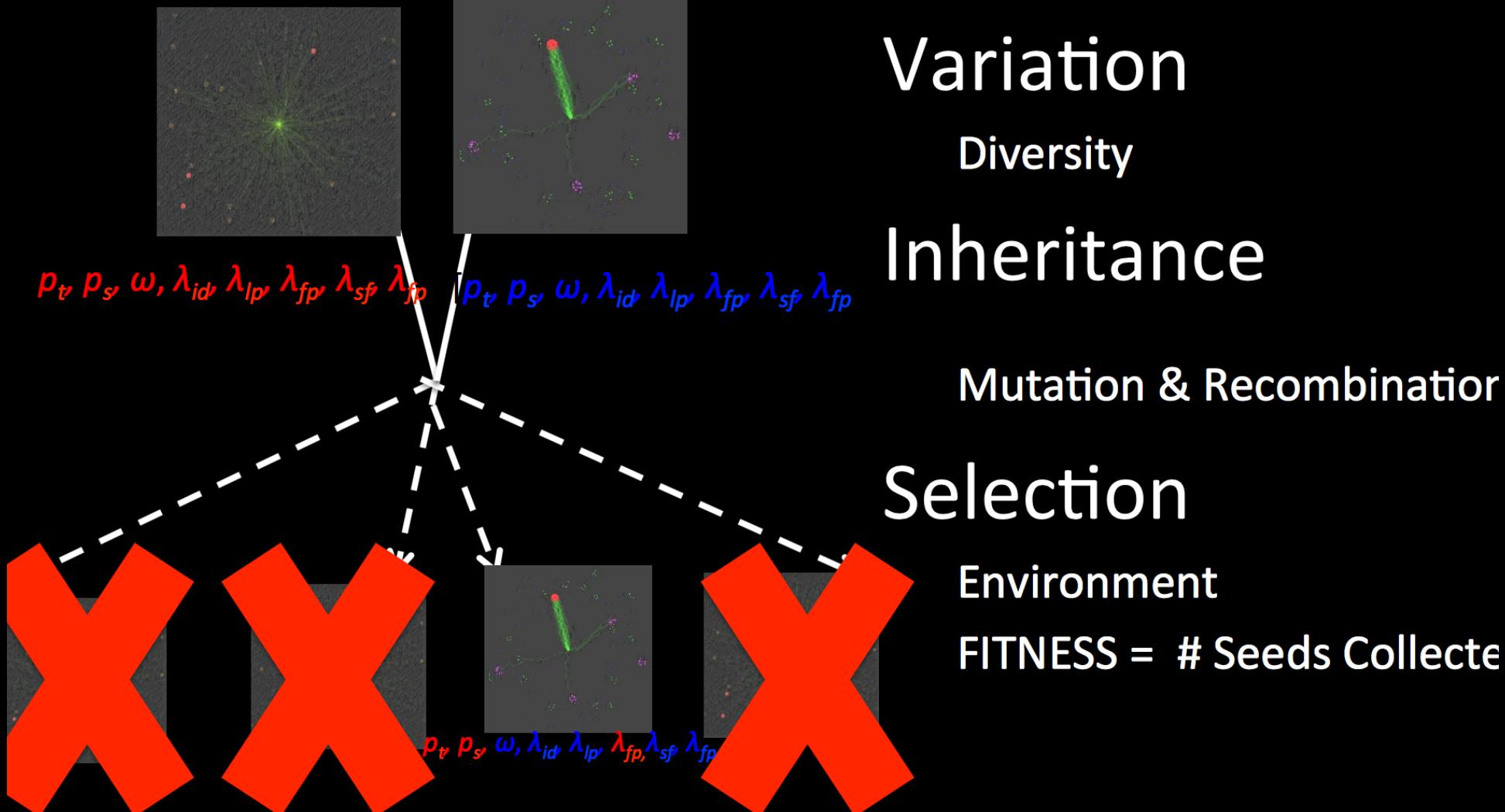


Parameter	Description	Function
$p_t$	Probability of switching to traveling	—
$p_s$	Probability of switching to searching	—
$\omega$	Uninformed search correlation	$\sigma = \omega$
$\lambda_{id}$	Informed search decay	$\sigma = \omega + (4\pi - \omega) * e^{-\lambda_{id}*t}$
$\lambda_{lp}$	Rate of laying pheromone	$F_{lp}(x) = 1 - e^{-\lambda_{lp}*(x+1)}$
$\lambda_{fp}$	Rate of following pheromone	$F_{fp}(x) = 1 - e^{-\lambda_{fp}*(9-x)}$
$\lambda_{sf}$	Rate of site fidelity	$F_{sf}(x) = 1 - e^{-\lambda_{sf}*(x+1)}$
$\lambda_{pd}$	Rate of pheromone decay	$e^{-\lambda_{pd}*t}$

# Genetic Algorithms



# Genetic Algorithms



# GA selects parameters to maximize seeds collected in fixed time

## Group Selection Experiments *in silico*

Each model run requires a set of input parameters  $[p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}]$

Each individual in a colony is identical

Cross over and mutation on parameters

G0:  $[p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}] \times [p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}]$

G1:  $[p_t, p_s, \omega, \lambda_{id}, \lambda_{lp}, \lambda_{fp}, \lambda_{sf}, \lambda_{fp}]$

100 runs with different parameter sets (colonies) for 100 Generations

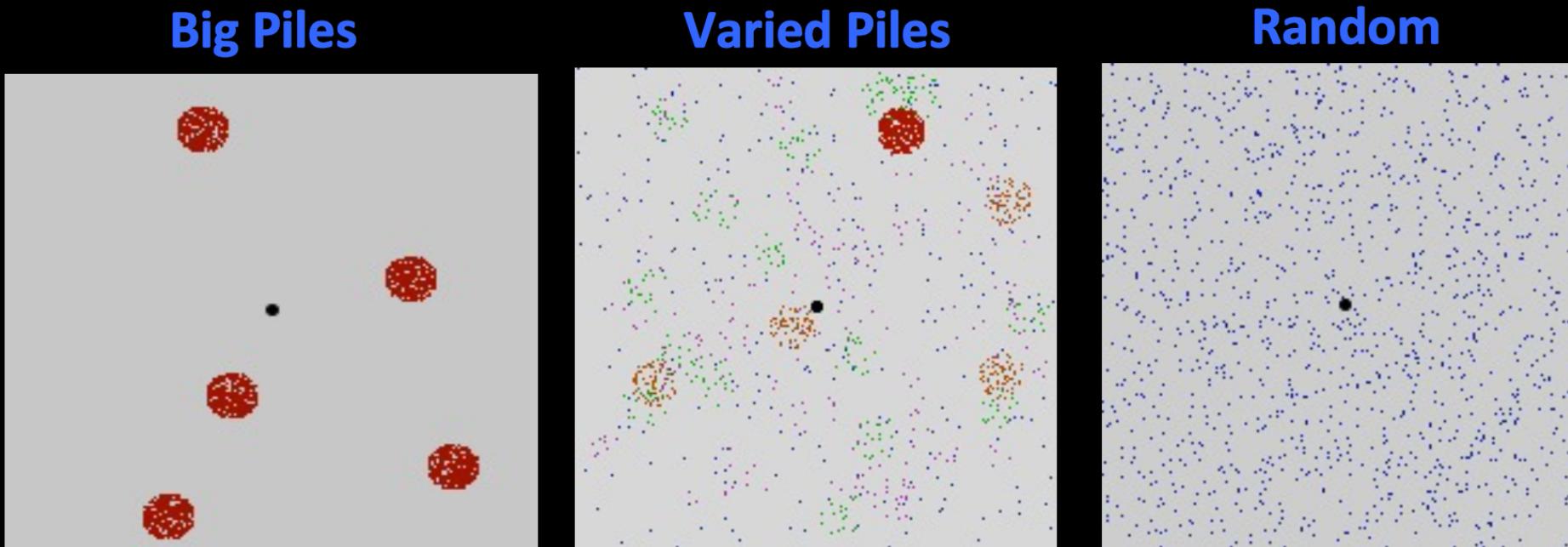
Each colony, each generation, evaluated on 8 grids for 20,000 time steps

Colonies with highest 'fitness' (seeds collected) replicate into next generation

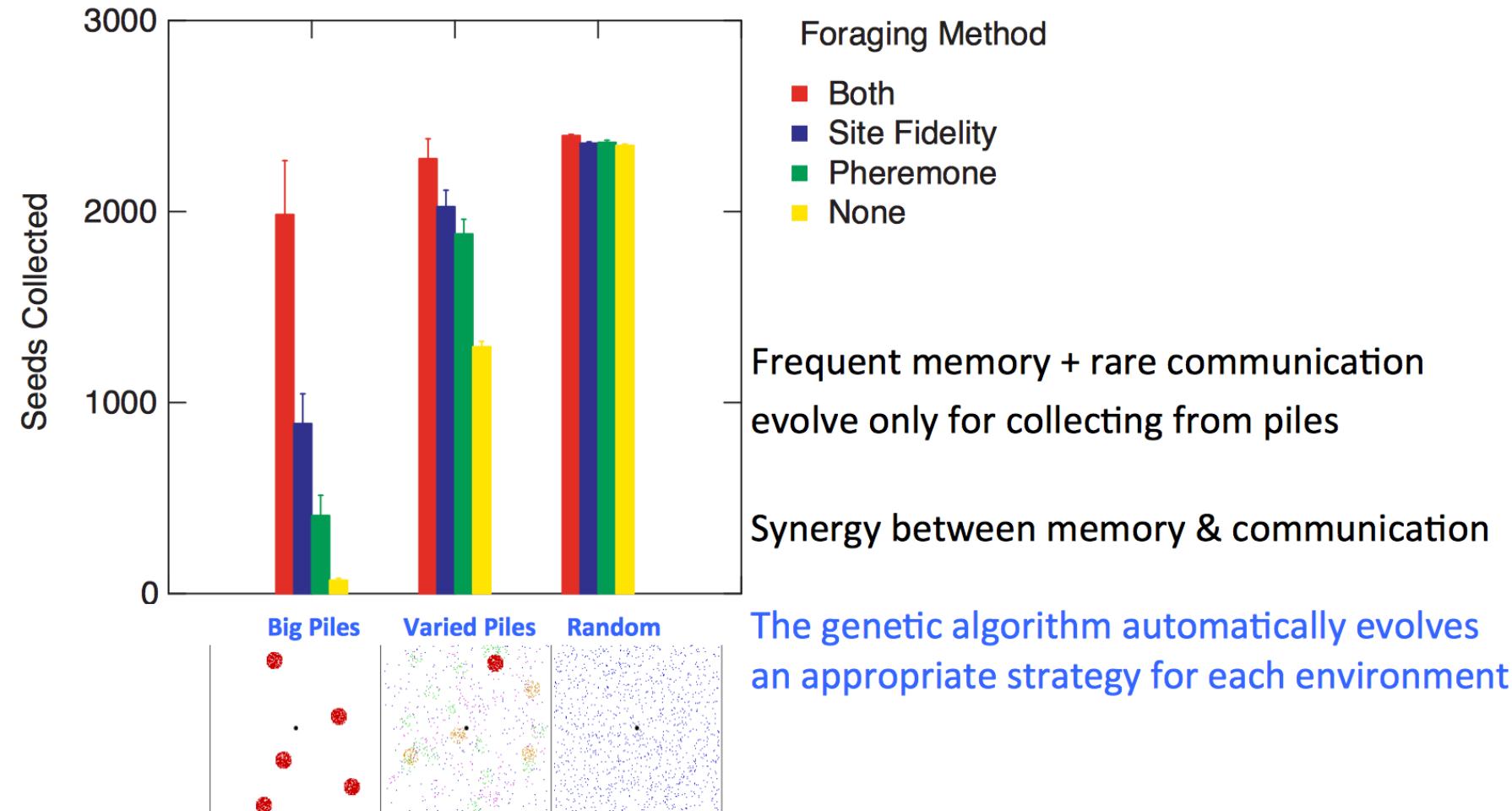
Run for colony sizes 10, 100, 1000, 10,000 foragers

**RESULT: Simulated colonies 'evolved' to maximize foraging rate**

# Simulated colonies evolve to collect from different environments

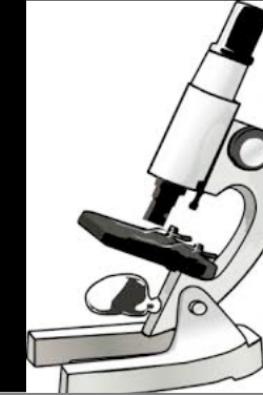
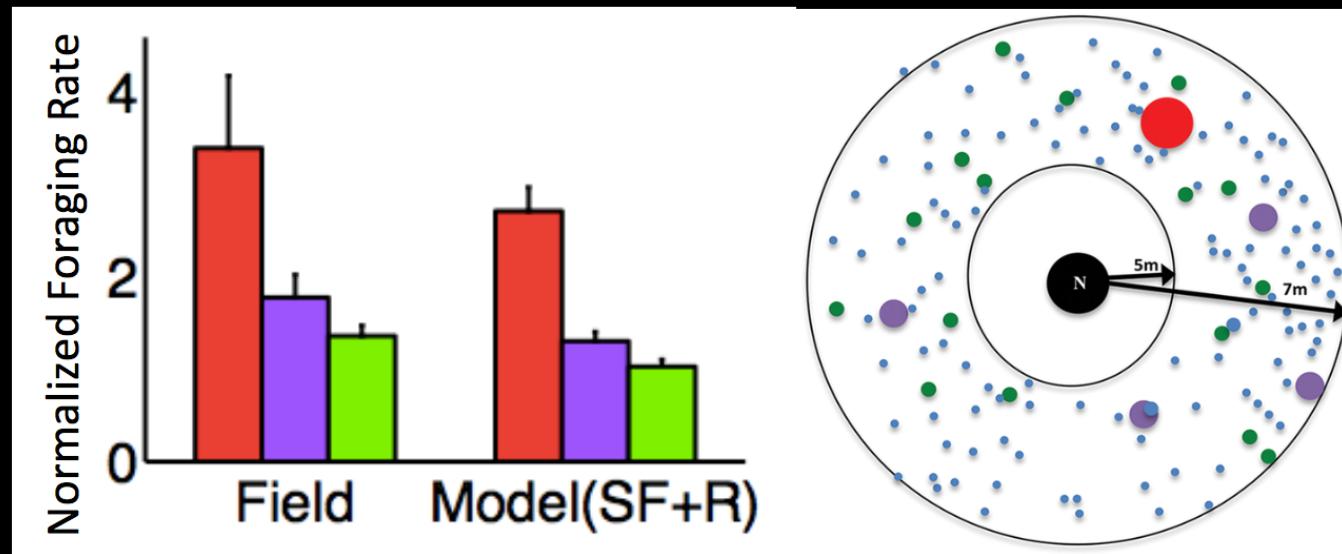


# Different strategies are useful in different environments

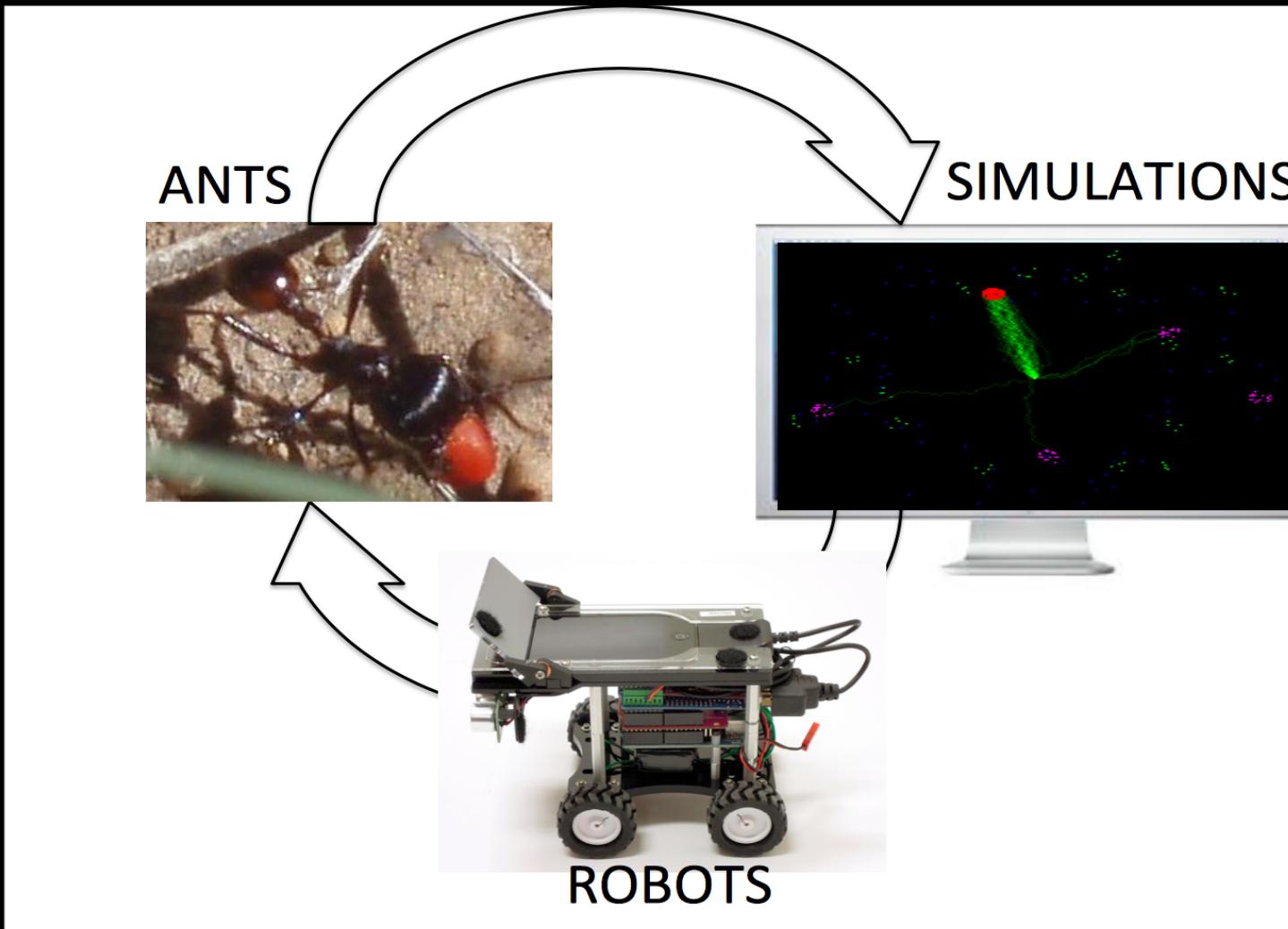


# Real ants forage as efficiently as simulated ants

Simulations reveal interactions among ants and their environment that lead to efficient foraging



# Program robots to cooperate using ant-like behaviors



# iANT SWARM ROBOTS

How can robots cooperate to search effectively  
in variable environments with noise, error,  
and no one in charge?



# Problem we are trying to solve: Central Place Foraging

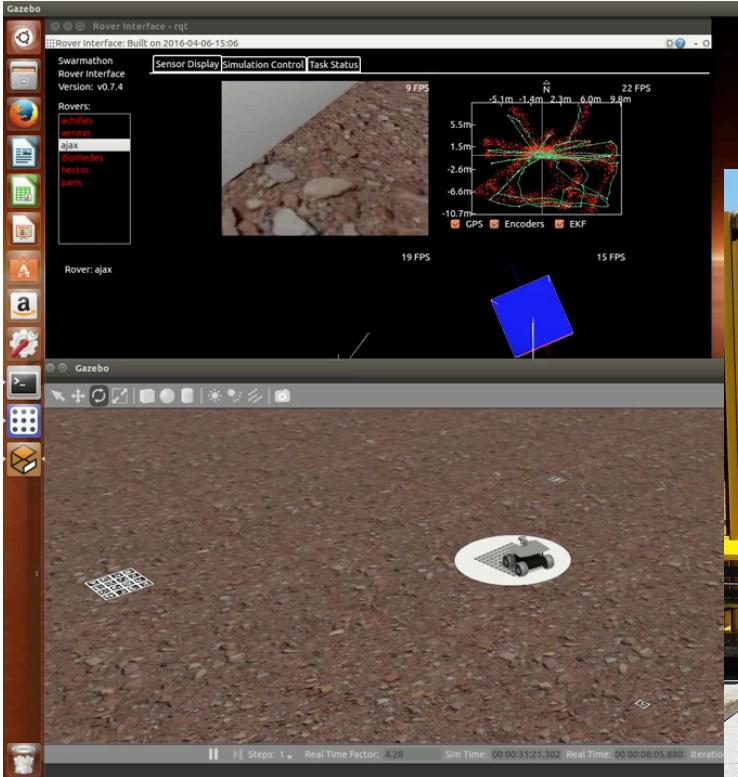


Introduction

# ‘Living off the land’ - Mars 2030



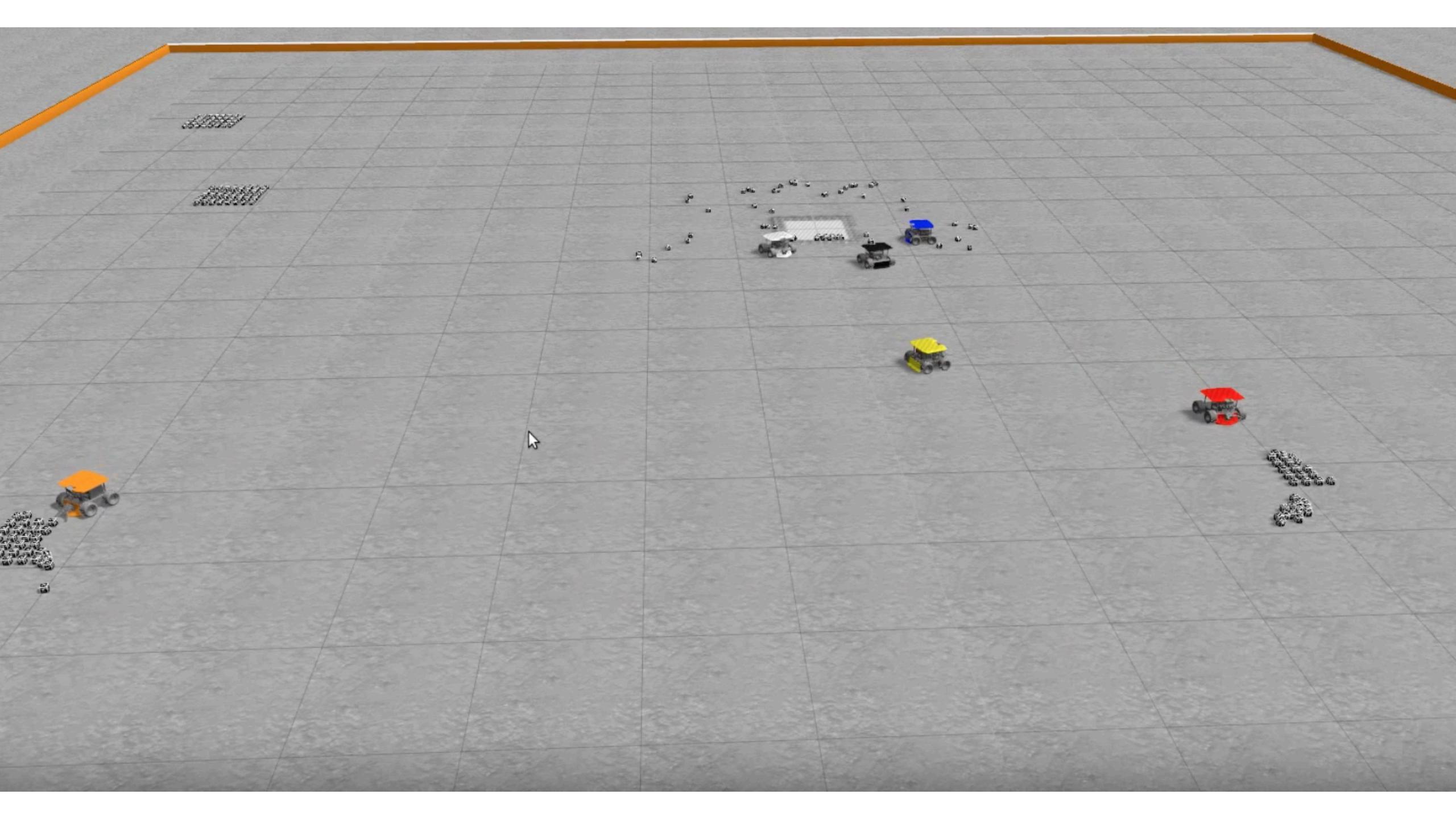
[nasaswarmathon.com](http://nasaswarmathon.com)

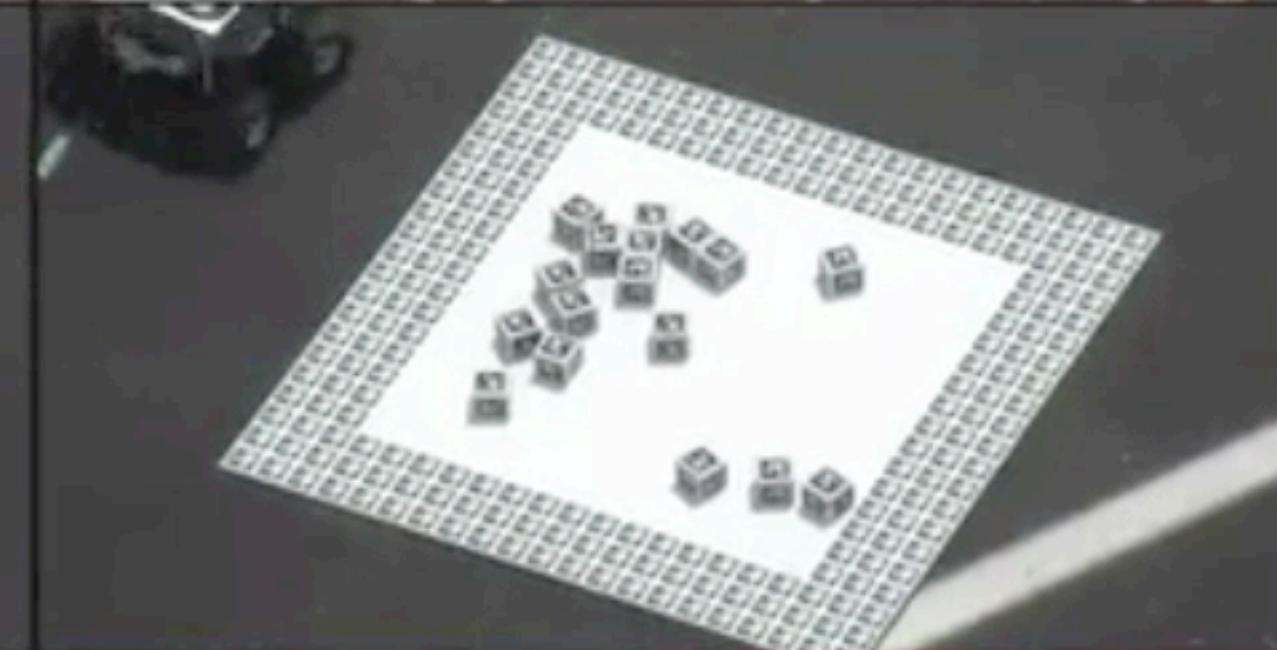
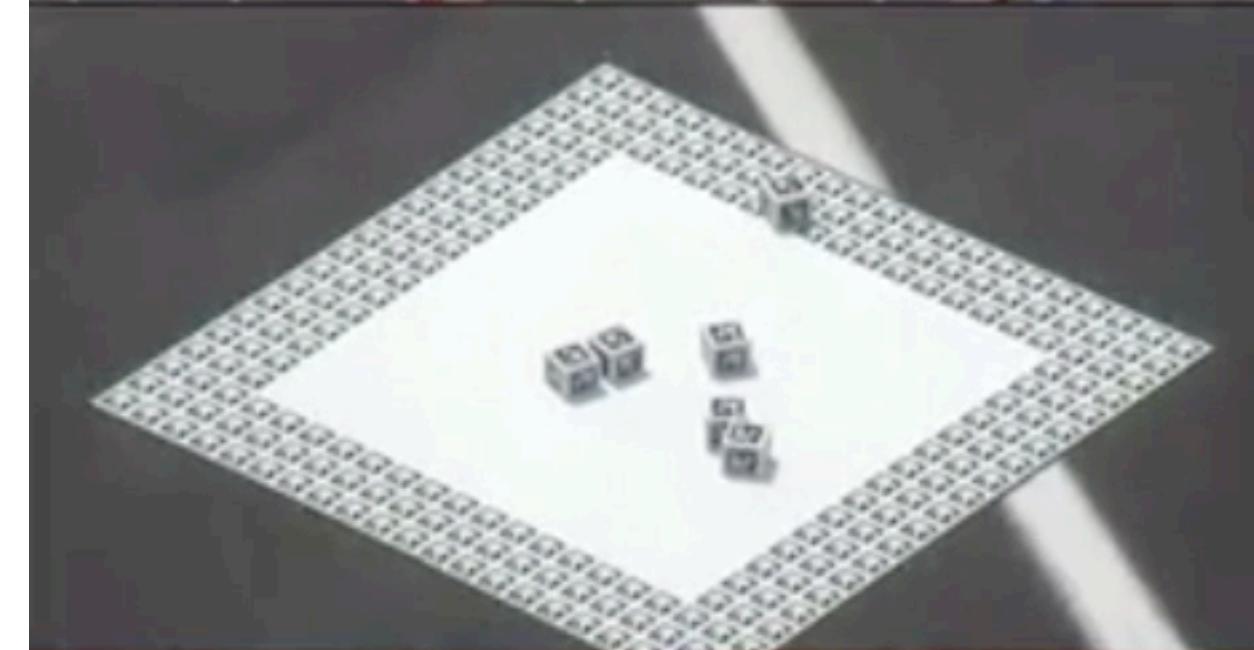


Managed by UNM, 40 colleges  
and universities competed  
Build ~100 robots so far...

Introduction





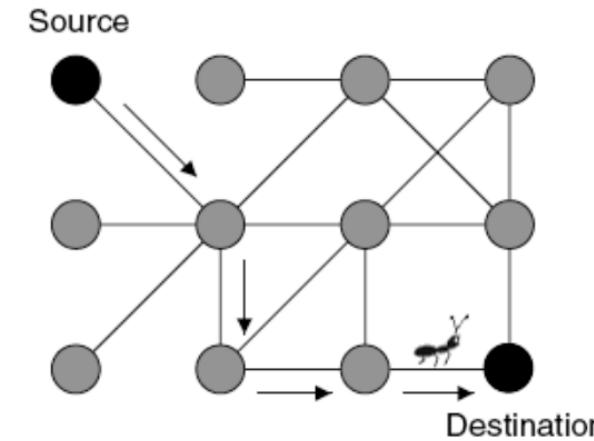


# Ant Colony Optimisation (ACO)

# Key Concepts From Dorigo's ACO

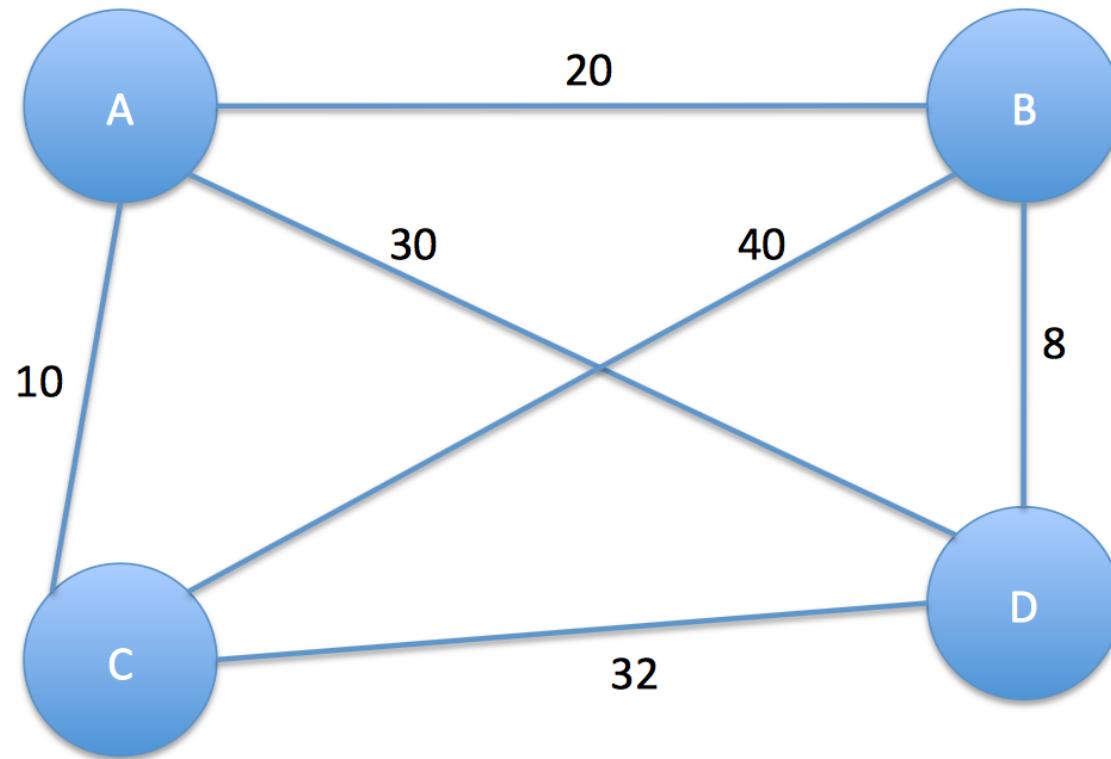
- Ant algorithms use ‘self-organizing principles’ to coordinate agents to solve computational problems
- Stigmergy: indirect communication and coordination through signals that modify the environment and stimulate other agents
- Pheromones: a chemical signal that triggers a response in another agent
  - Pheromone concentration increases the probability that an ant will follow a path
  - Evaporation removes stale solutions and mitigates premature convergence

# Simple-ACO



- S-ACO modifications of previous models
  - Ants remember their paths
  - Only backward pheromone deposition
  - Deterministic backward path
  - Pheromone evaporation
  - Pheromone deposition rate depends on quality of solution (ants deposit more pheromone on shorter paths)
  - Loop avoidance

# Use the Ant System ACO to solve this TSP



# Ant System

- Pheromone is stored in a matrix
- Heuristic information (distances between nodes) is stored in another matrix
- Ants remember where they've been on a given tour and do not repeat cities

Initialize Pheromone

While termination condition not met

    Construct Ant Solutions

        For each ant,

            choose a start city,

            construct a tour, biasing steps by pheromone, until it returns home

    Optionally Apply local search

    Update Pheromone

endwhile

Variations: elitist, rank based, max-min: alter pheromone deposition and update

# Ant System

- Ant cycle: pheromone deposit is determined globally (not very ant like) based on the length of the tour
- Initialization:

Initialize pheromone and

$$\tau_{i,j} = \frac{m}{C^{nn}} \quad m = \# \text{ ants}$$

heuristic information for all  $i, j$ :

$$\eta_{i,j} = \frac{1}{d_{i,j}} \quad C^{nn} = \text{length of nearest neighbor CYCLE}$$

$d_{i,j} = \text{distance from } i \text{ to } j$

We define the transition probability from town  $i$  to town  $j$  for the  $k$ -th ant as

- Tour construction formula
- What do alpha and beta represent?

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

# Ant System

## The amount of pheromone on edge $(i, j)$

of the tour

- Initialization:

Initialize pheromone and

heuristic information for all  $i, j$ :



$$\tau_{i,j} = \frac{m}{C^{nn}} \quad m = \# \text{ ants}$$

$$\eta_{i,j} = \frac{1}{d_{i,j}} \quad C^{nn} = \text{length of nearest neighbor CYCLE}$$

$d_{i,j} = \text{distance from } i \text{ to } j$

like) based on the length

- Tour construction formula
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# Ant System

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$$\eta_{i,j} = \frac{1}{d_{i,j}} \quad C^{nn} = \text{length of nearest neighbor CYCLE}$$

$d_{i,j}$  = distance from  $i$  to  $j$

## The attractiveness of an edge other than pheromone level. (Distance to city)

- What do alpha and beta represent?

$$p_{ij}^k(t) = \begin{cases} \sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta & \\ 0 & \text{otherwise} \end{cases}$$

# Ant System

- Ant cycle: pheromone deposit is determined globally (not very ant like) based on the length

$\alpha$  and  $\beta$  tune the relative importance of pheromone and local information.

• CYCLE

How does this relate to GAs and the mutation rate?

We define the transition probability from town  $i$  to town  $j$  for the  $k$ -th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

- Tour construction formula
- What do alpha and beta represent?

# Ant System

- Ant cycle: pheromone deposit is determined globally (not very ant like) based on the length of the tour
- Initialization:

Probability of ant following edge  $(i,j)$

heuristic information for all  $i,j$ :

$$\eta_{i,j} = \frac{m}{d_{i,j}} \quad \begin{aligned} m &= \text{length of nearest neighbor CYCLE} \\ d_{i,j} &= \text{distance from } i \text{ to } j \end{aligned}$$

We define the transition probability from town  $i$  to town  $j$  for the  $k$ -th ant as

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- Tour construction formula
- What do alpha and beta represent?

- Pheromone update

$$\tau_{ij} \leftarrow \tau_{ij} + \Delta\tau^k.$$

$$\Delta\tau_{i,j}^k = \begin{cases} \frac{1}{C^k} & \text{If } (i,j) \text{ are on the tour of the } k^{\text{th}} \text{ ant} \\ 0 & \text{otherwise} \end{cases}$$

- Pheromone evaporation

$$\tau_{ij} \leftarrow (1 - \rho)\tau_{ij}, \quad \forall (i, j) \in A,$$

where  $\rho \in (0, 1]$  is a parameter.

- AS parameter settings:

- alpha = 1
- beta = 2 to 5
- rho = 0.5
- m = n (number of ants = number of cities)
- Tau<sub>0</sub> initialization = m/C<sup>nn</sup>

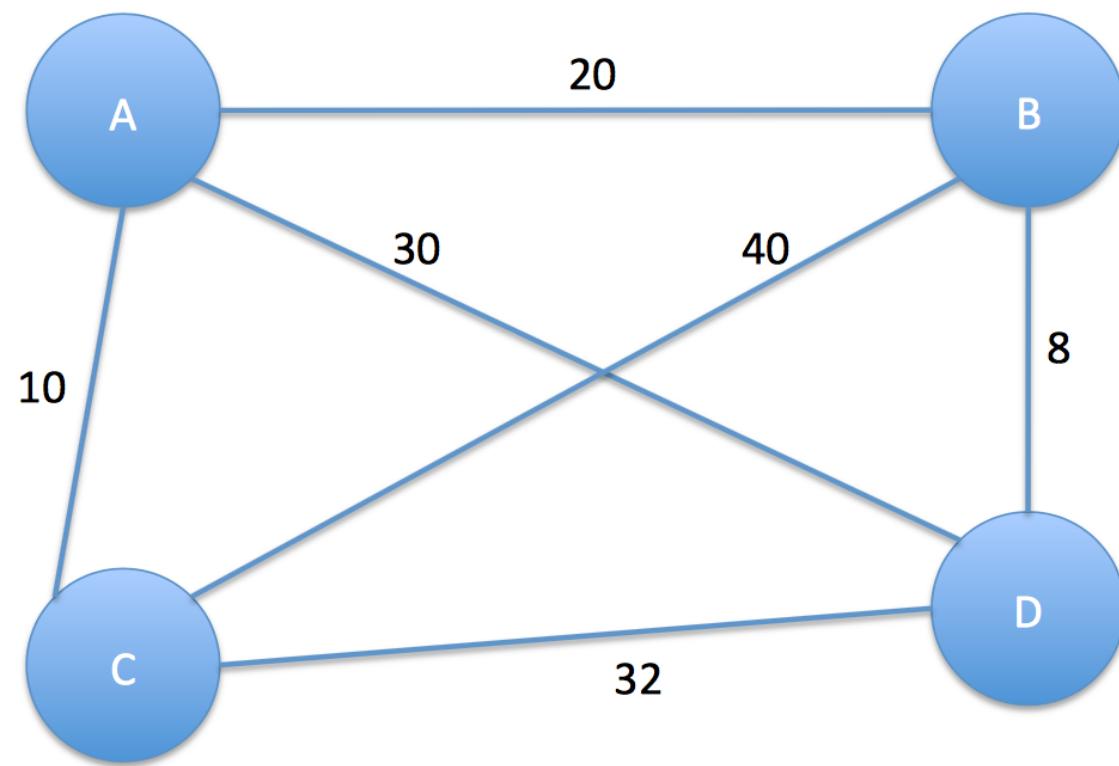
- Ant Cycle: pheromone update depends on tour length,

So it is updated only after a completed tour

- Elistist AS: Reinforce T<sup>bs</sup> (best so far tour)

$$\tau_{i,j} = \tau_{i,j} + \sum_{k=1}^m \Delta\tau_{i,j}^k + e\Delta\tau_{i,j}^{bs}$$

$$\Delta\tau_{i,j}^{bs} = \frac{1}{C^{bs}}$$



## Initialize

$$\tau_{i,j} = \frac{m}{C^{nn}}$$

$C^{nn}$  = length of nearest neighbor CYCLE

$d_{i,j}$  = distance from i to j

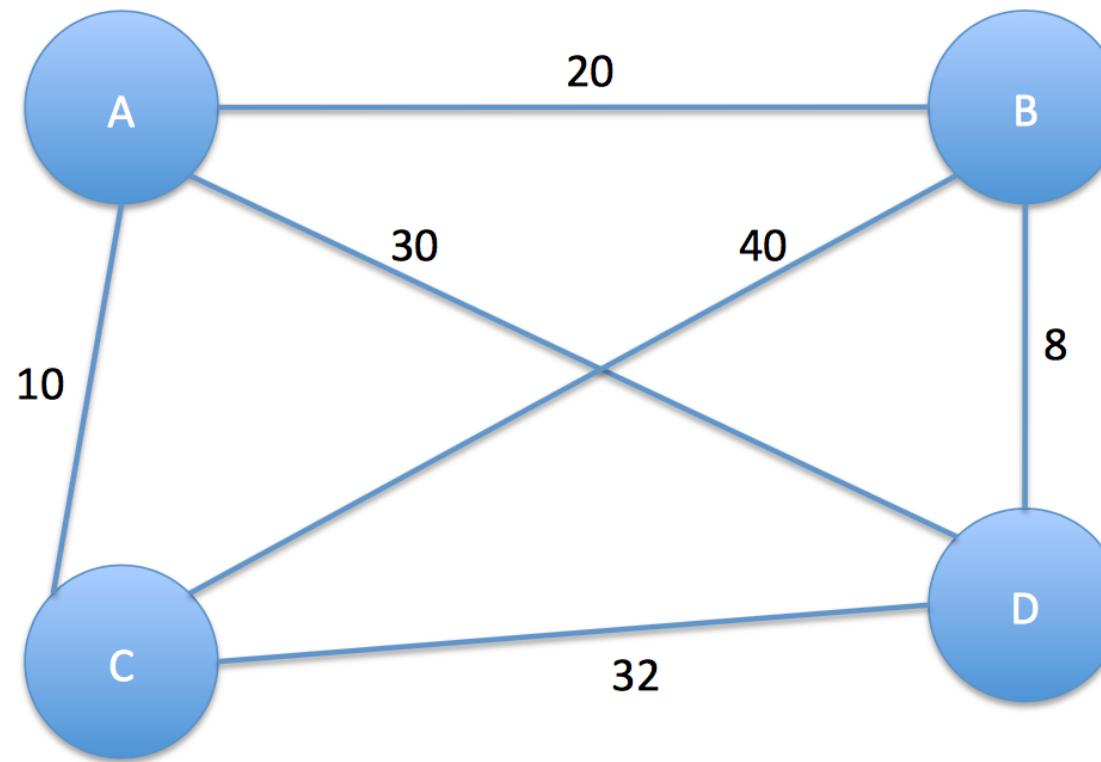
$$\eta_{i,j} = \frac{1}{d_{i,j}}$$

Start at A

$$C^{nn} = 10 + 32 + 8 + 20 = 70$$

A, C, D, B

$m$  = # cities = # ants = 4



## Initialize

$$\tau_{i,j} = \frac{m}{C^{nn}}$$

$C^{nn}$  = length of nearest neighbor CYCLE

$d_{i,j}$  = distance from i to j

$$\eta_{i,j} = \frac{1}{d_{i,j}}$$

Start at A

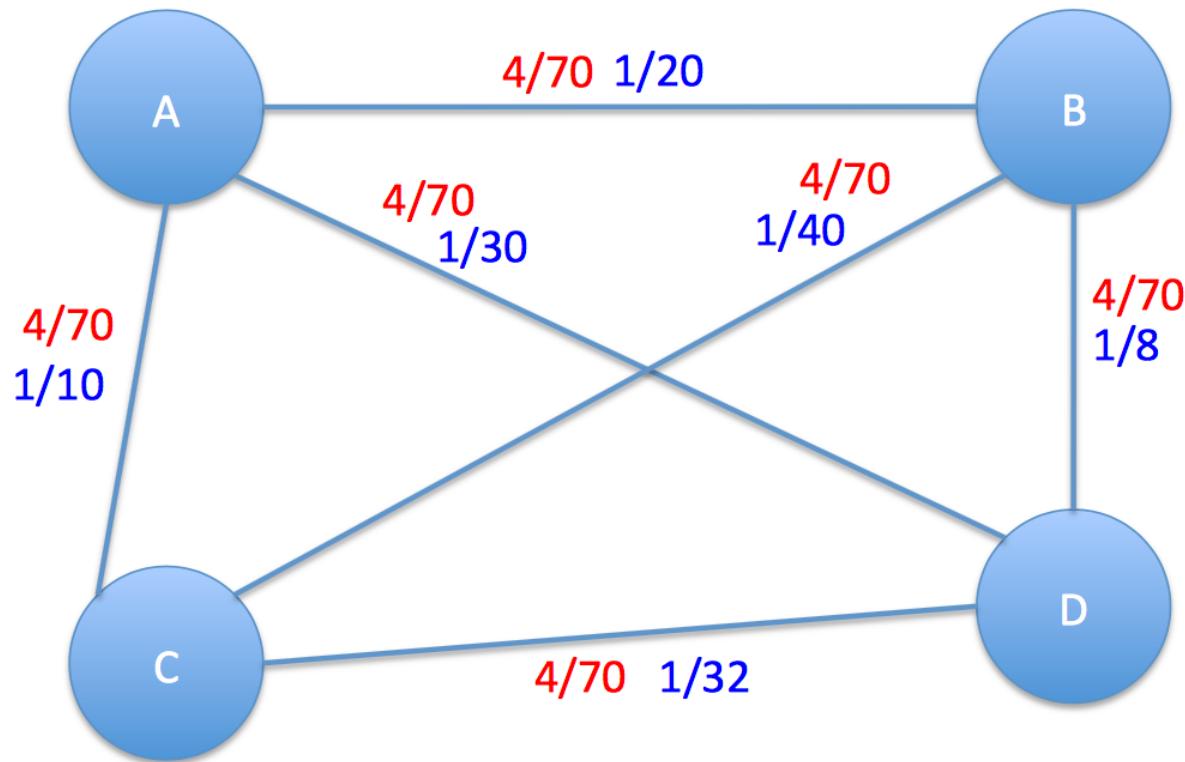
$$C^{nn} = 10 + 32 + 8 + 20 = 70$$

A, C, D, B

$m$  = # cities = # ants = 4

All initial  $\tau = 4/70$

$\tau, \eta$



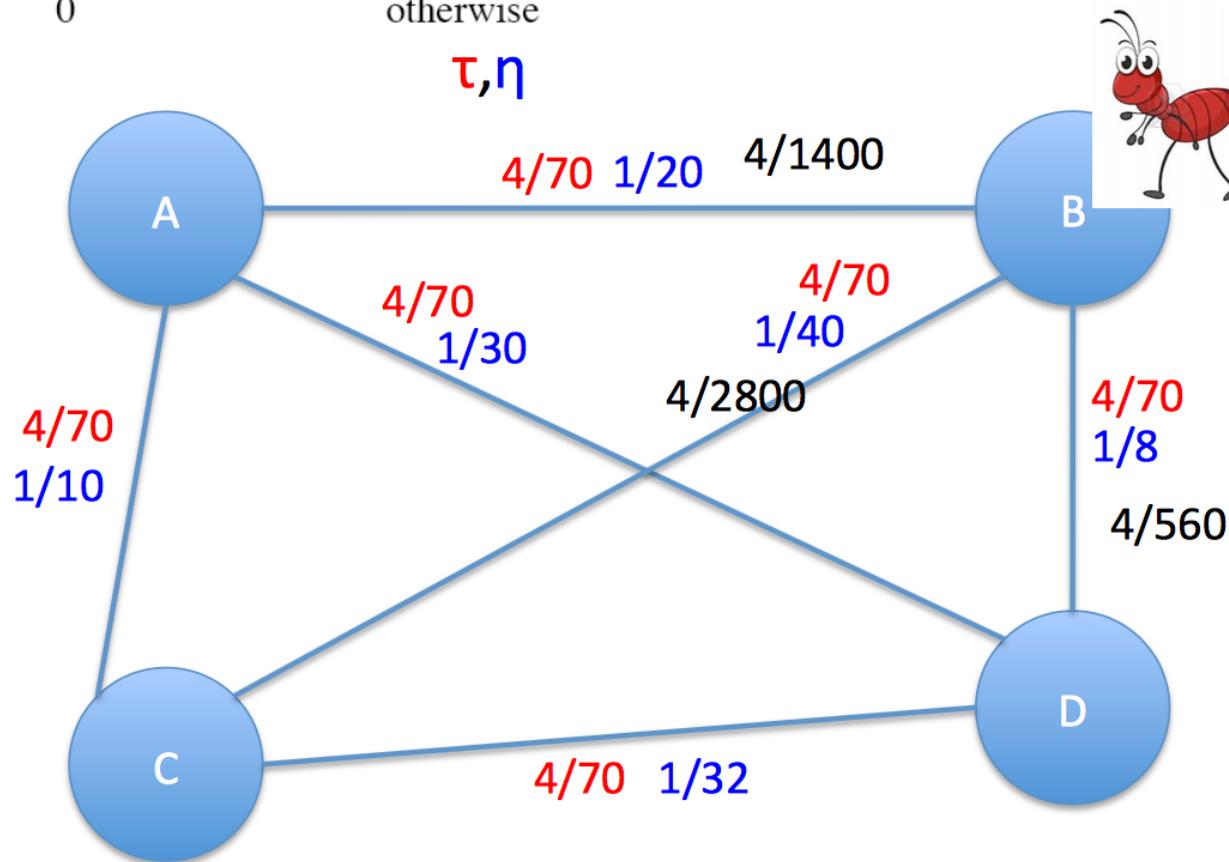
We define the transition probability from town i to town j for the k-th ant as

**TRAVERSE**

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

$\alpha = 1$   
 $\beta = 1 \text{ (usually 2 - 5)}$

denominator =  $(8+4+20)/2800$



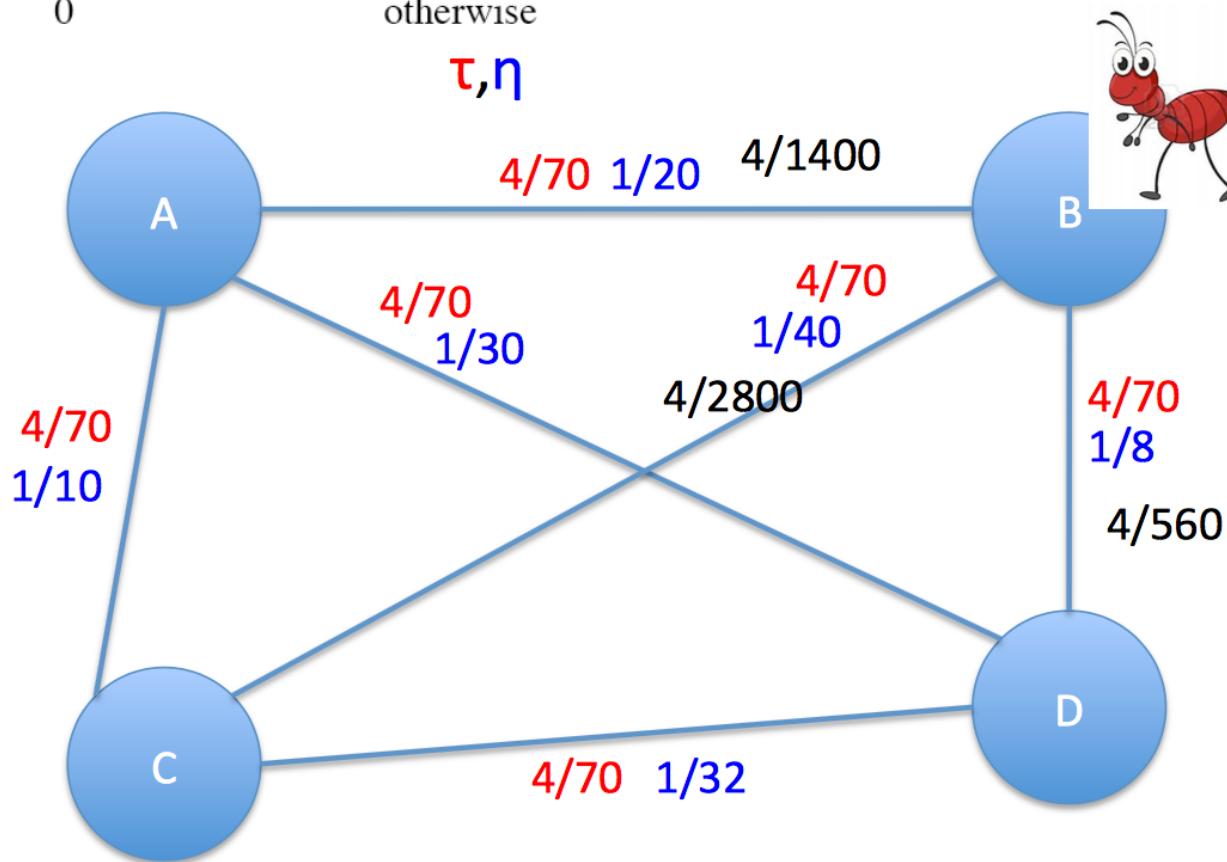
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$\tau, \eta$   
denominator =  $(8+4+20)/2800$

$\alpha = 1$   
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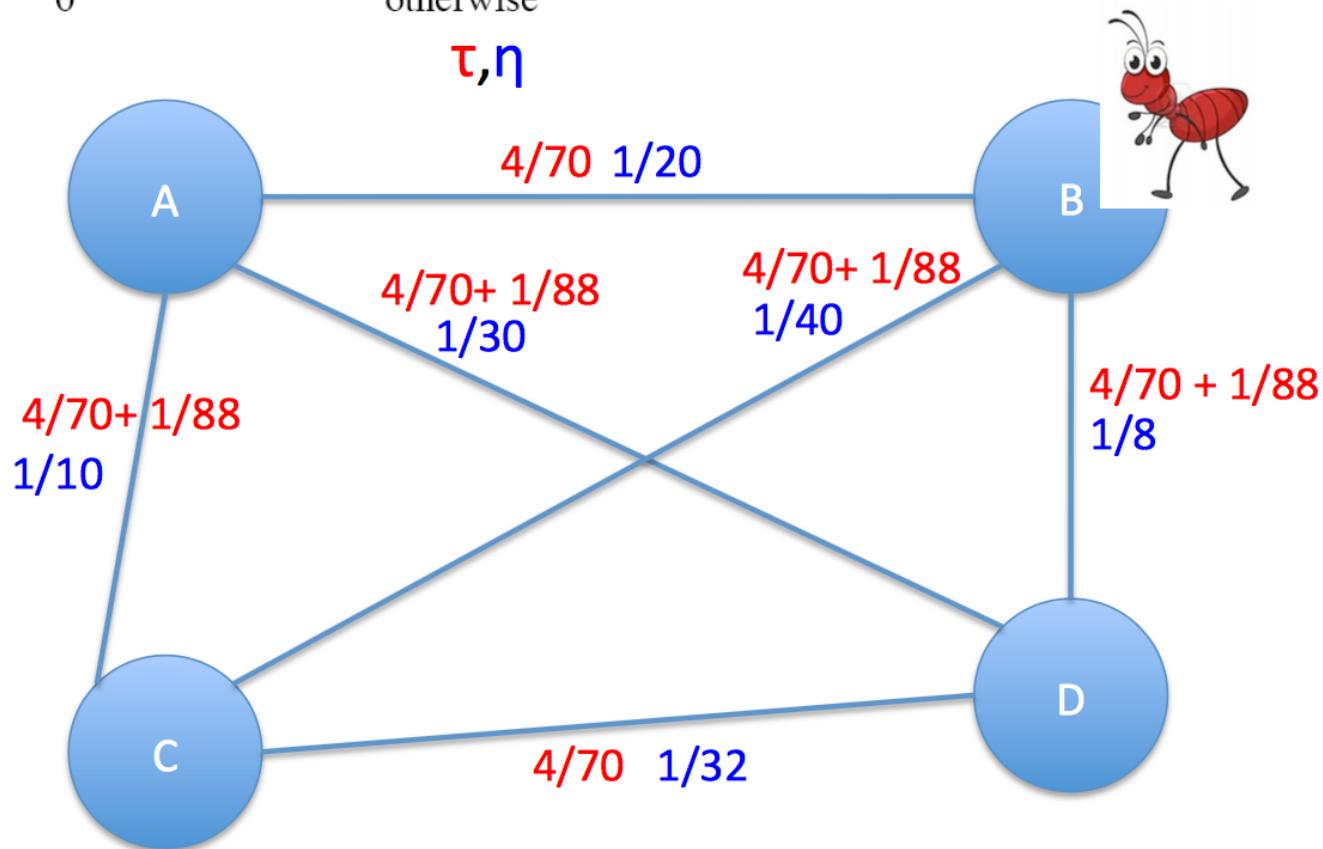
Usually : B, D, A, C, B: Cycle =  $8+30+10+40 = 88$   
 Rarely: B,D,C,A, B: Cycle =  $8+32+10+20 = 70$

We define the transition probability from town  $i$  to town  $j$  for the  $k$ -th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$

UPDATE Pheromone

$$\Delta\tau_{i,j}^k = \frac{1}{C^k}$$

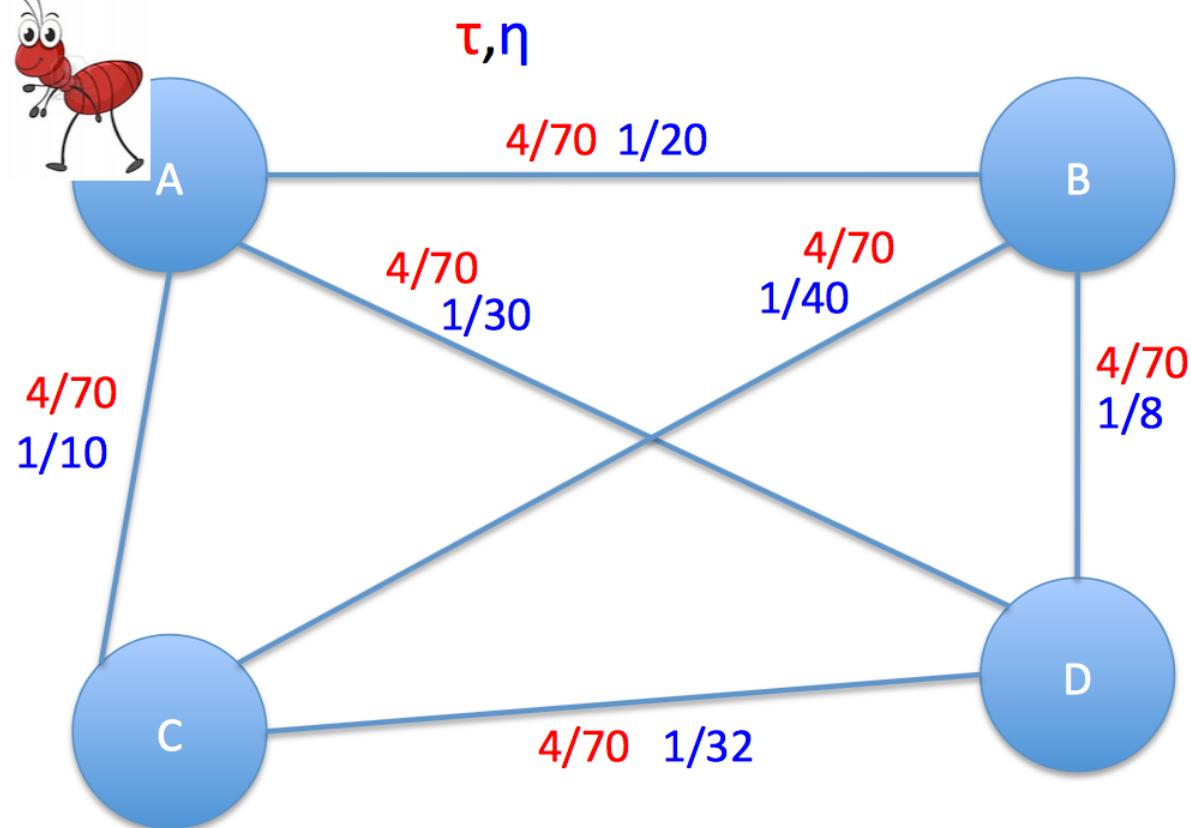


Usually : B, D, A, C, B: Cycle = 8+30+10 +40 = 88

Rarely: B,D,C,A, B: Cycle = 8+32+10 + 20 = 70

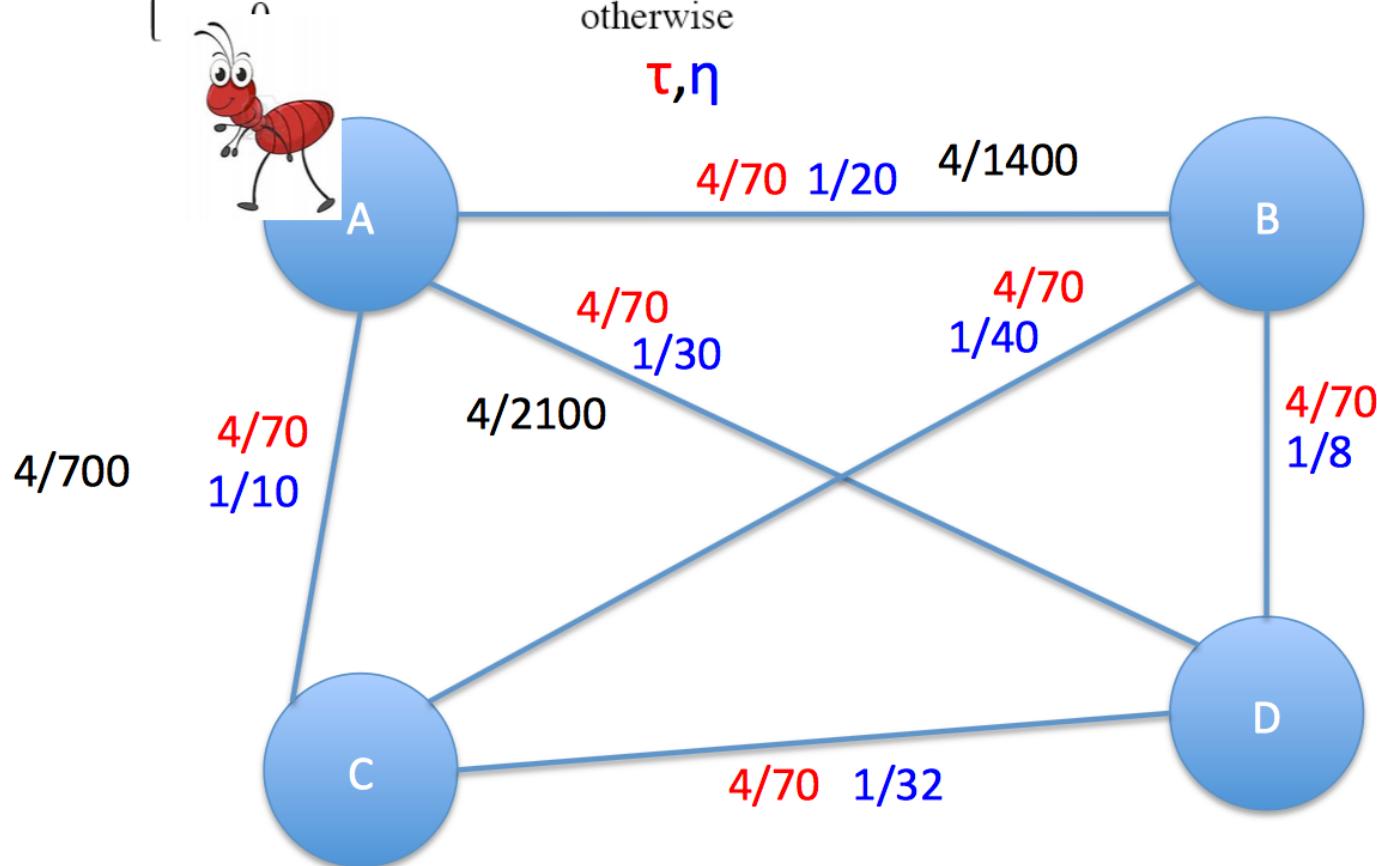
We define the transition probability from town  $i$  to town  $j$  for the  $k$ -th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases} \quad \begin{matrix} \alpha = 1 \\ \beta = 1 \end{matrix}$$



We define the transition probability from town  $i$  to town  $j$  for the  $k$ -th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases} \quad \begin{aligned} \alpha &= 1 \\ \beta &= 1 \text{ (usually 2 - 5)} \end{aligned}$$

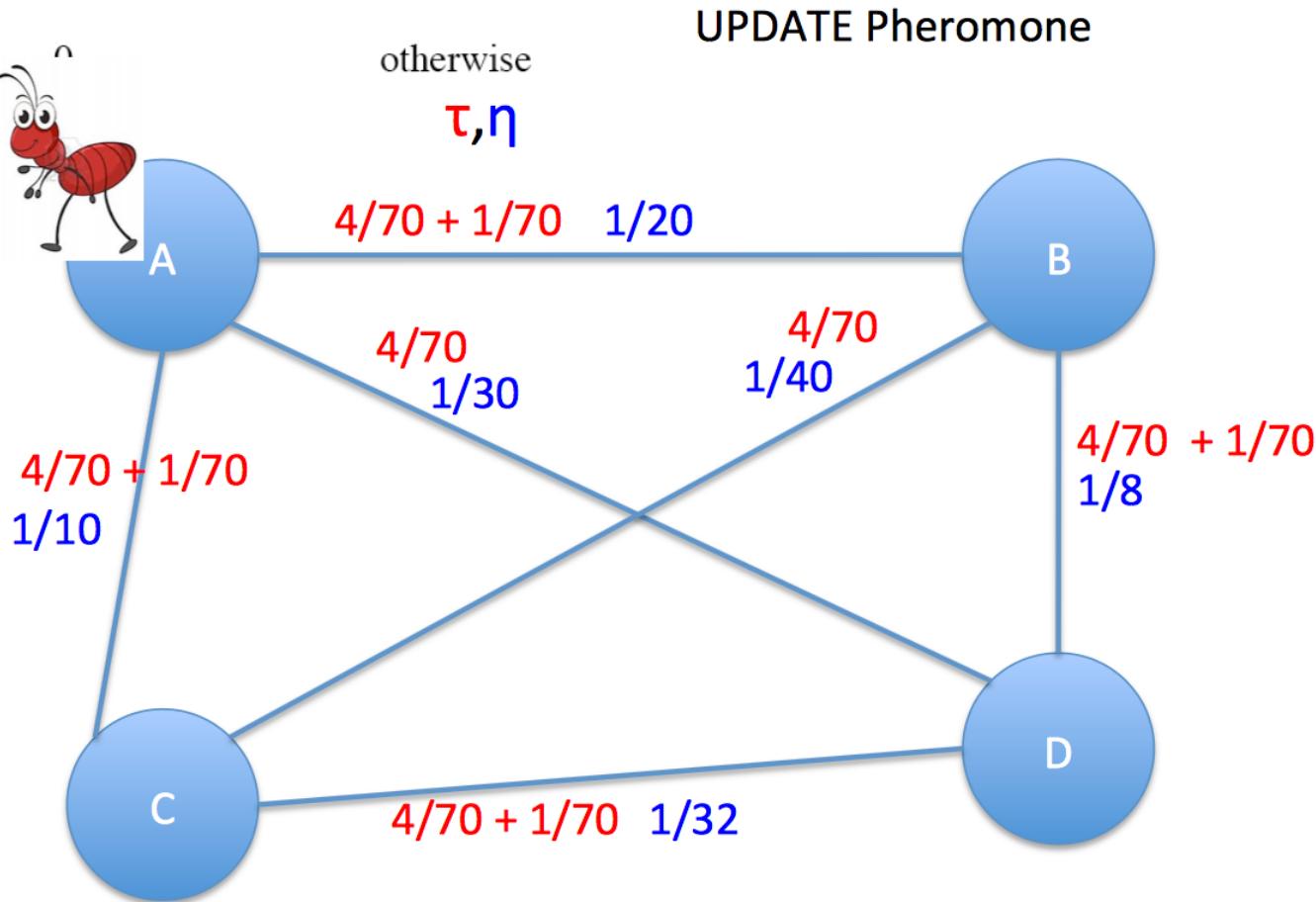


Usually : A, C, D, B, A Cycle =  $10+32+8+20=70$

Very Rarely: A, D, C, B, A Cycle =  $30+32+40+20=122$

We define the transition probability from town i to town j for the k-th ant as

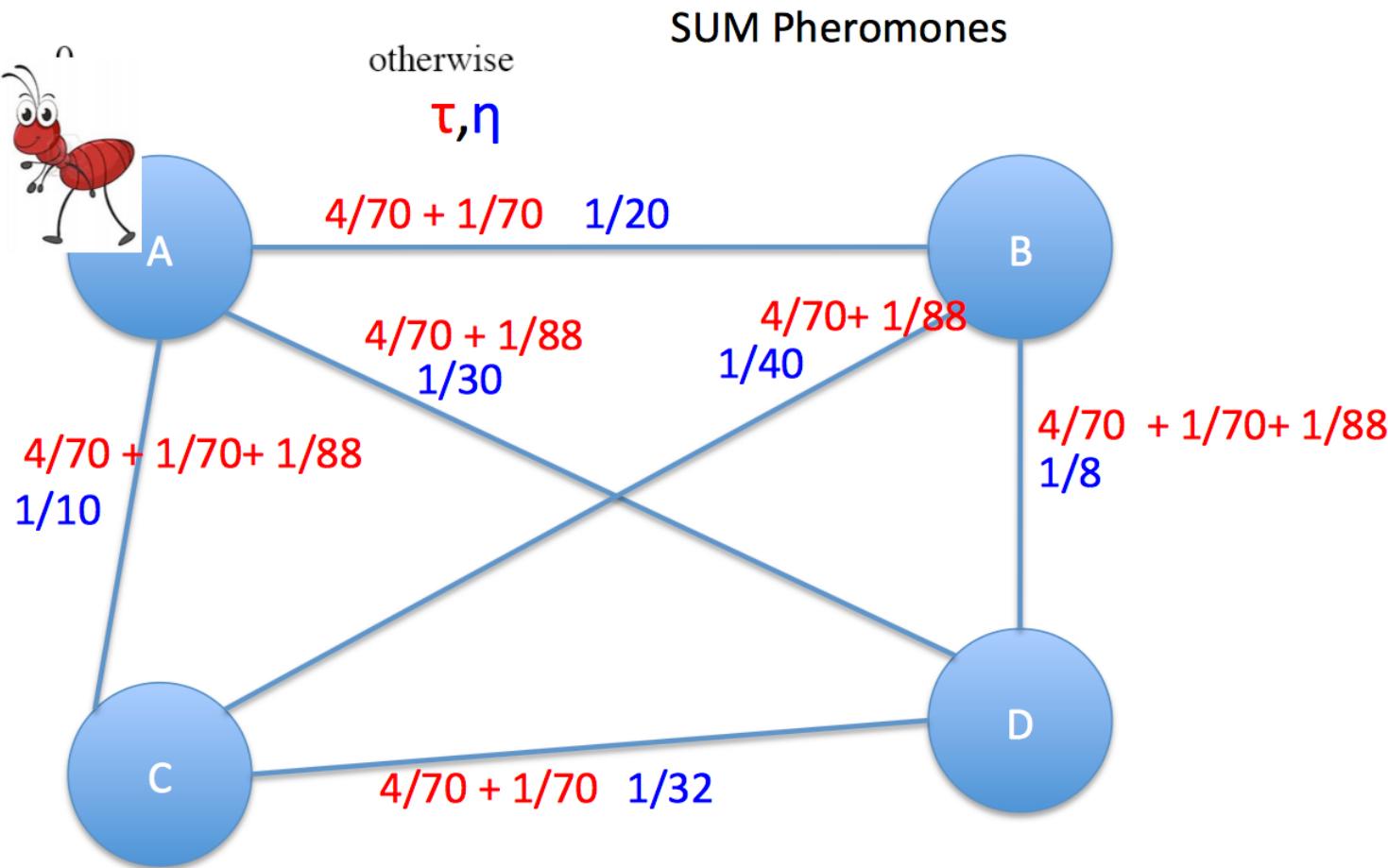
$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$



Usually : A, C, D, B, A Cycle =  $10+32+8+20=70$   
 Rarely: A, D, B, C, A Cycle =  $30+8+40+10=88$

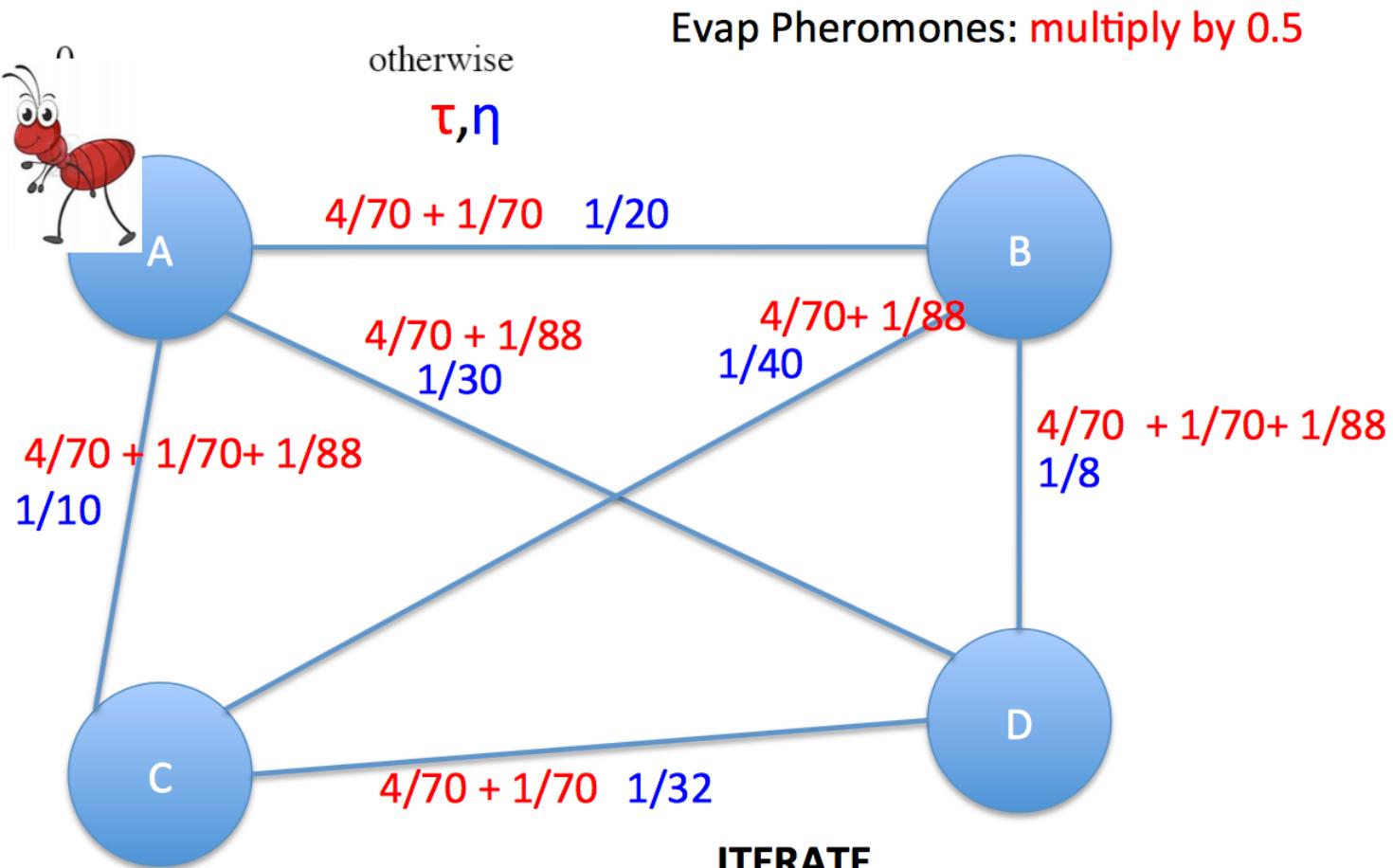
We define the transition probability from town  $i$  to town  $j$  for the  $k$ -th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$



We define the transition probability from town i to town j for the k-th ant as

$$p_{ij}^k(t) = \begin{cases} \frac{[\tau_{ij}(t)]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{k \in \text{allowed}_k} [\tau_{ik}(t)]^\alpha \cdot [\eta_{ik}]^\beta} & \text{if } j \in \text{allowed}_k \\ 0 & \text{otherwise} \end{cases}$$



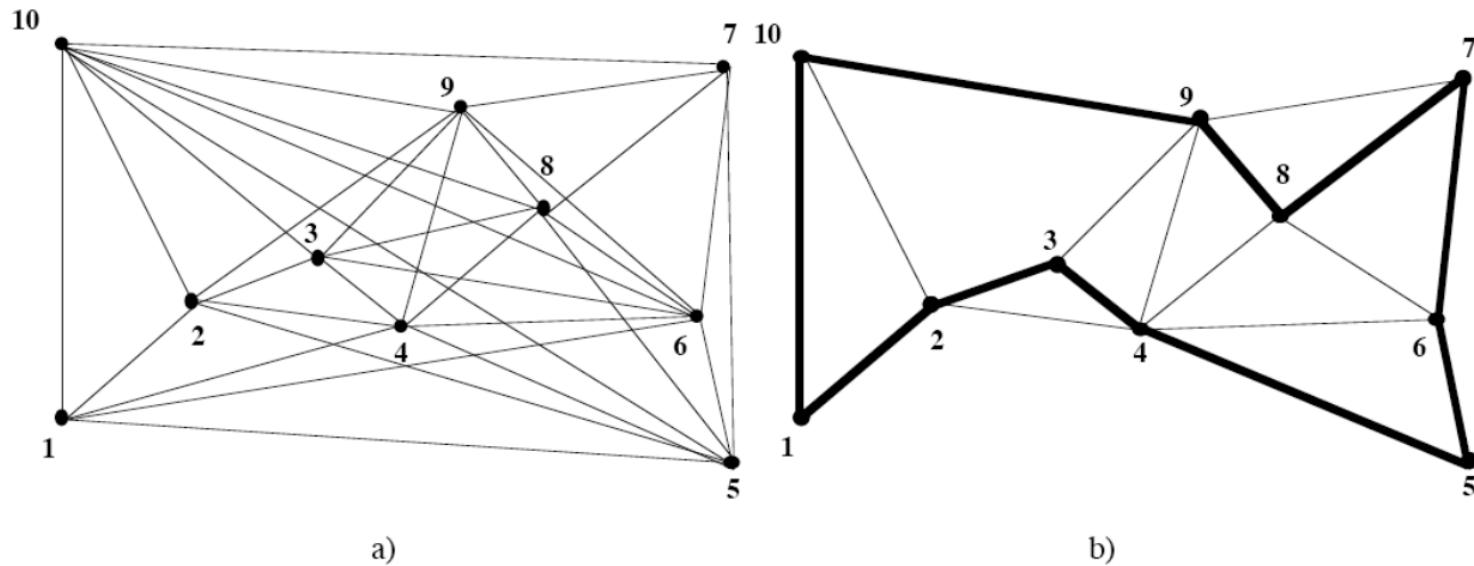
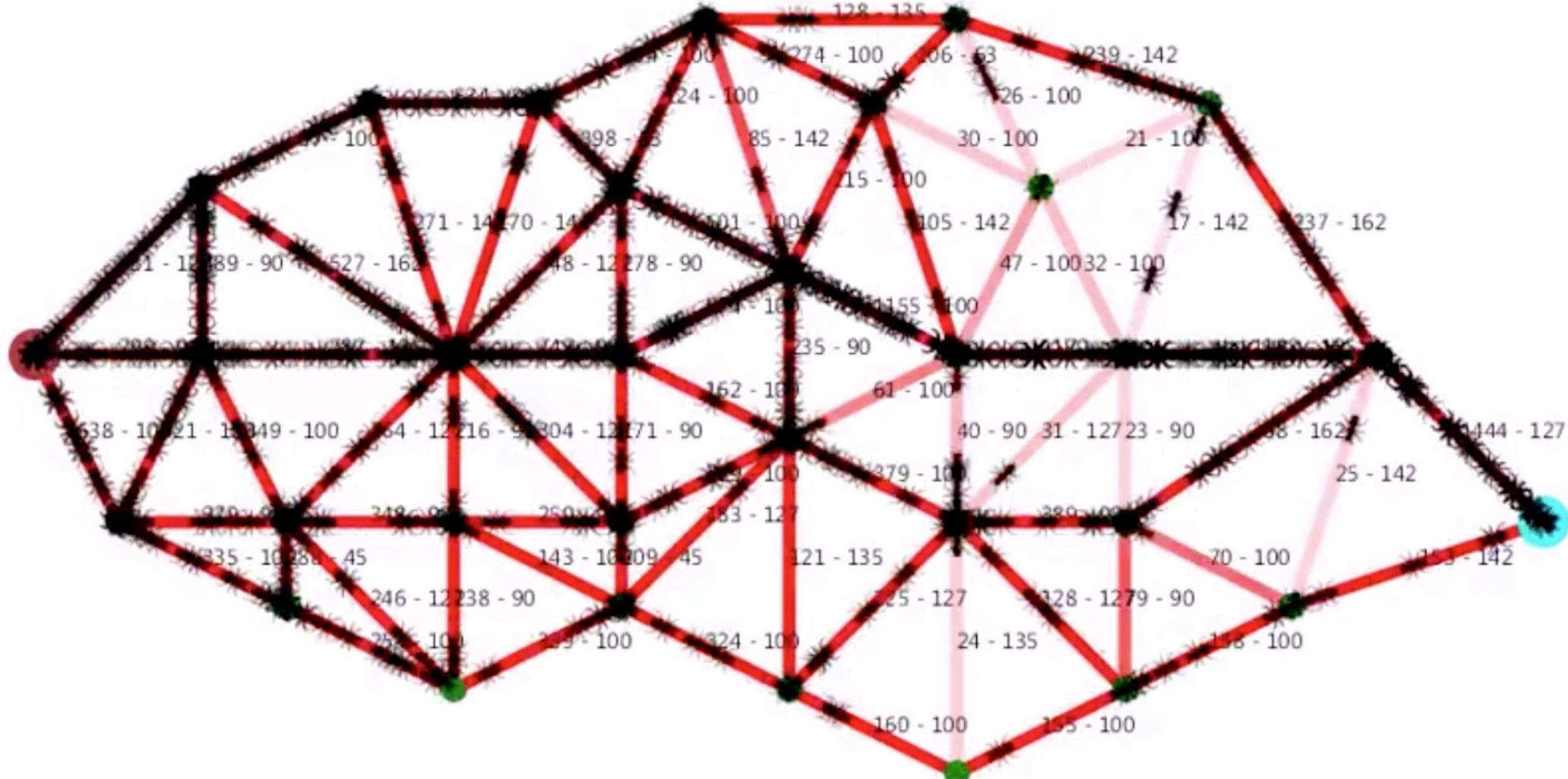
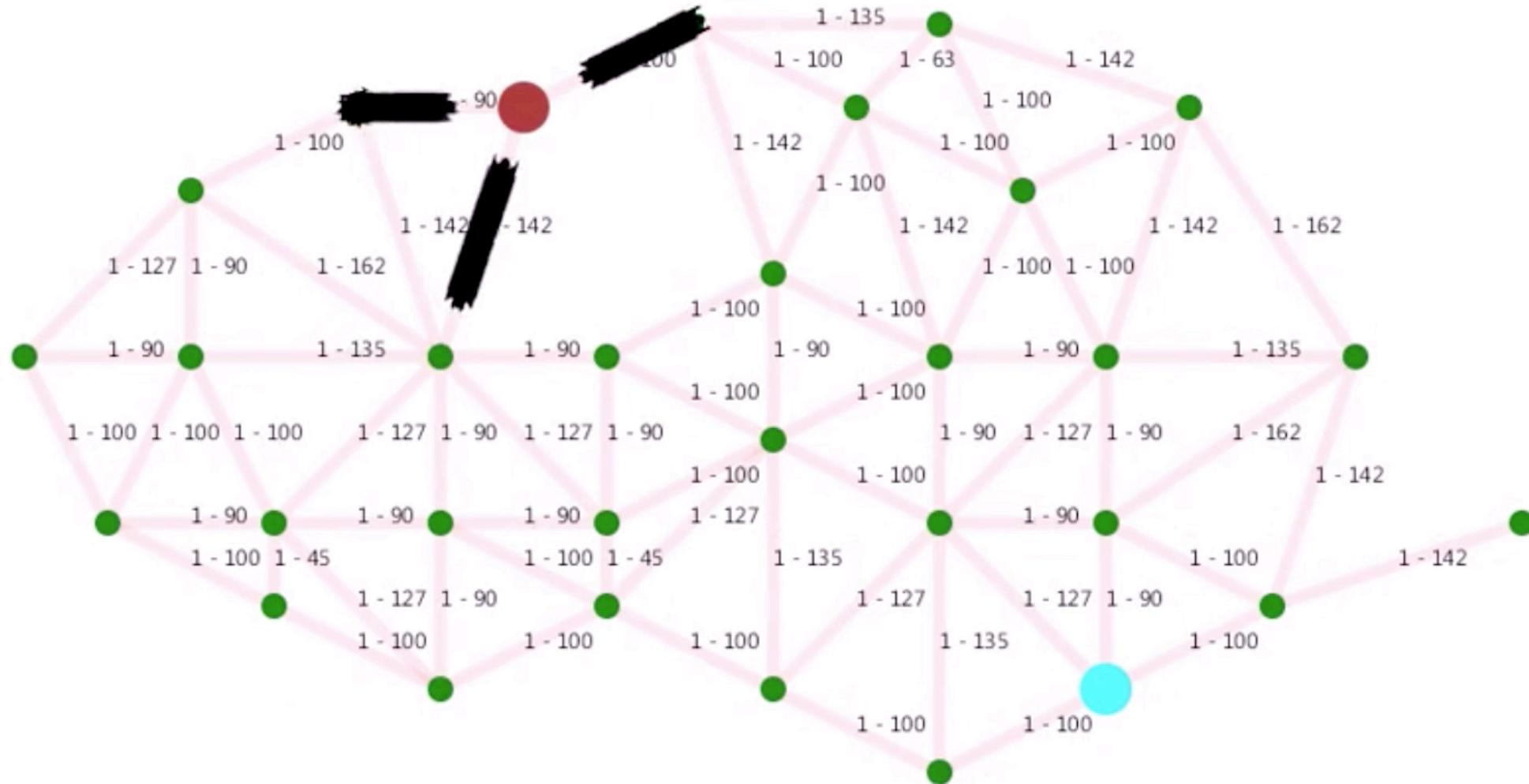


Fig. 6. Evolution of trail distribution for the CCA0 problem.

a) Trail distribution at the beginning of search.

b) Trail distribution after 100 cycles.

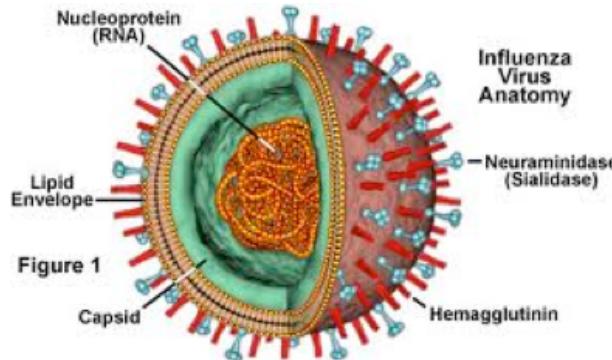




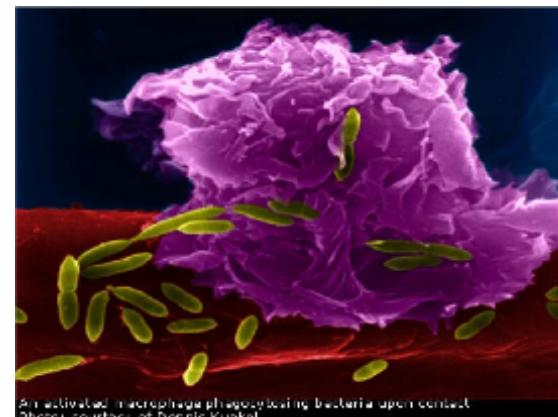
# The Immune System

# Introduction

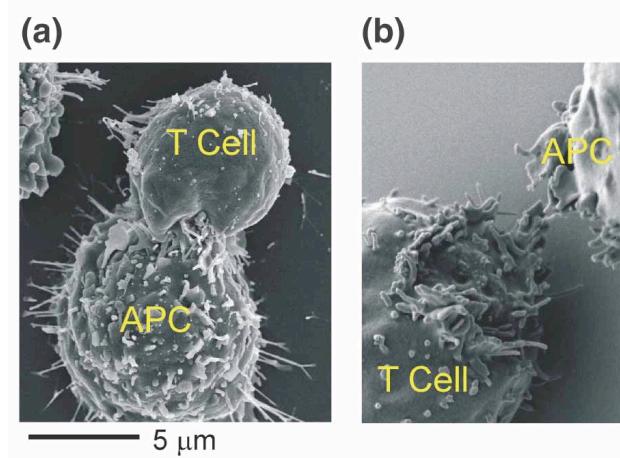
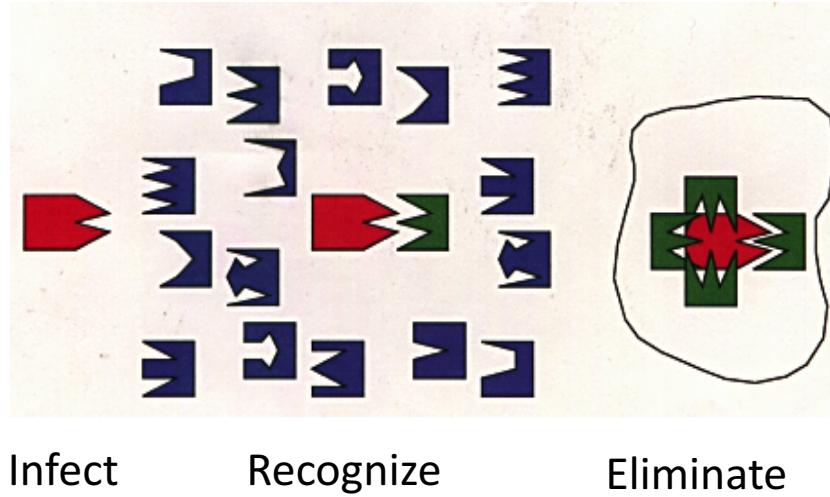
- Immune systems protect the body against foreign pathogens
  - Viruses
  - Bacteria
  - Parasites



Downloaded from [micro.magnet.fsu.edu](http://micro.magnet.fsu.edu) (2010)



# A Brief Introduction to the Immune System



<http://wires.wiley.com/WileyCDA/WiresArticle/wisId-WNAN1195.html>

- Cells and molecules
- Recognition implemented as binding
- Specific recognition to avoid autoimmunity

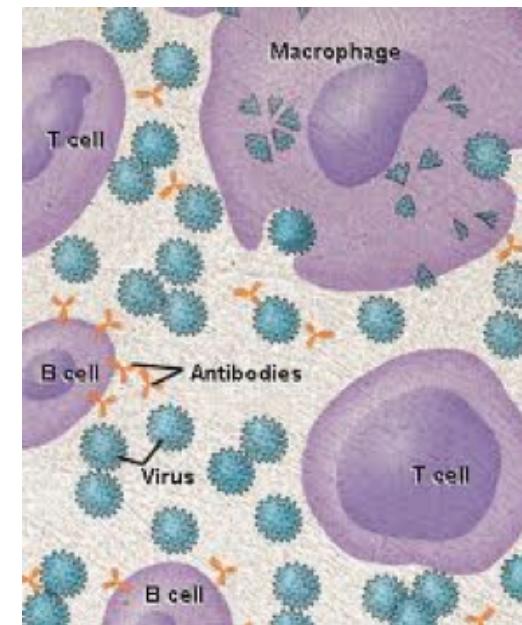
# An Information Processing Perspective

- Immune systems **learn** to recognize relevant patterns:
  - Primary response to new foreign antigen
  - Evolved biases towards common pathogens
  - Learned distinction between self and dangerous other
- Immune systems **remember** patterns seen previously
  - Secondary response
  - Cross-reactive memory
- **Combinatorics** to construct pattern detectors
  - $10^{11} - 10^{16}$  different foreign patterns from 30,000 genes
- Massive **parallelism** and **distributed** control

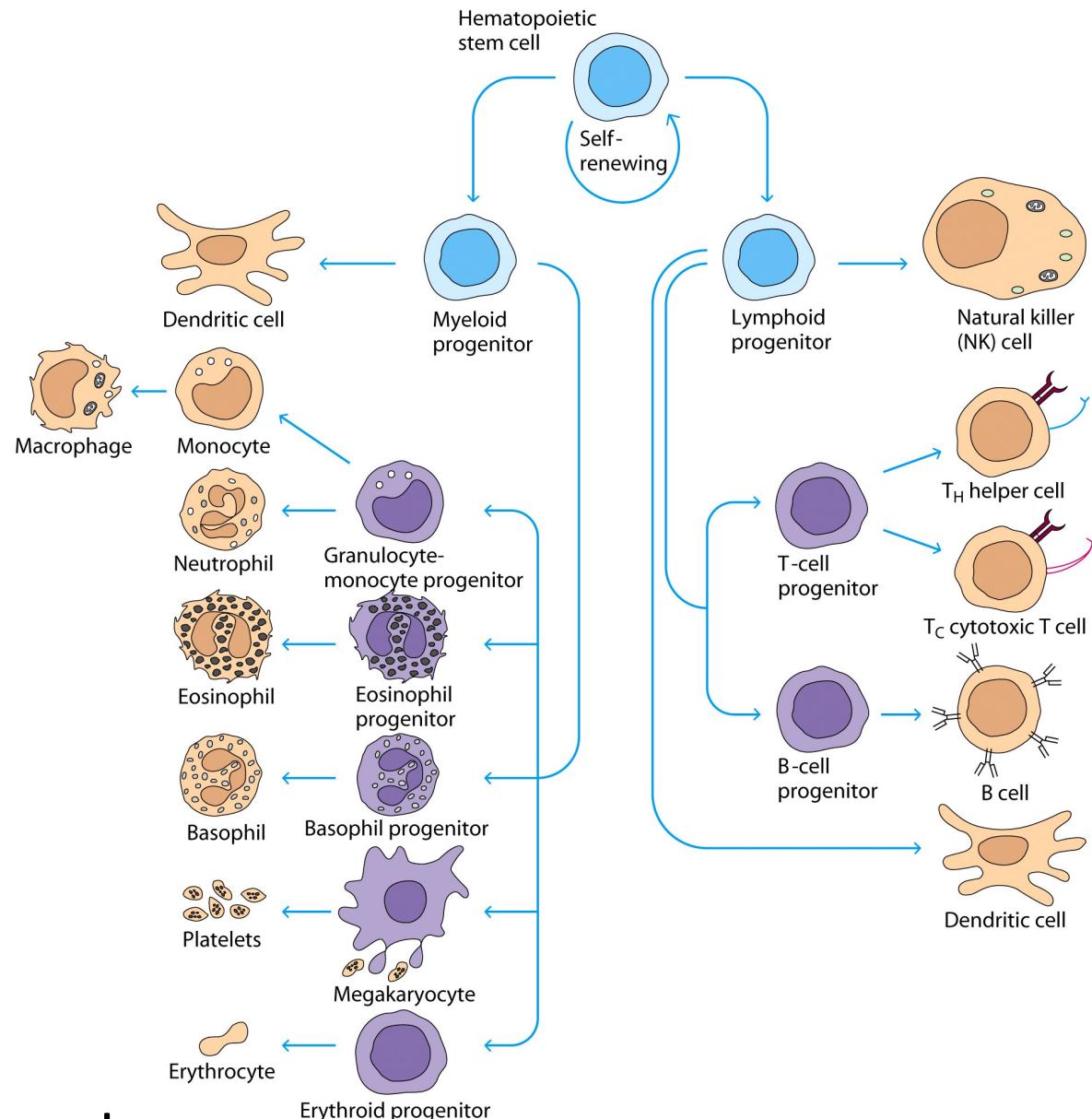
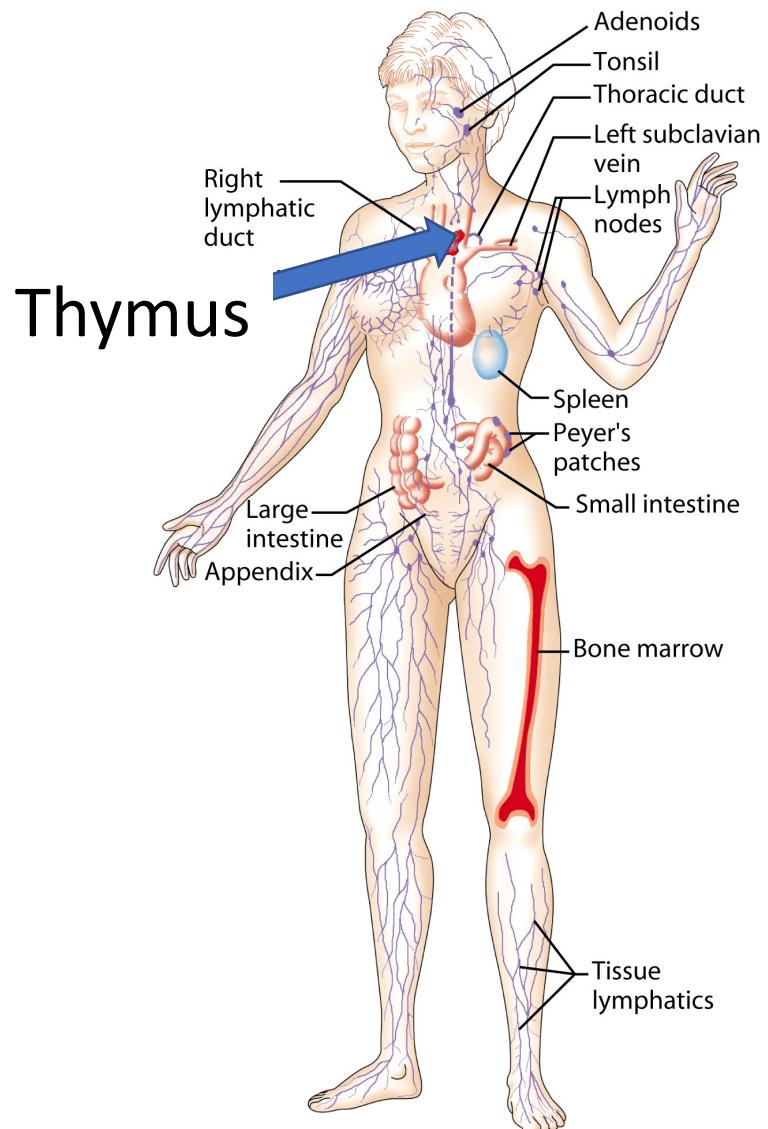
- Innate response
  - Generic
  - Inflammation
- Adaptive response
  - Specific
  - Self-tolerant
  - Learning, memory



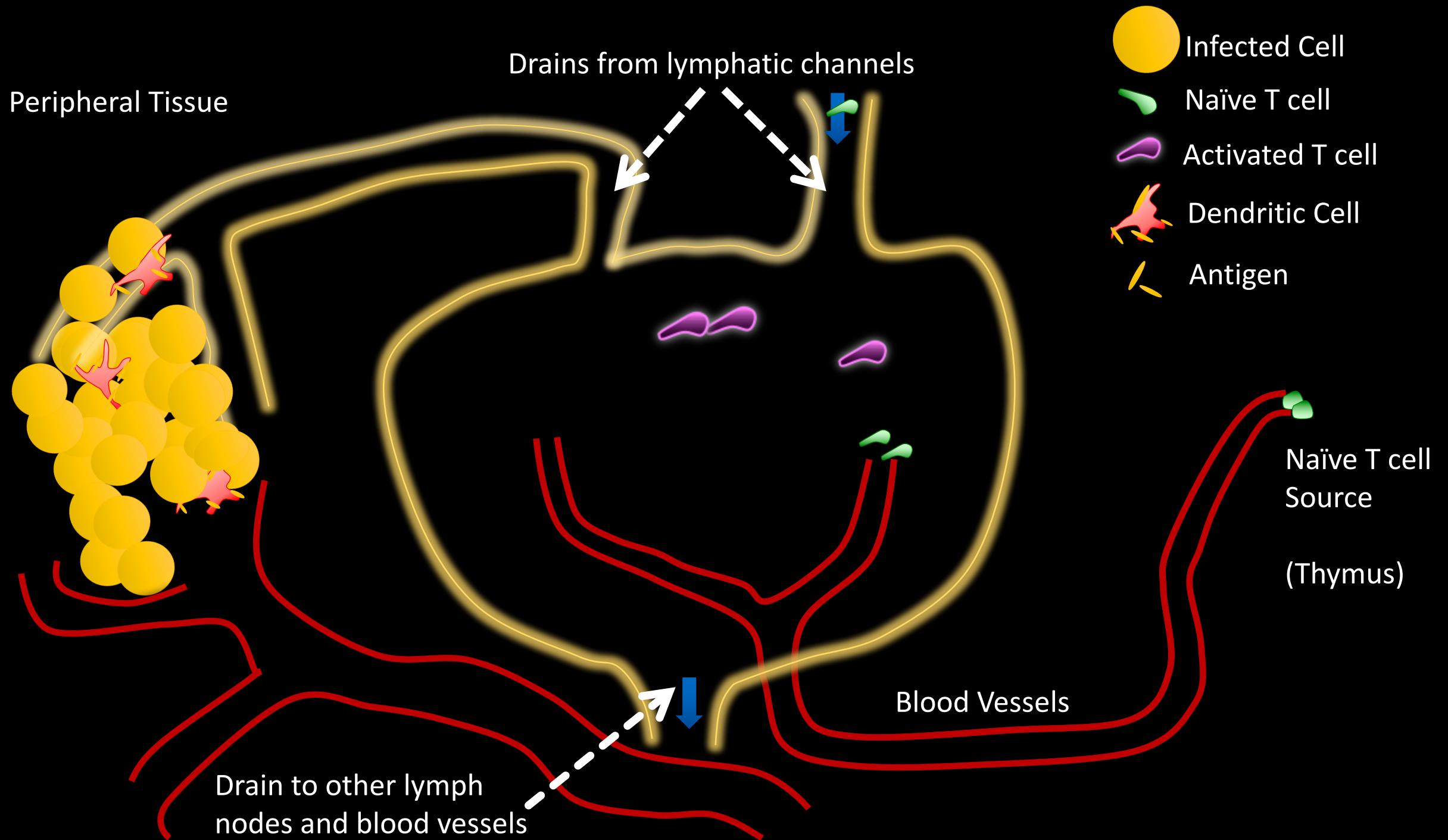
Figure 2-8a  
Kuby IMMUNOLOGY, Sixth Edition  
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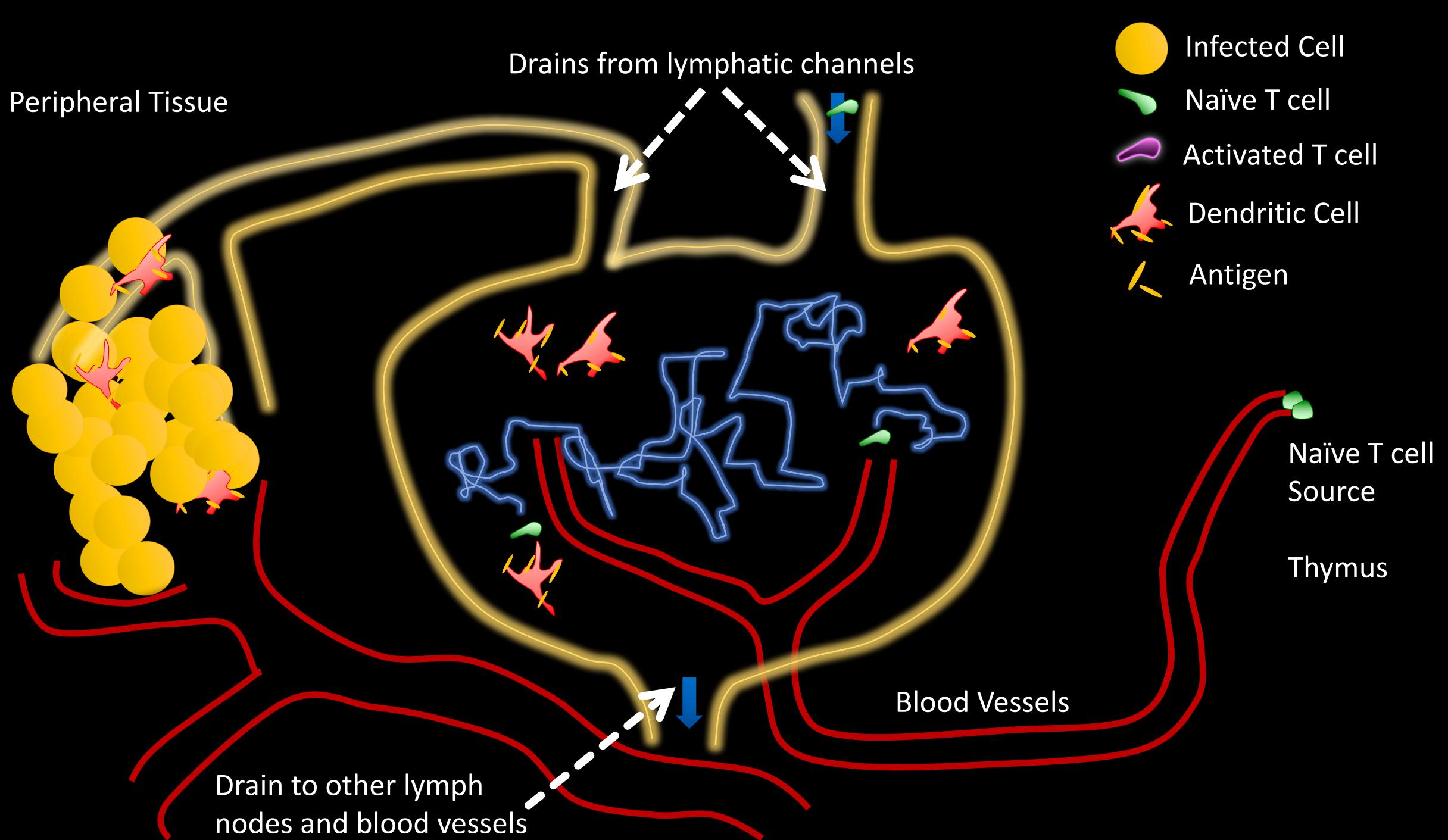


# How is it implemented?



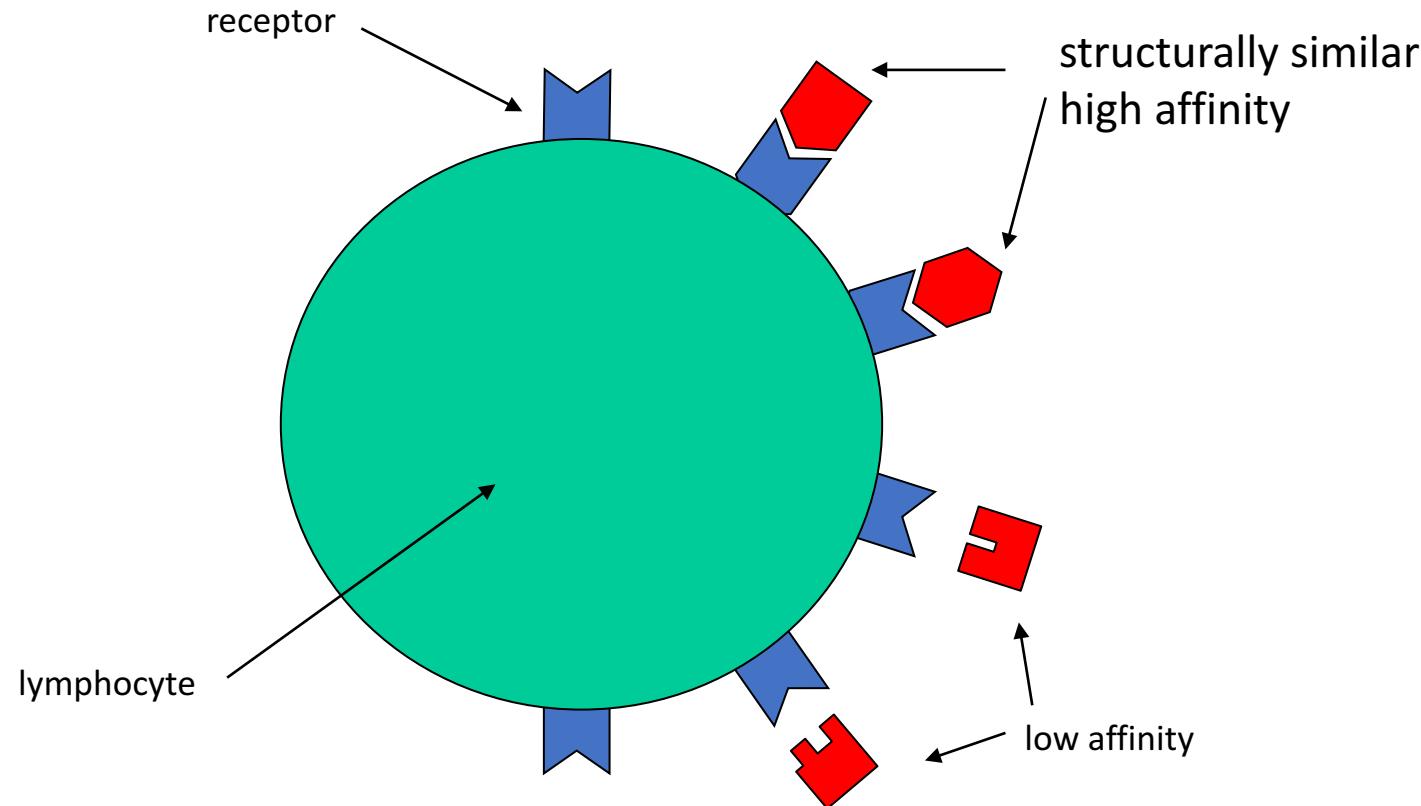
Lymph Nodes distributed throughout



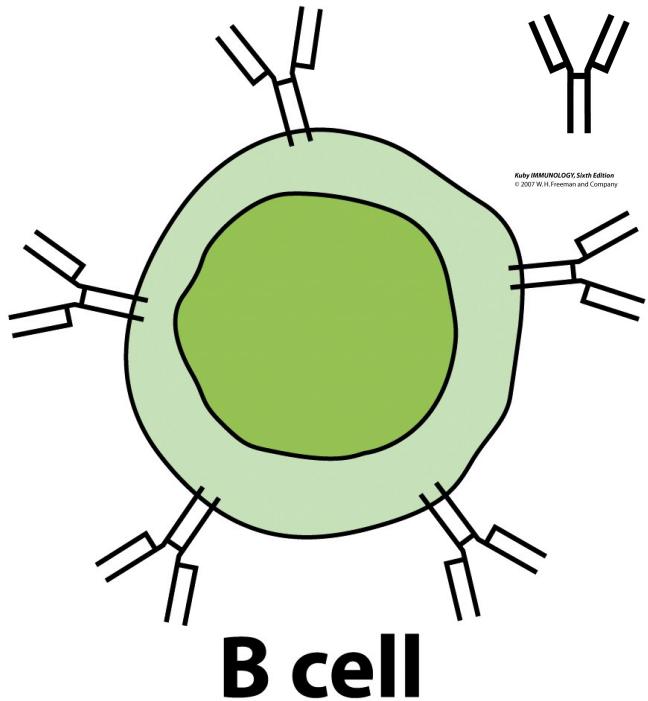


# Detection

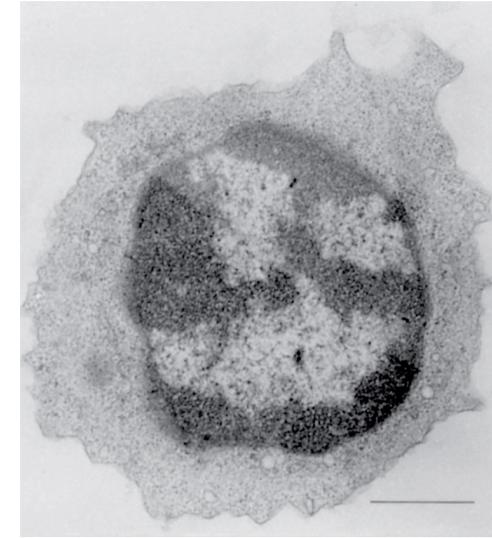
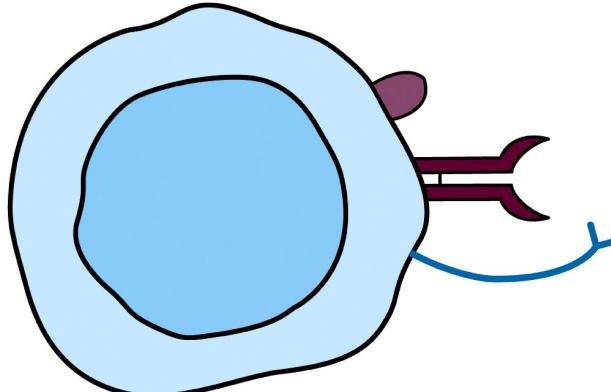
## *Lymphocyte Binding and Cross-reactivity*



# *B-cells and T-cells*

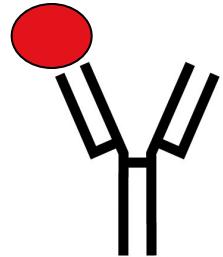


**Antibody**



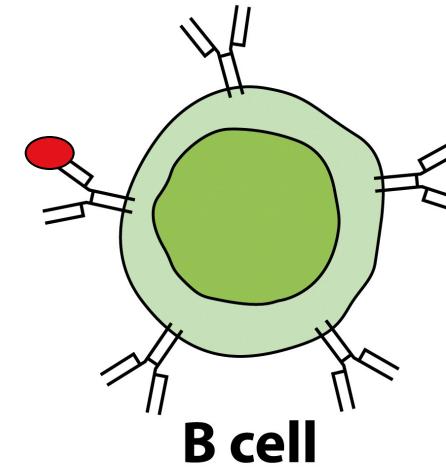
**Figure 2-6b part 1**  
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Antigen



# Antibody

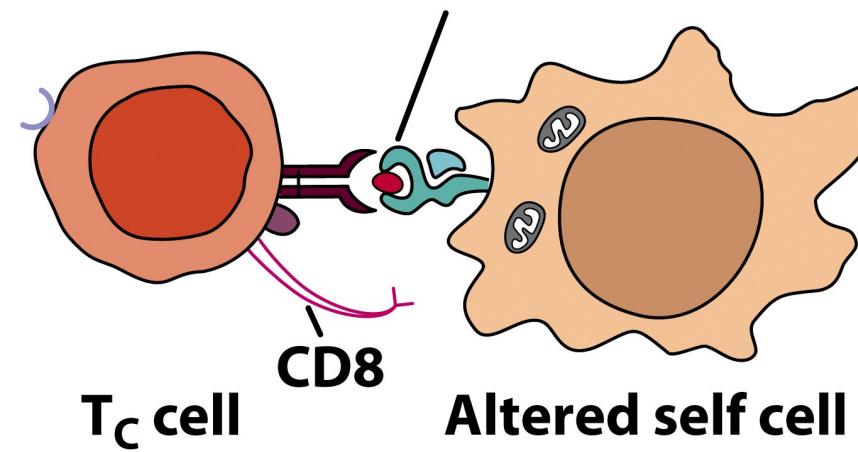
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**B cell**

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**Class I MHC**

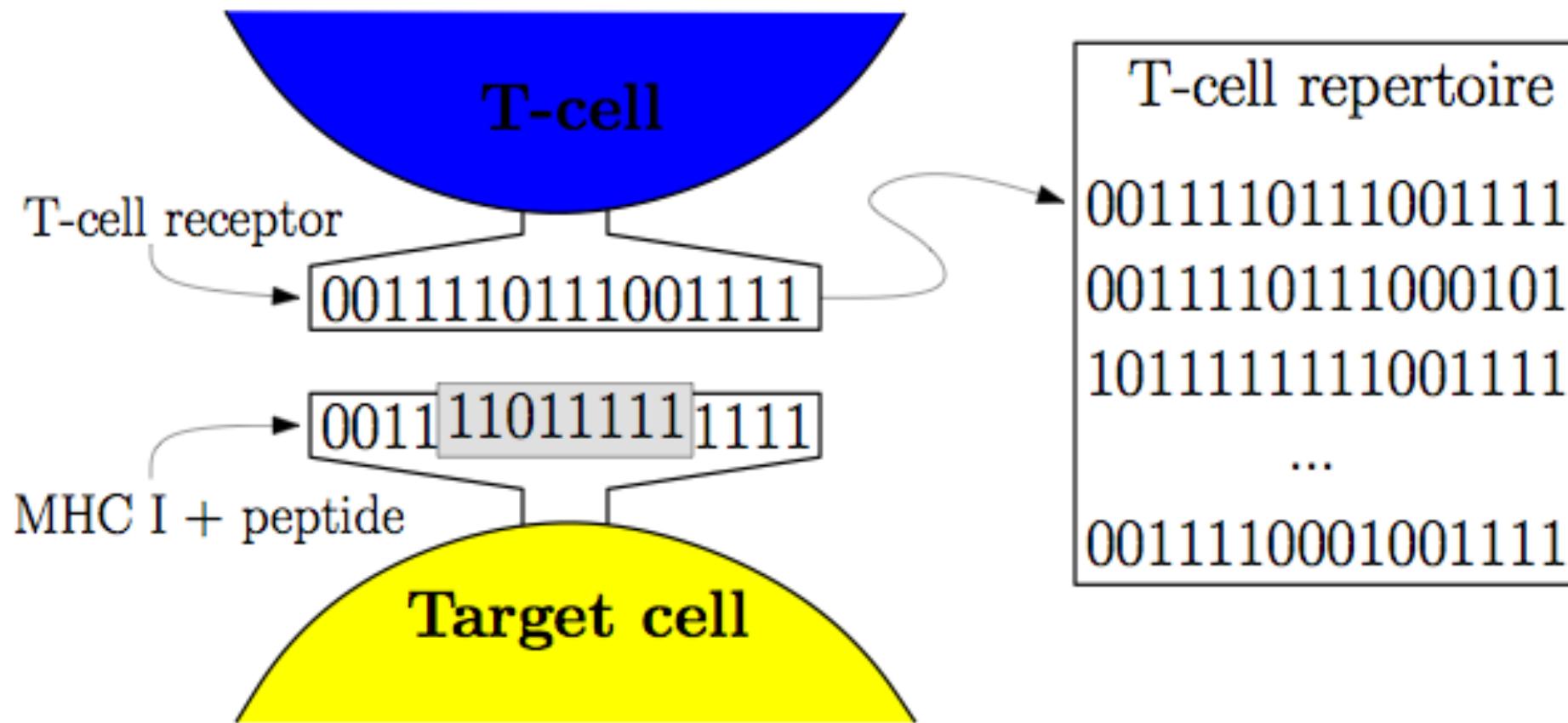


**T<sub>C</sub> cell**

**Altered self cell**

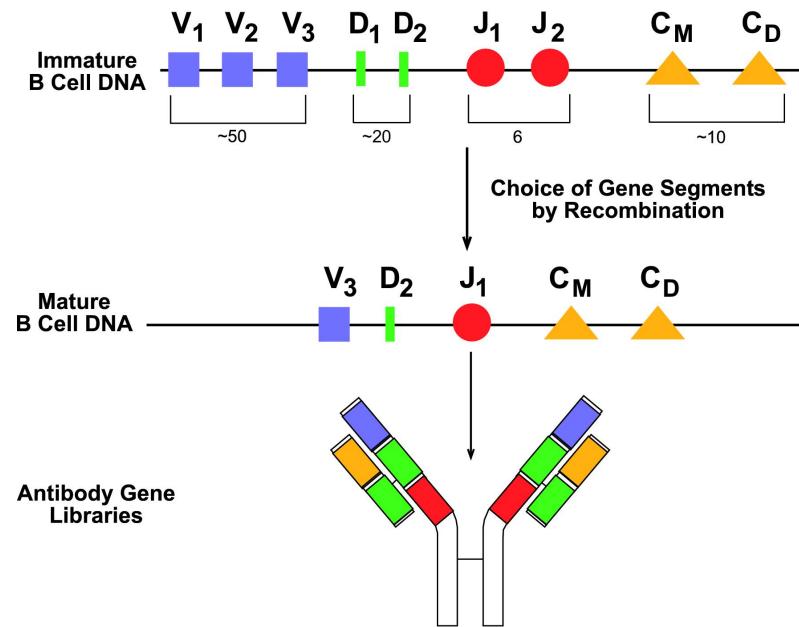
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# Fundamental Modeling Abstraction

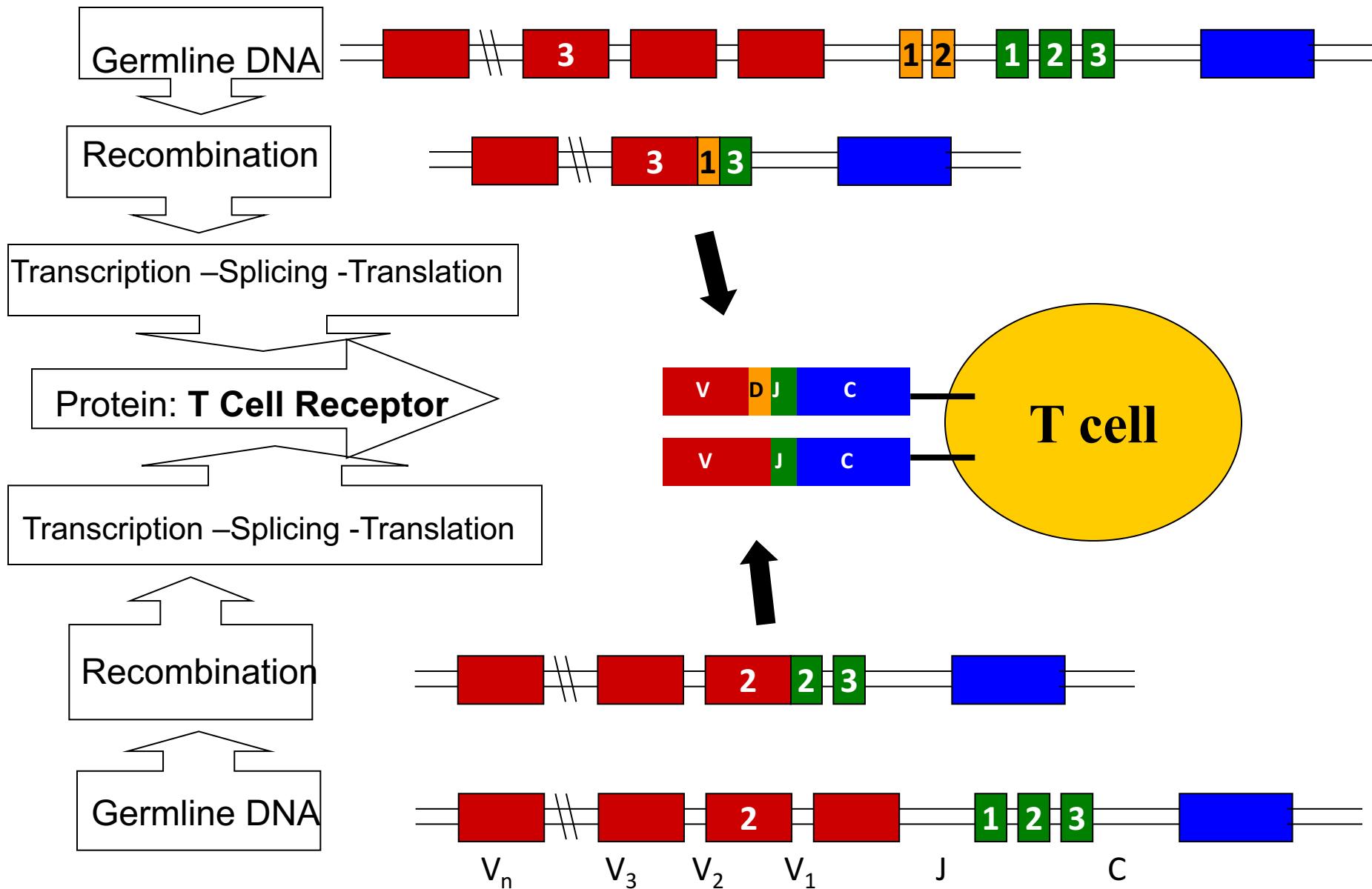


# How does the I.S. make so many different receptor patterns?

- Recombination of gene fragments
- Junctional diversity
- Diploid genetics
- Somatic mutation



# Generation of Diversity in Antigen Receptors



Element	Immunoglobulin		$\alpha:\beta$ receptors	
	H	$\kappa+\lambda$	$\beta$	$\alpha$
Variable segments (V)	65	70	52	~70
Diversity segments (D)	27	0	2	0
D segments read in 3 frames	rarely	–	often	–
Joining segments (J)	6	5( $\kappa$ ) 4( $\lambda$ )	13	61
Joints with N- and P- nucleotides	2	50% of joints	2	1
Number of V gene pairs	$3.4 \times 10^6$		$5.8 \times 10^6$	
Junctional diversity	$\sim 3 \times 10^7$		$\sim 2 \times 10^{11}$	
Total diversity	$\sim 10^{14}$		$\sim 10^{18}$	

Fig 4.13 © 2001 Garland Science

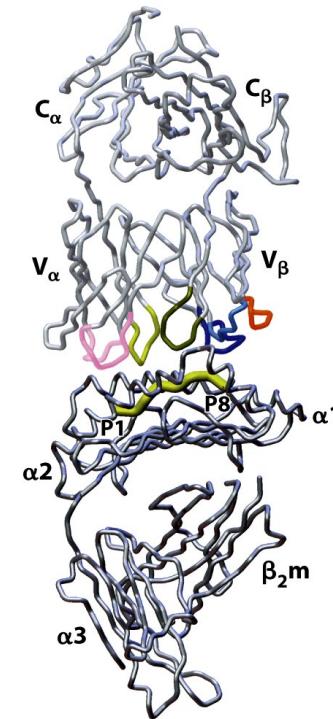


Figure 9-14b  
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## How much diversity?

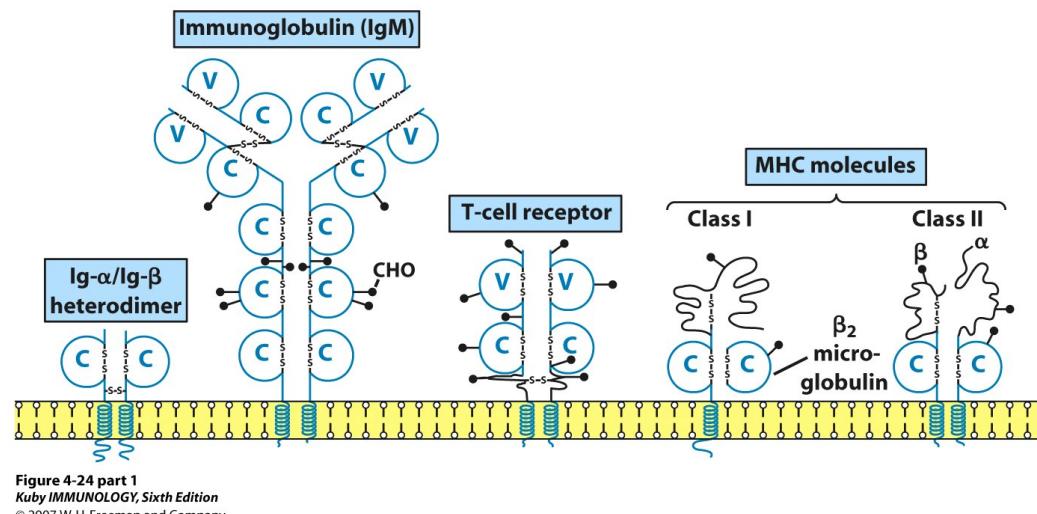


Figure 4-24 part 1  
Kuby IMMUNOLOGY, Sixth Edition  
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# How does the I.S. make a diverse set of receptors that avoids autoimmunity?

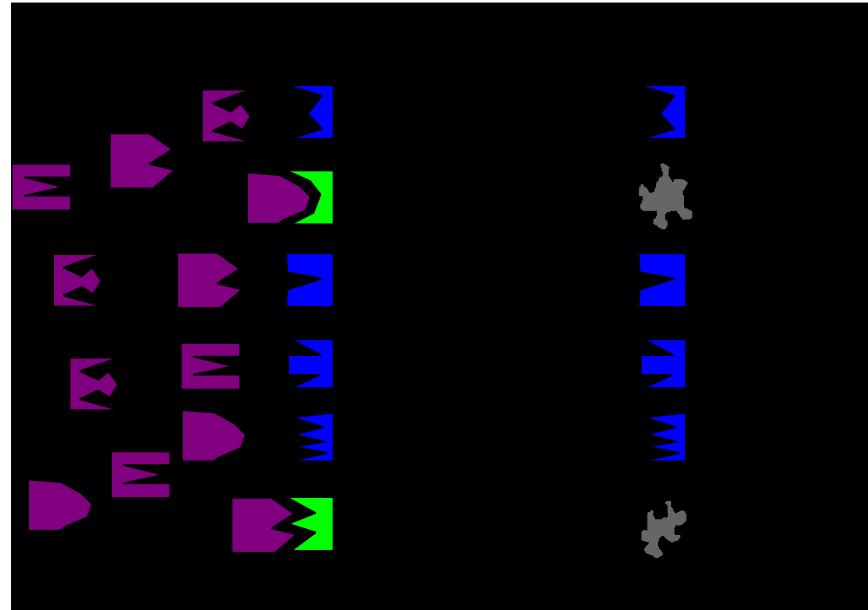
- Clonal Selection Theory
- Believed that any correct theory must explain:
  - How antigen selects correct specificity
  - Why only a single specificity is produced
  - How self tolerance is maintained
  - Why second response to same antigen is so much larger than the first



Frank Macfarlane Burnet  
Nobel Prize, 1958

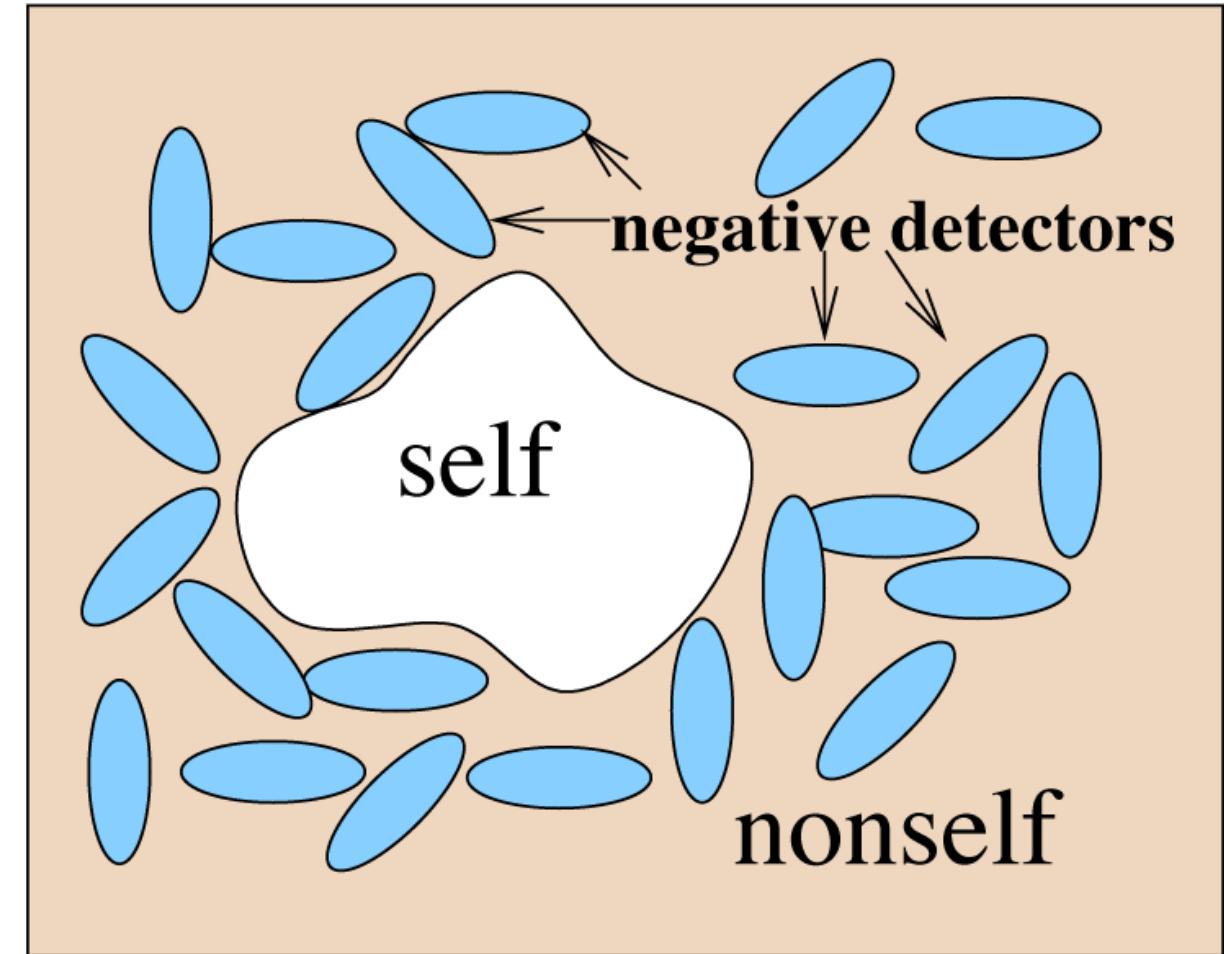
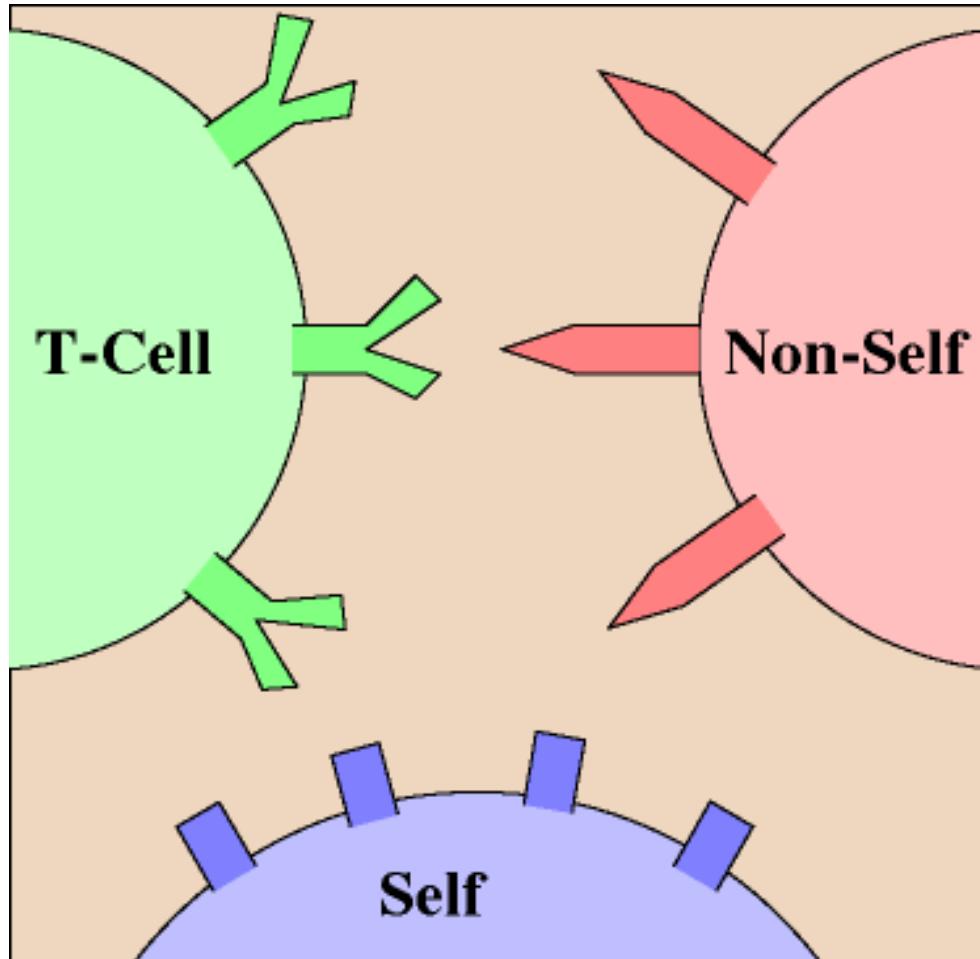
# Clonal Selection Theory

- Each lymphocyte is a unique clone with its own specificity
- Negative selection
  - If an immature lymphocyte binds  $Ag^*$ , it dies
  - Mature pool of cells represents those that did not bind to Ag during development
- A mature lymphocyte is stimulated to divide when it encounters  $Ag^*$ 
  - Clonal expansion

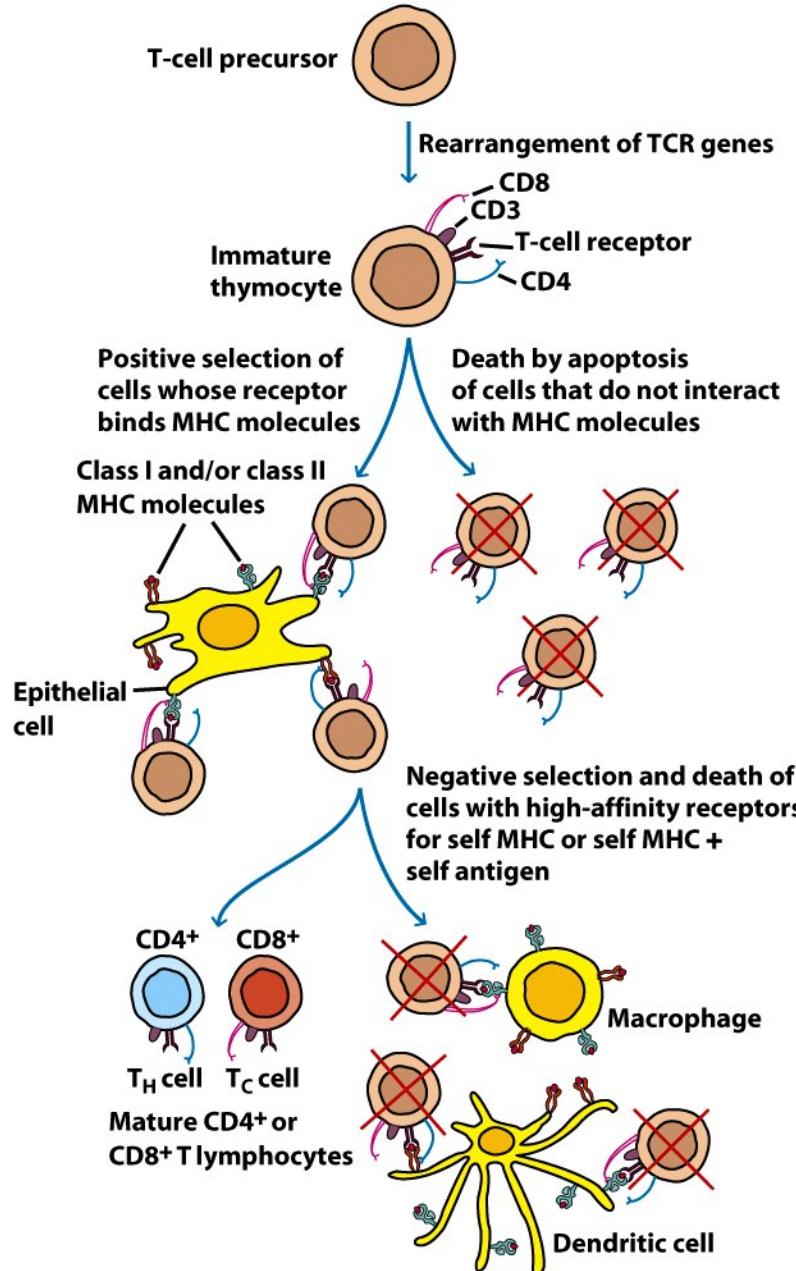


\*Ag stands for antigen.

# Negative Selection



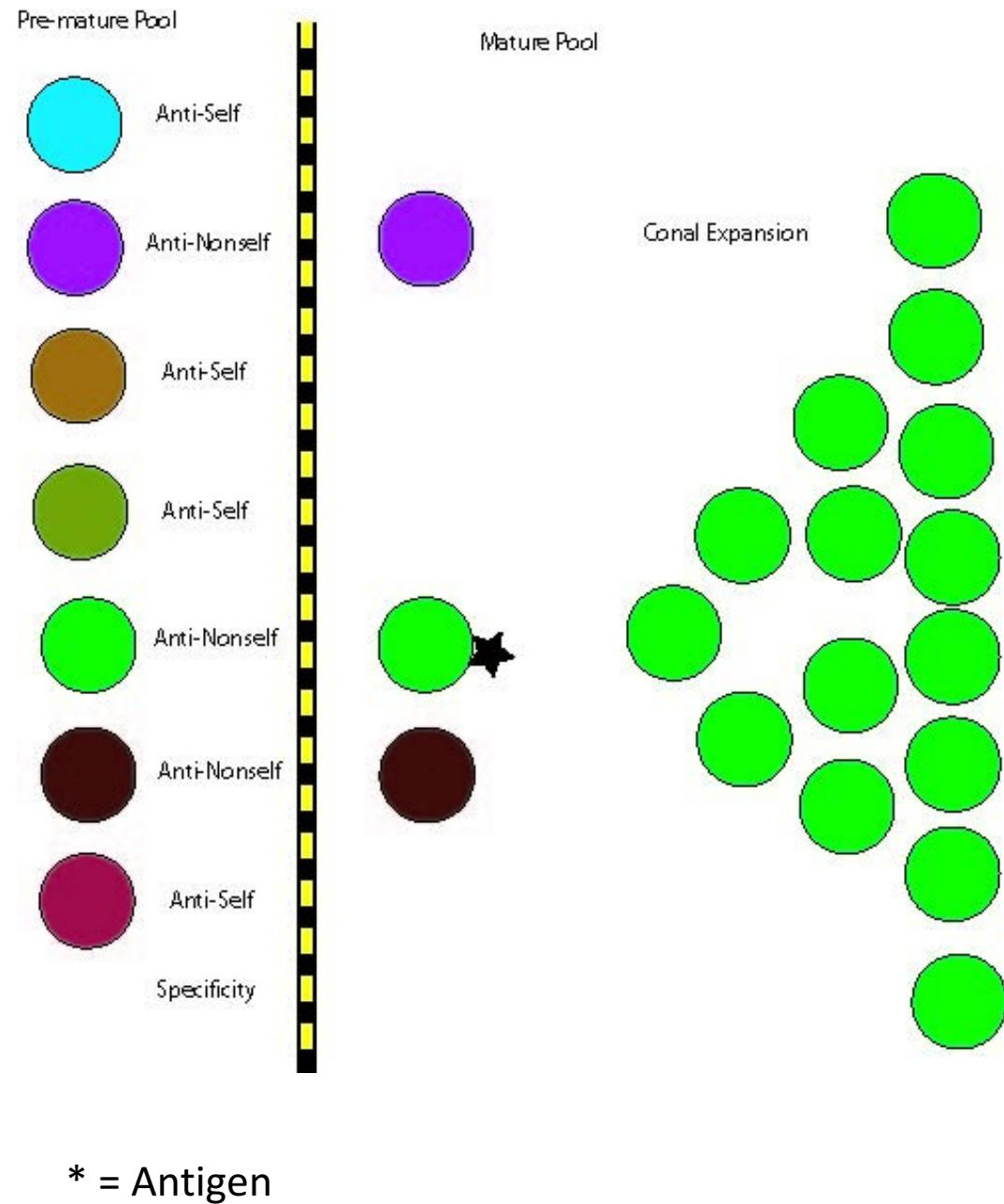
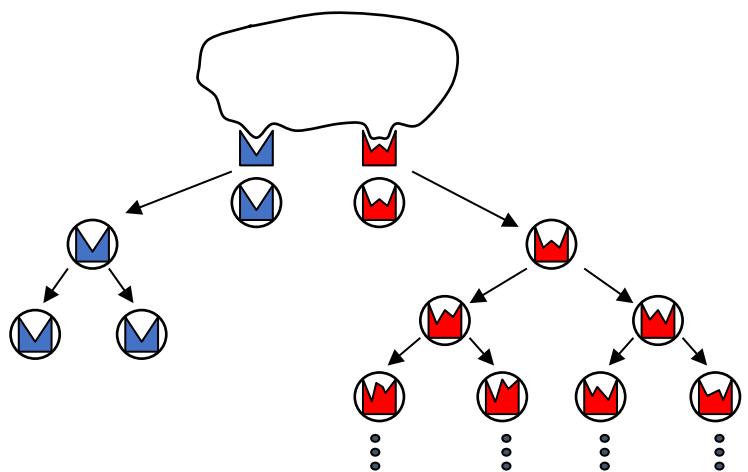
# Positive and Negative Selection



**Figure 10-6**  
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# Clonal Expansion

- B-cells compete for antigen
  - Affinity (binding strength)
  - Avidity (average affinity over all )
- Proliferation phase in LN
- Somatic hypermutation



# Managing the Immune Response

- How does the immune system know what to respond to?
- How does the immune system choose the type of response?
- How does the immune system adjust the magnitude of response?
- How does the response terminate?

- Experimentalists generally focus on the specific cell and molecule types required
- A more abstract view focuses on general pattern matching and distributed control principles

# Managing the Immune Response

- Complex network of signaling molecules, called cytokines
  - Interleukin, interferon, etc.
- Every cytokine type affects multiple cells
  - ~100 different cytokine types
- Every function (immune response) is affected by multiple cytokines
- Immune cells secrete a mixture (vector) of cytokines
- Signals are molecules, and therefore distributed (locally) by diffusion
- Signals can be subverted (e.g., viruses can evolve to avoid or interfere with cytokines, e.g., by blocking receptors), so there is an evolutionary pressure towards robust, secure networks
- Current state of knowledge
  - Many points of light
  - No systematic theory

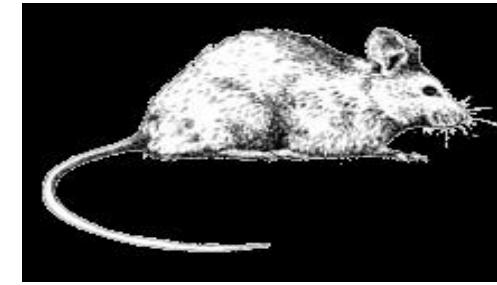
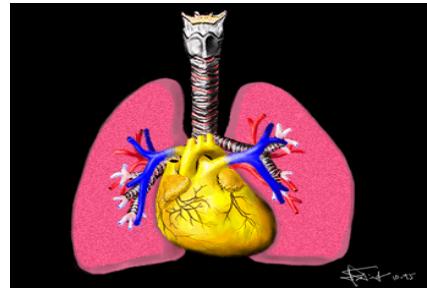
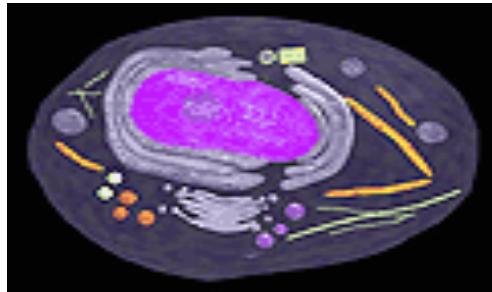
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  - Many points of light
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Compare to the foraging  
strategies of ants

# Modeling the Immune System

- Intracellular
- Organ
- Systemic

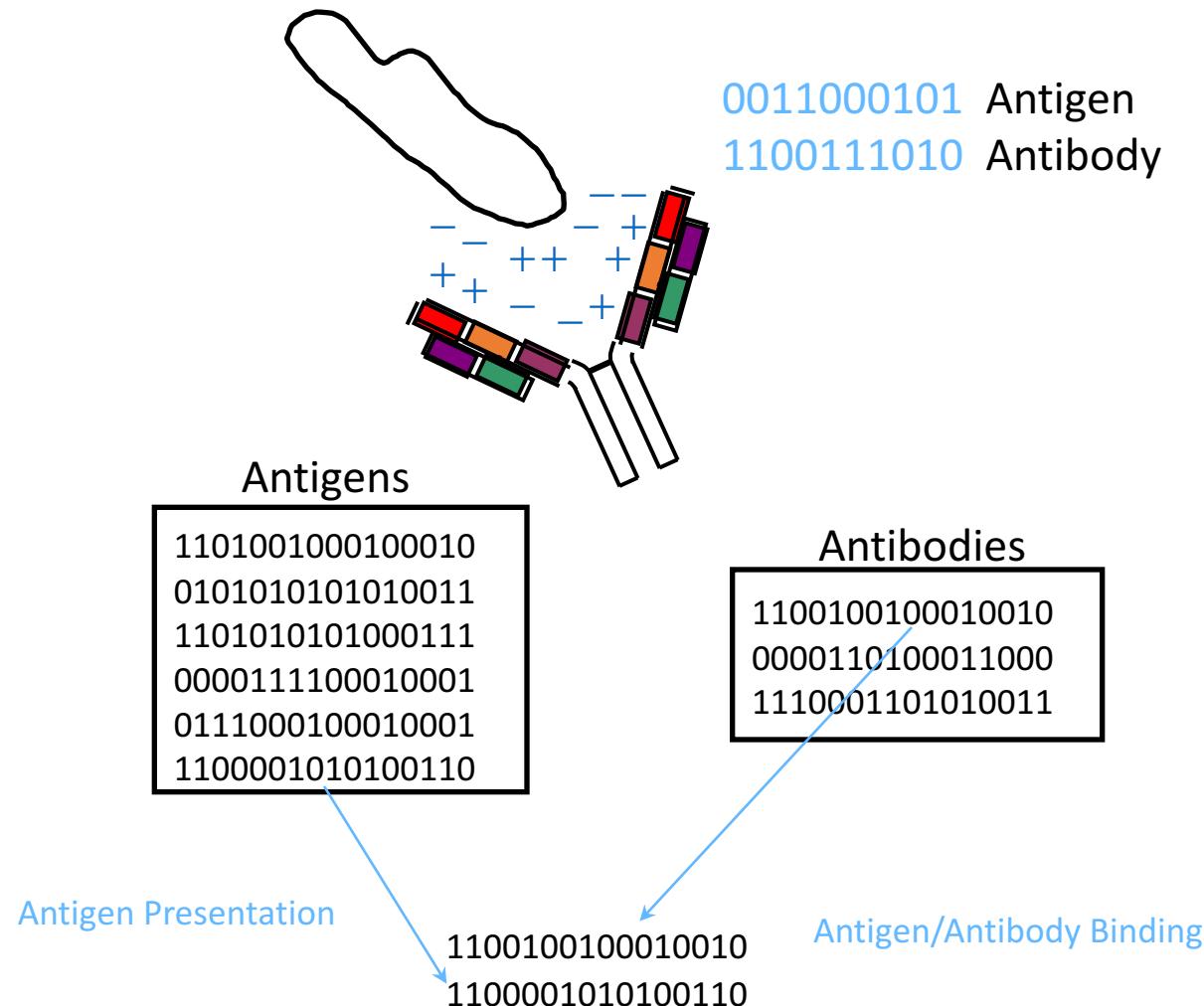


# Approaches to Modeling Immune Systems

- Differential equations
  - Each equation describes the concentration of a different antibody/cell type
- Molecular dynamics simulations
- Agent-based models
  - E.g., cellular automata, genetic algorithms, and Smith's B-cell model
- Focus on informational aspects of immune systems

# Artificial Immune Systems

# Immune System Models



# Mapping

## Immune System

- Lymphocytes (b-cells, t-cells, antibodies)
- Pathogens (antigens)
- Proteins (nucleic acids)
- Inter-molecular binding
- Antibody/pathogen binding

## Computer Science

- Detectors
- Intruders, foreign code
- Strings
- Partial string matching
- Pattern matching

# Example AIS Application Areas

- Data mining and clustering
- Computer security
- Other anomaly detection problems
- Fault isolation and tolerance
- Recommenders and filterers
- Robotics
- Data storage

Aickelin, Uwe, Dipankar Dasgupta, and Feng Gu.  
"Artificial immune systems."  
*Search Methodologies*. Springer US, 2014. 187-211.

Hofmeyr, Steven A., and Stephanie Forrest. "Architecture for an artificial immune system."  
*Evolutionary computation* 8.4 (2000): 443-473.

